



PIE Tech

POLLACHI INSTITUTE OF ENGINEERING AND TECHNOLOGY
(Approved by **AICTE** and Affiliated to **Anna University**) *sky is the limit*

Department of Electrical and Electronics Engineering

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CS3353-C Programming and Data Structures

C3353 C programming & Data Structures

①

UNIT-1 C PROGRAMMING FUNDAMENTALS

Data types - Variables - Operations - Expressions and Statements - Conditional Statements - Functions - Recursive Functions - Arrays - Single and Multi Dimensional Arrays.

Introduction:

- C is a structured Programming Language developed by a programmer Dennis Ritchie.
- It is also called as a high Level Language.
- It has small Instruction set.
- It is Case Sensitive Language.

Keywords, Variables and Constants

- Keywords are the standard words in C.
- All keywords are written in lower case. (small letters).
- Each words which have special meaning. The meaning of keywords cannot be changed.
- Some of keywords used in C are,

int	do	while	for	break	continue
double	goto	float	char	@num	
switch	void	long	short	case	

Identifiers:

- Identifier is a Collection of alphanumeric characters in which the first character must not be numeric.
- Name of the Identifier must not be the keyword.

Validity of Variable names:

- The first letter of the variable name must not be digit or any special character.
- Special characters such as \$, #, % are not allowed, except underscore (-).
- Variable name is case sensitive.
- Blank space, special characters, commas, use of quotes are not allowed.
- Arithmetic operators should not be used.
- Variable name should be Informative. It should describe the purpose of it.

EX:

Count, tax_id, INDEX, xyz

#id, 1A — Not valid.

Constants:

The specific alphabetical (or) numerical value that never gets changed during the processing of the instruction is called Constant.

EX: PI.

Comparison b/w Constant and Variable.

Constants	Variables
<ol style="list-style-type: none">1. Constant can not be changed.2. Storage location is given a name.3. <u>EX</u> $PI = 3.142$	<p>Values of the variables may be changed during processing.</p> <p>Storage location is given names.</p> <p><u>EX:</u> Name = "AAA"</p>

Header Files:

It contains standard library functions. For using these library functions directly in the program, it is necessary to include the header file at the beginning of the program.

Commonly used header files are,

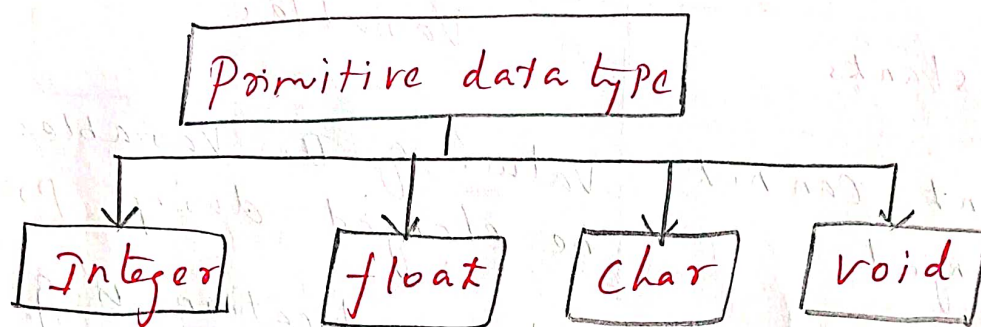
1. stdio.h - It is standard input output header file. In this file the functions for printf, scanf, fprintf, fscanf are defined.

2. conio.h - It is Console Input Output Header file. By using clrscr(), the console screen gets cleared.

3. math.h - All the functionalities related to mathematical operations are defined.

4. alloc.h - Allocating the memory dynamically.

Data types:



Integer Data type:

→ These data types are used to store whole number.

Type	Size	Range
int (or) Signed int	2	-32,768 to 32,767.
Unsigned int	2	0 to 65,535.
Short int (or) Signed short int	1	-128 to 127.
Unsigned short int	1	0 to 255.
Long int (or) Signed long int	4	-2,147,483,648 to 2,147,483,647.
Unsigned long int	4	0 to 4,294,967,295.

float Data type:

(5)

These are the data types used to store the real numbers. (i.e. number with fractional part).

Type	Size	Range
float	4	$3.4E-38$ to $3.4E+38$
double	8	$1.7E-308$ to $1.7E+308$.
long double	10	$3.4E-4932$ to $3.4E+4932$.

Char Data type

It is used to store the character value.

Type	Size	Range
Char or Signed char	1	-128 to 127.
unsigned char	1	0 to 255.

Void data type:

Void data types means no value. This data type normally associated with a function that return no value.

Expressions using Operators:

1. Arithmetic Operators

+ Addition

- Subtraction

* Multiplication.

/ Division

% Mod

2. Relational Operator

< - Less than

> - greater than

<= - less than equal to.

>= - greater than equal to.

= - Equal to

!= - Not equal to.

3. Logical operator

&& - And.

|| - Or

4. Assignment

= - Is assigned to

5. Increment

++ - Increment by one.

6. Decrement

-- - Decrement by one.

Conditional Operator

Condition ? expression 1 : expression 2

↓
True Condition

↓
False Condition.

Ex:

$a > b ? \text{true} : \text{false}.$

If a is greater than b, If yes then the value will be true. Otherwise false.

Precedence of Operator

1. Functions

6. =, <, >, <=, >=, <>

2. Power.

7. NOT

3. MOD.

8. AND

4. *, /

9. OR.

5. +, -

EX:

(7)

$$a = 3/3 * 4 + 3/8 + 3$$

$$a = 3/3 * 4 + 3/8 + 3 \quad \text{operation /}$$

$$= 1 * 4 + 3/8 + 3 \quad \text{operation *}$$

$$= 4 + 3/8 + 3 \quad \text{operation /}$$

$$= 4 + 0 + 3 \quad \text{operation +}$$

$$= 7$$

Input and Output Operations

In C inputting some data is done by `scanf` and outputting or printing the data on console is done by `printf` statement.

Syntax:

`scanf (format specifier, variables);`

EX:

`scanf ("%d", &val);`

`printf (format specifier, variables);`

EX:

`printf ("%d", val);`

Decision Making and Conditional Statement (8)

1. If Statement
2. While Statement
3. Do-While Statement
4. Switch Case "
5. For Loop

1. IF Statement:

Two types of IF Statement. They are,

Simple IF - Single statement

Compound IF - group of statement.

Types	Syntax	Example.
1. Simple if	<pre>if (condition) statement</pre>	<pre>if (a < b) printf("a is smaller than b")</pre>
2. Compound if	<pre>if (condition) { statement1; ... }</pre>	<pre>if (a < b) printf("a is smaller than b") printf("b is larger than a")</pre>
3. if... else	<pre>if (condition) statement1; else statement2;</pre>	<pre>if (a < b) printf("a is smaller than b"); else printf("a is larger than b");</pre>
4. Compound if... else	<pre>if (condition) { statement1 ... } else { statement1 ... }</pre>	<pre>if (a < b) { printf("a is smaller than b"); printf("b is larger than a"); } else { printf("a is larger than b"); printf("b is smaller than a"); }</pre>

if.. else if

if (condition)

{ statement 1;

==

} else if (condition)

{ statement 1;

==

} else

{

statement 1;

--

}

if (a < b) ⁹

printf("a is smaller than b");

else if (a < c)

printf("a is smaller than c");

else

printf("a is larger than b & c");

2. While Statement

While statement is executing repeatedly until the condition is false.

Simple While

while (condition)

{ statement

while (a < 10)

printf("a is smaller than 10");

Compound While

while (condition)

{ statement 1;

--

}

while (a < 10)

{ printf("a is less than b");

a++;

}

3. Do. While

It is used for repeated execution. Difference between while and do. while is that, while statement the condition is checked before executing any statement whereas do while statements, the statement is executed first and then condition is tested.

do. While

```
do
{
    statement;
} while (condition);
```

EX: ⁽¹⁰⁾
do int a = 0
{
 printf("a is less than 10");
 a++;
} while (a < 10);

4. Switch Case Statement

From multiple cases if only one case is to be executed at a time then switch case statement is executed.

Syntax

```
Switch (condition)
{
    case case no: statements
        break;
    default: statement
```

EX:

```
printf("Enter your choice");
switch (choice)
{
    case 1:
        printf("you selected 1");
        break;
    case 2:
        printf("you selected 2");
        break;
    default:
        printf("good bye");
}
```

5. For Loop

It is not a statement. It is a loop, using which the repeated executions of statements occurs.

Syntax

```
for (initialization; termination; step count)
    statement
```

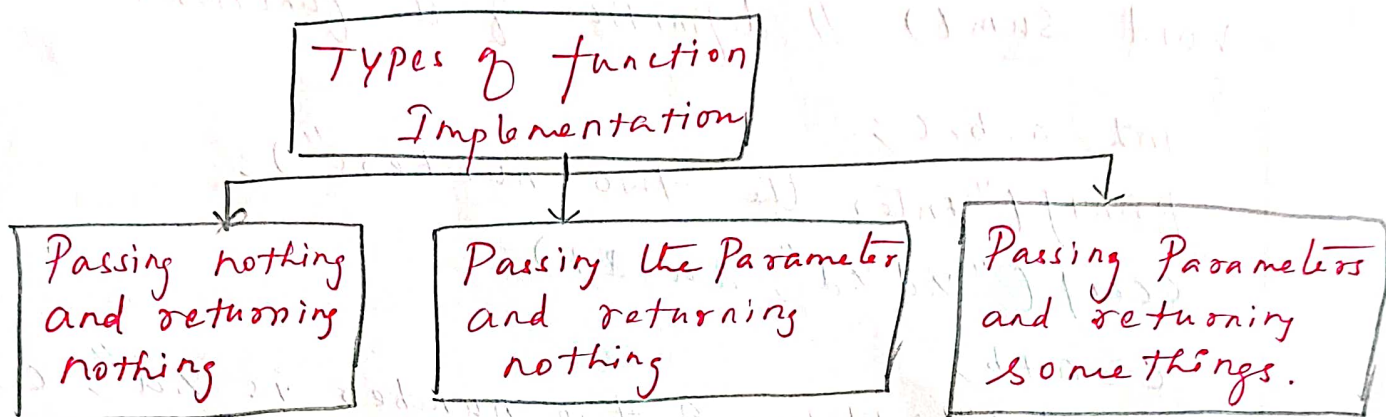
EX:

```
for (i = 0; i < 10; i++)
    c[i] = a[i] + b[i];
```


functions

(11)

If certain set of instructions is required frequently then those instructions are wrapped within a function.



Declaration of function:

Syntax:

Return-type Function-name (Data-type Parameter)

Definition of function:

Syntax:

Return-type Function-name (Data-type Parameters)

{

// body of function.

}

Call the function:

Syntax:

function-name (Parameters);

EX:

```
void main()
{
    void sum(); // declaration of function.
    sum(); // call the function.
}

void sum() // definition of the function.
{
    int a, b, c;
    printf("Enter the two numbers");
    scanf("%d %d", &a, &b);
    c = a + b;
    printf("Addition of two number is %d", c);
}
```

Parameter Passing Method:

TYPE 1: Passing nothing and Returning nothing.

EX:

```
void main()
{
    void sum();
    sum();
}

void sum()
{
    int a, b, c;
    printf("Enter the two numbers");
    scanf("%d %d", &a, &b);
    c = a + b;
    printf("Addition of two numbers is %d", c);
}
```

→ In above example no parameter is passed and there is no return value from the function. (13)

→ Void data indicates that the function is return nothing.

TYPE 2: Passing the Parameter and returning Nothing

EX:

```
main()
```

```
{
```

```
    int a, b;
```

```
    void sum (int a, int b);
```

```
    printf("Enter two numbers");
```

```
    scanf("%d %d", &a, &b);
```

```
    sum(a, b);
```

```
}
```

```
void sum (int x, int y)
```

```
{
```

```
    int c;
```

```
    c = x + y;
```

```
    printf("Addition is %d", c);
```

```
}
```

Here Parameter a, b are passed.

Two methods of parameter Passing.

1. Call by Value

2. Call by Reference.

Difference between Call by Value & Call by Ref.

Call By Value

1. When a function is called, then in that function actual values of the parameters are passed.

2. The Parameters are simple variables.

3. Compiler executes this type of function slowly as values get copied to formal parameters.

4.

```
main()
{
    x=10;
    fun(x);
    printf("%d", x);
}
void fun(x)
{
    x=15;
}
o/p is 10
```

Call By Reference

When a function is called, then in that function addresses of the parameters are passed.

The parameter are pointer variables.

Compiler executes this type of function faster as addresses get copied to the formal parameters.

```
main()
{
    *x=10;
    fun(x);
    printf("%d", *x);
}
void fun(x)
{
    x=15;
}
o/p is 15.
```

TYPE 3: Passing the parameters and returning

EX:

```
void main()
{
    int a, b, c;
    int Sum(int, int)
```

```
printf ("Enter two numbers");
scanf ("%d %d", &a, &b);
c = sum(a, b);
printf ("The Addition is = %d", c);
}
int sum()
{
    c = a + b;
    return c;
}
```

- 1) Write a C program to interchange two variables without using third variables.

```
#include <stdio.h>
void main()
{
    int a = 11;
    int b = 20;
    a = a + b; 31
    b = a - b; 11
    a = a - b; 20
    printf ("In a = %d b = %d", a, b);
}
```

- 2) Write a C program to get two numbers and exchange these numbers using pass by value and pass by reference.

```
#include <stdio.h>
void swap-by-value (int a, int b)
{
    int temp;
    temp = a;
    a = b;
    b = temp;
}
```


void swap-by-ref (int *a, int *b)

{ int temp;

temp = *a;

*a = *b;

*b = temp;

}

int main()

{ int x, y;

printf("Enter first number:");

scanf("%d", &x);

printf("Enter second number:");

scanf("%d", &y);

printf("Before Swapping x=%d and y=%d", x, y);

Swap-by-value (x, y) // Call by value.

printf("After swapping x=%d and y=%d", x, y);

printf("Before Swapping x=%d and y=%d", x, y);

Swap-by-ref (&x, &y); // Call by reference

printf("After swapping x=%d and y=%d", x, y);

}

Recursive Functions

Recursion is a programming technique in which the function calls itself repeatedly for some input.

Properties of Recursion:

(17)

1. There must be at least one condition in recursive function which do not involve the call to recursive routine. This is called base case property.
2. Each recursive call must reduce to some manipulation and must go closer to base case condition.

EX:

```
if (n == 0)
```

```
    return 1;
```

```
else
```

```
    return n * fact(n-1);
```

Write a C program to find factorial of a number using recursive function.

```
#include <stdio.h>
```

```
void main (void)
```

```
{  
    int n, f;
```

```
    int fact (int n);
```

```
    printf ("Enter the number");
```

```
    scanf ("%d", &n);
```

```
    f = fact(n);
```

```
    printf ("The factorial of %d is %d, n, f);
```

```
}
```


int fact (int n)

{ int x, y;

~~if (n < 0)~~

if (n == 0)

return 1;

x = n - 1;

y = fact(x);

return (n * y);

}

GCD (Greater Common Divisor)

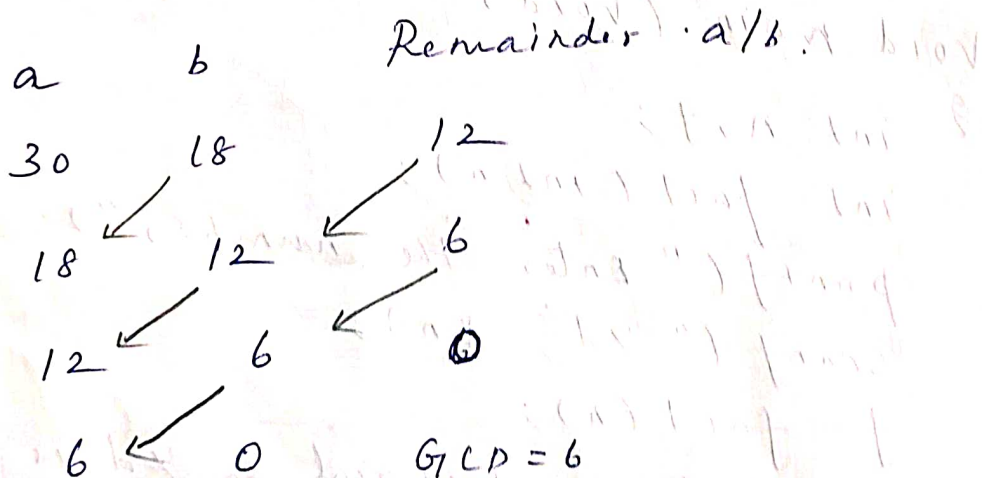
GCD is calculated using following function.

$$\boxed{\text{gcd}(a, b) = \text{gcd}(b, a \bmod b)} \quad \text{if } a > b.$$

$$\text{gcd}(a, 0) = a$$

Ex:

Consider two numbers 30 and 18.



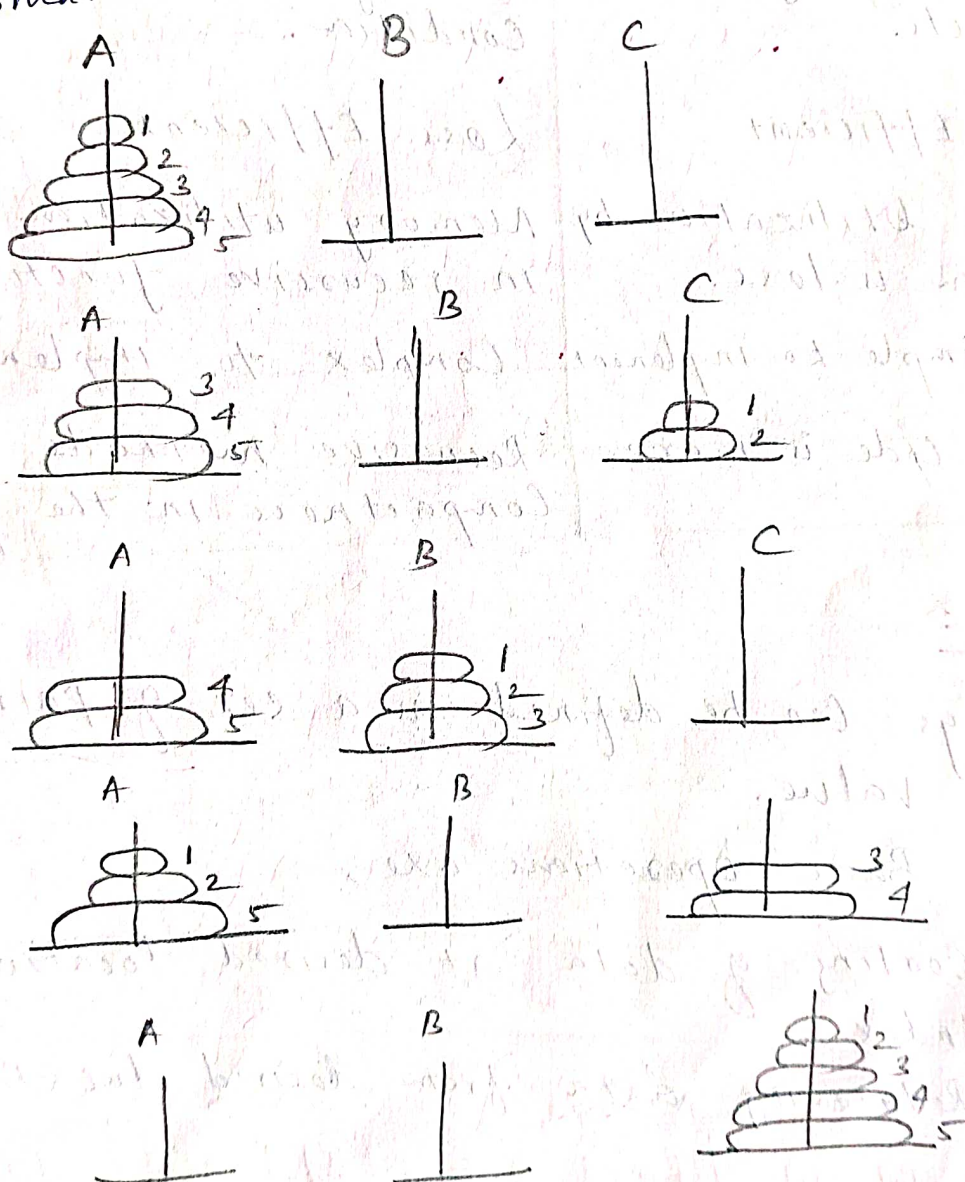
Tower of Hanoi

(19)

"Tower of Hanoi" states that the move the five disks from peg A to peg C using peg B as a Auxillary.

Conditions are,

1. Only the top disk on any peg may be moved to any other peg.
2. A larger disk should never rest on the smaller one.



Comparison b/w Iteration and Recursion

Iteration	Recursion
1. Iteration is a process of executing certain set of instructions repeatedly, without calling the self function.	Recursion is a process of executing certain set of instructions repeatedly by calling the self function repeatedly.
2. It is implemented with the help of for, while, do-while programming constructs.	It is obtained by calling the same function again and again over some condition.
3. More Efficient	Less Efficient.
4. Memory utilization by iteration is less.	Memory utilization is more in recursive functions.
5. It is simple to implement	Complex to implement.
6. Line of code is more	Recursive methods bring compactness in the program.

Arrays:

→ Arrays can be defined as a set of pair-index and the value.

→ Two Basic operations are,

(i) Storing of data at desired location or index.

(ii) Retrieving data from desired location.

a[0]	a[1]	a[2]	a[3]	a[4]	a[5]	a[6]	a[7]	a[8]	a[9]
10	20	30	40	50	60	70	80	90	100

Advantages of Array.

(21)

1. Elements can be retrieved or stored very efficiently in array with the help of index or memory location.
2. All the elements are stored at continuous memory location. Hence searching of elements from sequential organization is easy.

Disadvantages of Array.

1. Insertion and deletion of elements become complicated due to sequential nature.
2. Memory fragmentation occurs if we remove the elements randomly.

Syntax:

```
data-type name-of-array [size];
```

Ex:

```
int a[10];
```

Initialization:

It is possible to initialize an array during declaration only. for example.

```
int a[10] = {0, 1, 2, 3, 4, 5, 6, 7, 8, 9};
```

Types:

1. Single Dimensional Array.
2. Two Dimensional Array.

Single Dimensional Array

(22)

0	10
1	20
2	30
3	40
4	50
5	60
6	70
7	80
8	90
9	100

Index
of
Array

Here $a[2] = 30$.

$a[8] = 90$.

Program.

```
#include <stdio.h>
```

```
main()
```

```
{
```

```
    int a[10], index;
```

```
    printf("Elements in an Array a");
```

```
    for(index=0; index<=9; index++)
```

```
        scanf("%d", &a[index]);
```

```
    printf("You have stored these numbers  
           in the array");
```

```
    for(index=0; index<=9; index++)
```

```
        printf("%d", a[index]);
```

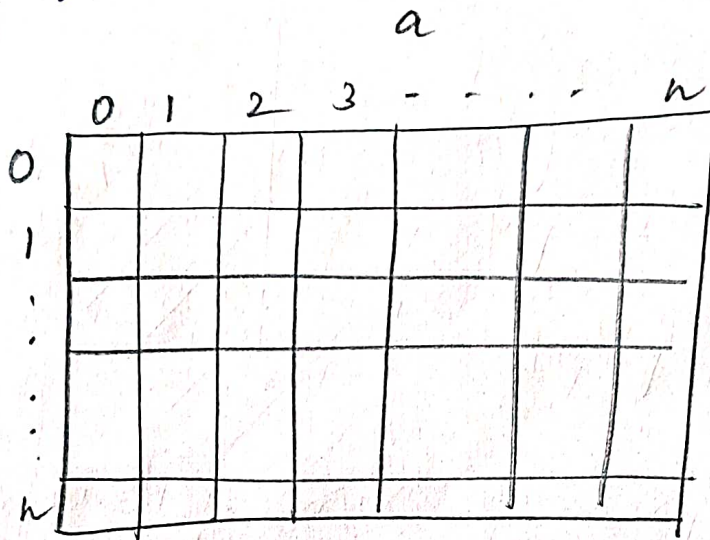
```
}
```

Two Dimensional Arrays:

(29)

→ It is something which you can compare with the two storied building!

→ Extra space which is arranged in rows and columns.



Syntax:

Data-type Name-of-Array [row-size] [column-size];

Ex:

```
int a[10][10];
```

```
for (i=0; i<=2; i++)
```

```
{ for (j=0; j<=2; j++)
```

```
{ scanf("%d", &a[i][j]);
```

```
}
```

```
}
```


Unit-II C programming - Advanced Features. ①

Structures - Union - Enumerated Data types -
Pointers - Pointers to Variables, Arrays and
Functions - File Handling - Preprocessor Directives.

Structures:

→ A Structure is a group of items in which each item is defined by some identifiers. These items are called members of the structure.

→ Structure is a collection of various data items which can be ~~defined~~ of different data types.

Syntax:

```
struct name  
{  
    member1;  
    member2;  
    ...  
    member n;  
};
```

Example:

```
struct stud.  
{  
    int roll-no;  
    char name[10];  
    float marks;  
};  
struct stud stud1, stud2;
```

Instead of struct we
use typedef.

Comparison between Arrays and Structures.

(2)

Array	Structure
1. Array is a Collection of similar type of elements.	Structure is a Collection of Variety of elements which can be of different datatypes.
2. Array elements can be accessed by the index placed within [].	Structure elements can be accessed with the help of . (dot) operator.
3. To represent an array, array name is followed by [].	To represent structure a keyword struct has to be used.
4. <u>EX:</u> <pre>int a[20];</pre>	<u>EX:</u> <pre>struct student { int roll-no; char name[20]; }</pre>

Initializing Structure

There are 3 ways by which structure can be defined.

1.

```
struct student {  
    int roll-no;  
    char name[10];  
    float marks;  
} s1;
```

2.

```
struct student {  
    int roll-no;  
    char name[10];  
    float marks;  
};  
struct student s1;
```

3.

```
typedef struct student  
{  
    int roll-no;  
    char name[10];  
    float marks;  
} s;  
s, s1;
```


Array of structures

Structure is used to store information of one particular object and if one has to store large number of such objects then array of structure is used.

Union

Union is a user defined data structure which is just similar to structure. It is used to store members of different data types.

Ex:

```
union Employee
{
    int empid;
    char empName[30];
};
```

Difference between structure and Union.

Structure	Union
1. The keyword struct is used to define the structure.	The keyword union is used to define Union.
2. All the members of structure can be accessed at a time.	Only one member of union is accessible at a time.
3. The memory is allocated for each member of the structure.	One block of memory is used by all the members of union.
4. One or more members of structure can be initialized at once.	A union may only be initialized with a value of the type of its first member.
5. It takes more memory.	Less memory.

Enumerated Data types

The enum is an abbreviation used for enumerated data type.

Syntax:

```
enum identifier-name { sequence of items };
```

Ex:

```
enum fruit { Mango, Orange, Banana, Grapes };
```

Here mango = 0, Orange = 1, Banana = 2, Grapes = 3.

Pointers

→ Pointers is a variable that represents the memory location of some other variable.

→ purpose of pointer is to hold the memory location and not the actual value.

Advantage of Pointers

data type * ptr name;

→ It allow the dynamic memory management.

→ It helps to return more than one values from the function.

→ It allows to pass arrays, strings and structures efficiently.

→ It provides direct access to memory.

→ It improve the execution speed of program.

→ It help to build the complex data structures.

Initialization.

→ Once the pointer variable is declared then it can be used further.

→ pointer variable is basically used to store some address of the variable which is holding some value.

Consider,

```
int *ptr;
```

```
int a, b;
```

```
a = 10;
```

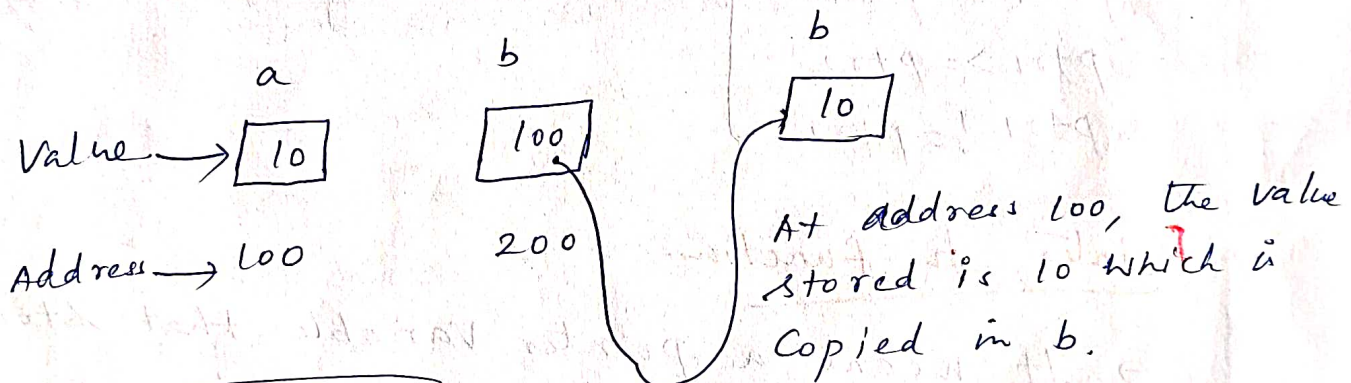
```
ptr = &a;
```

```
b = *ptr;
```

Here,

* means Content at the specified address.

& means address at.



```
a = 10  
ptr = &a.  
b = *ptr.
```

Pointer Arithmetic

Pointer Arithmetic is a method of calculating the address of an object with the help of arithmetic operations on pointers.

Operation

$$x = *ptr1 * *ptr2$$

$$x = ptr1 - ptr2$$

$$ptr1 -- \text{ or } ptr1 ++$$

$$x = ptr1 + 10$$

$$x = ptr1 - 20$$

$$ptr1 < ptr2$$

$$ptr1 = ptr2$$

$$ptr1 \leq ptr2$$

$$ptr1 \geq ptr2$$

$$ptr1 \neq ptr2$$

Meaning

Multiplication.

Subtraction.

Incremented or decremented

We can add some constant to pointer variable.

Subtract

Relational operations are possible on pointer variable

Pointer to function.

→ It means a pointer variable that stores the address of function. The function has an address in the memory same like variable.

Syntax:

`Return-Type * Pointer-variable (data-type);`

Ex:

`float(*fptr)(float);`

File Handling:

(8)

- file is a Collection of records.
- file of size n has n records in sequence where each record is a collection of one or more fields.

Ex:

Rollno	Name	Marks
1	John	66
2	Mathew	70
3	Steve	60.

Classification of file.

There are two types of files.

1. Text file.
2. Binary File.

- Text files are files in which textual information may be stored with essentially no formatting.
- Binary files in which any type of data encoded in binary form. The Binary files contain the binary digits. That means it contains the sequence of 1's and 0's.

Comparison between Text File and Binary File.

<u>Text file</u>	<u>Binary file</u>
1. Text files contains plain text data.	Binary File contain the data in binary form.
2. The text file does not contain the graphical data.	Binary file can store the data such as text, graphics, images and sound.
3. Text files can be directly read and interpreted.	Binary files can not be read directly.
4. Text files are not executable files.	Binary files can be executable files.

File operations

(9)

1. Creating a file / opening a file

Syntax:

```
file pointer = fopen ("filename", "mode");
```

Where,

→ filename is the name of file you want to create or open.

→ mode can be,

read - "r"

write - "w"

append - "a".

Ex:

```
fp = fopen ("student.dat", "w");
```

2. Closing the file

Syntax:

```
fclose (filepointer);
```

Ex:

```
fclose (fp);
```

3. Setting the pointer to start of file

Syntax:

```
rewind (filepointer);
```

Ex:

```
rewind (fp);
```


4. Writing a character to file

Syntax:

```
fputc (character, filepointer);
```

Ex:

```
fputc (ch, fp);
```

5. Reading a character from file

Syntax:

```
fgetc (filepointer);
```

EX:

```
char ch;
```

```
ch = fgetc (fp);
```

6. Writing string to file.

Syntax:

```
fputs (string, filepointer);
```

EX:

```
fputs (s, fp);
```

7. Reading string from file

Syntax:

```
fgets (stringaddress, length, filepointer);
```

EX:

```
char s[80];
```

```
fgets (s, 79, fp);
```

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8. Writing of characters, strings, integers, float to file

Syntax:

fprintf (file pointer, "format string", list of
Variable)

9. Reading of variables from file:

Syntax:

fscanf (file pointer, "format string", list of address
of variables);

Ex:

```
fscanf (fp, "x.d x.s", &no, &name);  
printf ("Read data is x.d x.s", no, name);
```

10. Writing Contents to file through structure:

Syntax:

fwrite (pointer to struct, size of struct,
no of data items, file pointer);

11. Reading Content of file through structure:

Syntax:

fread (pointer to struct, size of struct, no of
data items, file pointer);

Ex:

```
fread (&s, sizeof(s), 1, fp);
```


Detecting End of file

The end of file is detected using a macro EOF (End of file) When this condition occurs then we should not read the contents further.

EX:

```
#include <stdio.h>
```

```
void main()
```

```
{ FILE *fp;
```

```
char c;
```

```
fp = fopen("Exy.c", "r");
```

```
c = getc(fp);
```

```
while (c != EOF)
```

```
{ putchar(c);
```

```
c = getc(fp);
```

```
}
```

```
fclose(fp);
```

```
}
```

Sequential File Organization

We want to store the marks of 10 students in a file. We will organize the file in following manner.

Record Number	University Seat no	Name of Student	Marks
1			
2			
3			
...			
10	--	--	--

Preprocessor Directives

→ It is a separate step applied on the source file before presenting it to compilation process.

→ C preprocessor is a text substitution tool. It instructs the compiler to do all the necessary preprocessing before and after the compilation.

→ preprocessor directive is written at the beginning of the program with the # proceed to:

<u>Preprocessor</u>	<u>Syntax and Description.</u>
1. Macro	#define. This macro defines constant value and can be any of basic data type.
2. Header file inclusion	#include <file-name>.
3. Conditional Compilation.	#ifdef, #endif, #if, #else, #ifndef.
4. Other directives	#undef, #pragma.

EX:

- #define SIZE 10.
This directive tells the compiler to replace the instance of SIZE with 10.
- #include <stdio.h>
This directive tells to get `stdio.h` from system libraries and add the text to the current source file.

2. `#include "myfile.h"`

This line tells the Compiler to get `myfile.h` from local director and add the contents with the current source file.

4. `#undef F_SIZE.`

`#define F_SIZE 80.`

It tells to undefine existing `F_SIZE` and define it as 80.

5. `#ifndef MSG.`

`#define MSG "Welcome".`

`#endif.`

It tells to define `MSG` only if `MSG` isn't already defined.

Linear Data Structures - LIST

1) Data Structure:

⇒ The way of organizing data structure is called data structures.

Types of data structures are;

⇒ Array, stack, queue, linked list, Tree, ~~Queue~~ ^{Graph}

2) Abstract data types (ADTs):

(*) An ADT is a mathematical model of a data structure.

Eg: Lists, sets, and Graphs.

1) LIST ADT: A list is a dynamic collection of items (or) elements.

$E_1, E_2, E_3, \dots, E_n$ of size 'n' arranged in linear sequence.

A list is a size zero or with no elements.

List operations:

① Insert (x, L)

② Delete (x, L)

③ Find (x, L)

④ Make empty (L)

⑤ previous (x, L)

⑥ Next (x, L)

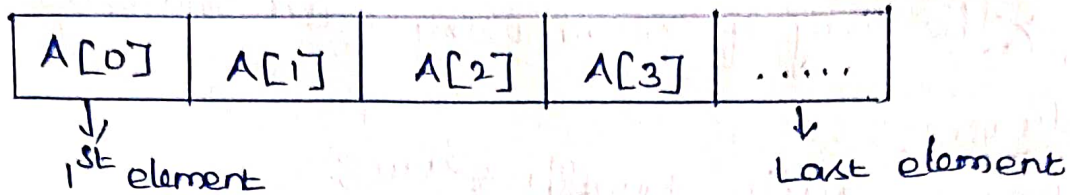
Implementation of List ADT

Array based Implementation

Linked list based Implementation

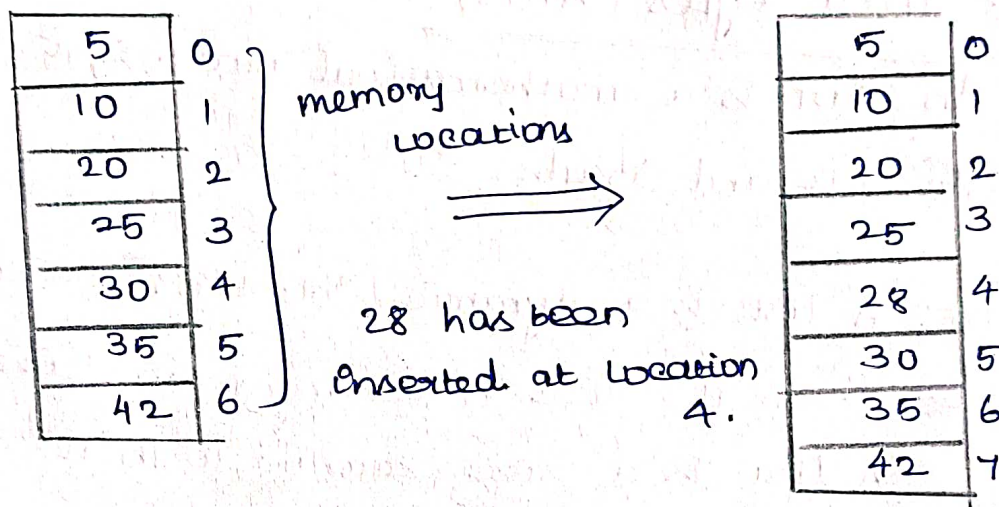
3) Array based Implementation (N/D-2018)

An array is a DS which can store a fixed sequential collection of elements of the same type.

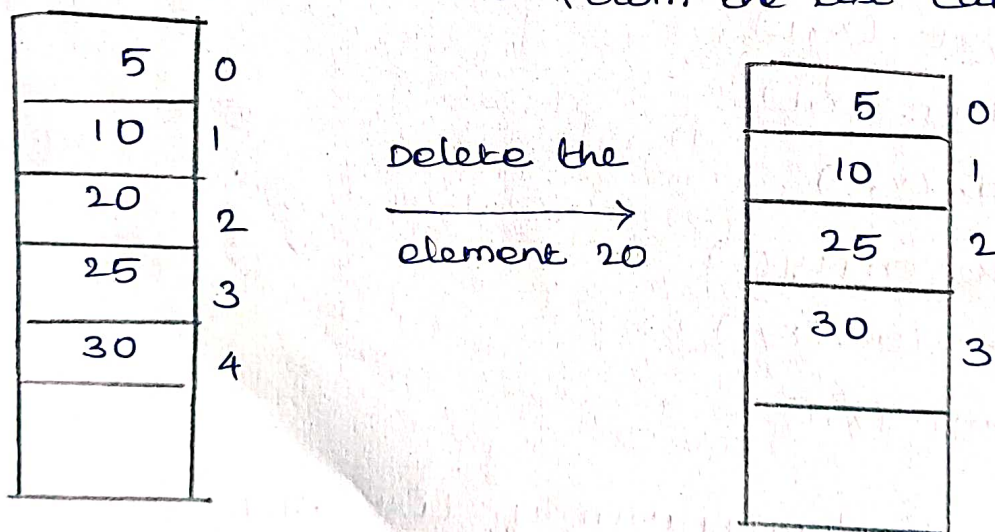


Operations:

① **Insertion:** List of size 'n'.



② **Deletion:** Element from the list can be removed.



3) **Print:** Print operation is used to display all elements in list.

4) **Find:** Find operation searches for a particular element in the list.

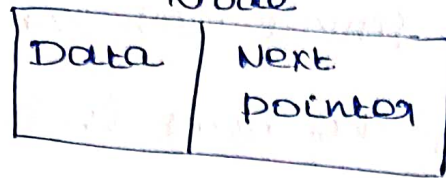
1) Linked list Implementation: [N/D - 2019]

(2)

It is a linear data structure which is a collection of nodes.

Two parts

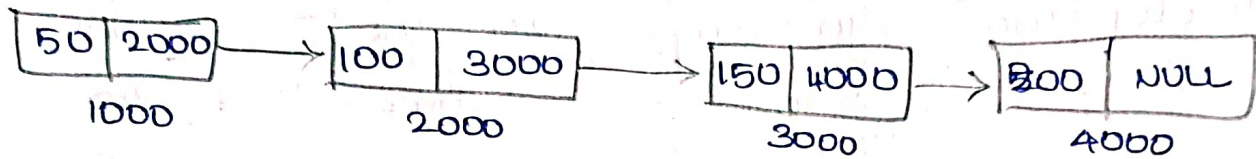
Node



Data field - element

Next pointer field - address of next node.

Eg:



Advantages: [A/M - 2019]

- (*) Dynamic DS
- (*) Size is not fixed.
- (*) Easy operations.

Types of Linked list:

- 1) Singly linked list
- 2) Doubly linked list
- 3) Circularly linked list

Representation:

struct node

{

int data;

struct node *next;

};

5) Singly linked list: [N/D-2019]

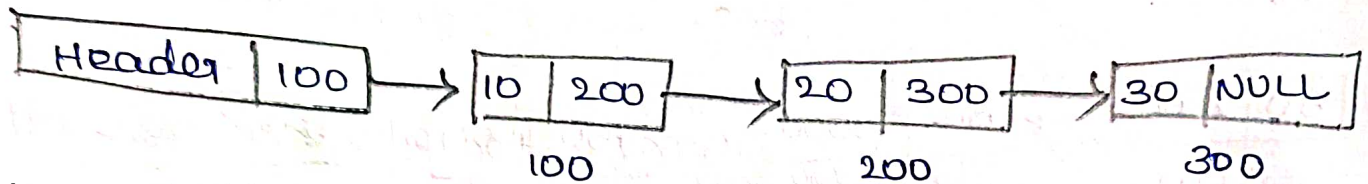
→ Linear data structure.

→ Collection of nodes.

→ Every node linked with some sequential node.

→ Header of the next is linked with next node.

Eg:



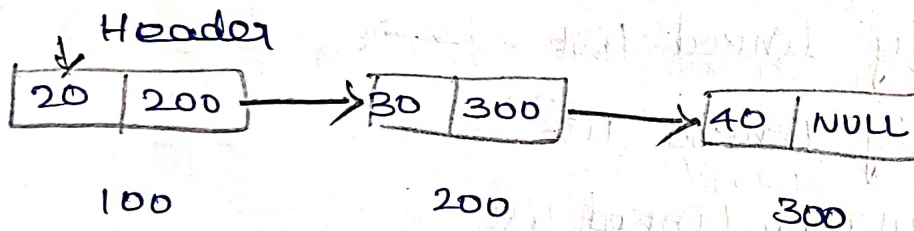
Operations:

① Insertion: [N/D-2021]

Three ways of Insertion.

① Insertion a node at first place:

Inserting a new node at first position of existing singly linked list.



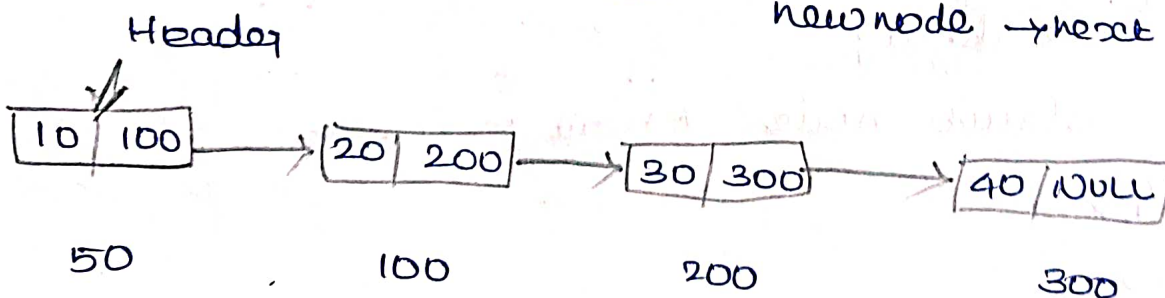
new node = malloc (size of (struct node)),

10 | NULL

New node.

new node → data = 10

new node → next = NULL



New node

2) Insert a node at Last place:

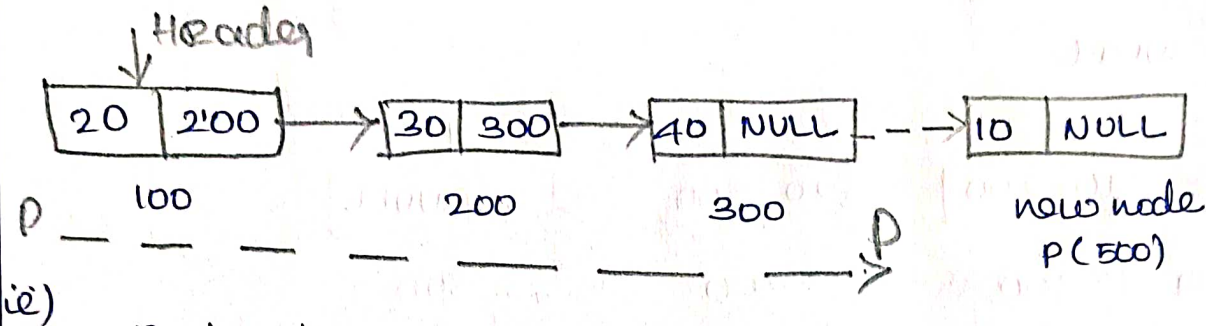
(3)

10 | NULL

new node

newnode \rightarrow data = x

newnode \rightarrow next = NULL

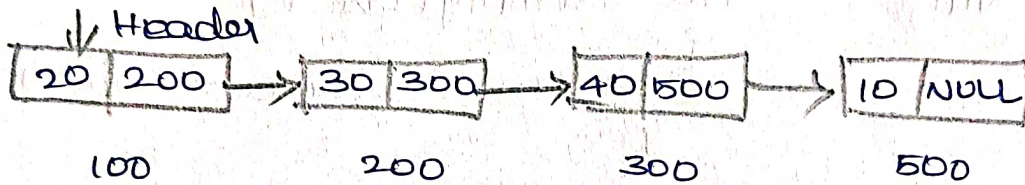


ie)

p = header

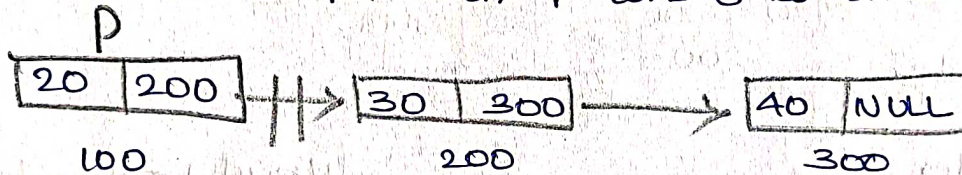
find last position

p \rightarrow next = newnode.



3) Insert a node in an Intermediate place:-

find position P where to insert.



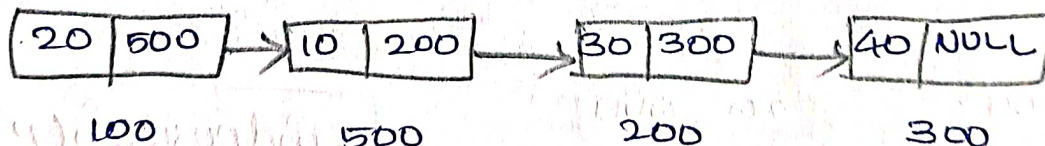
10 | NULL

500 (new node)

Now,

new node \rightarrow next = p \rightarrow next

p \rightarrow next = newnode.

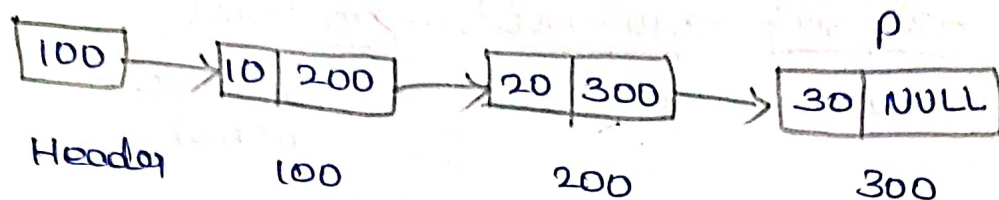


② Find operation: find the position of search

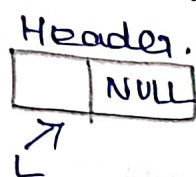
(i) find;

(ii) find previous

(iii) find next



3) check whether the list is empty:

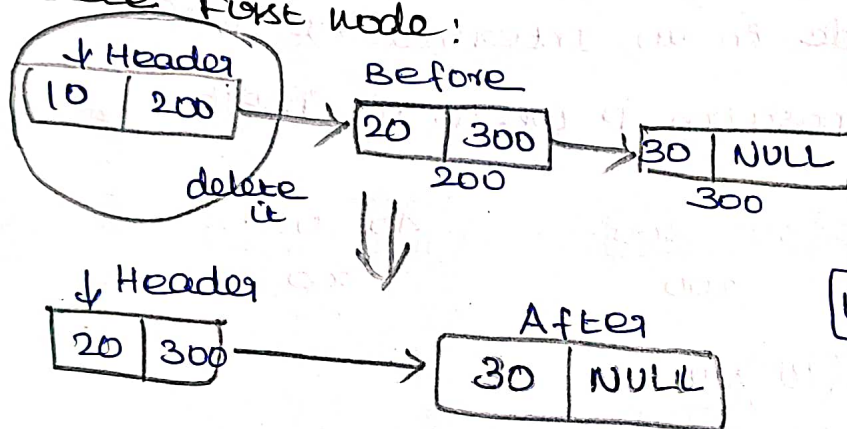


bool isEmpty(List L)

{ return (L → next == NULL)

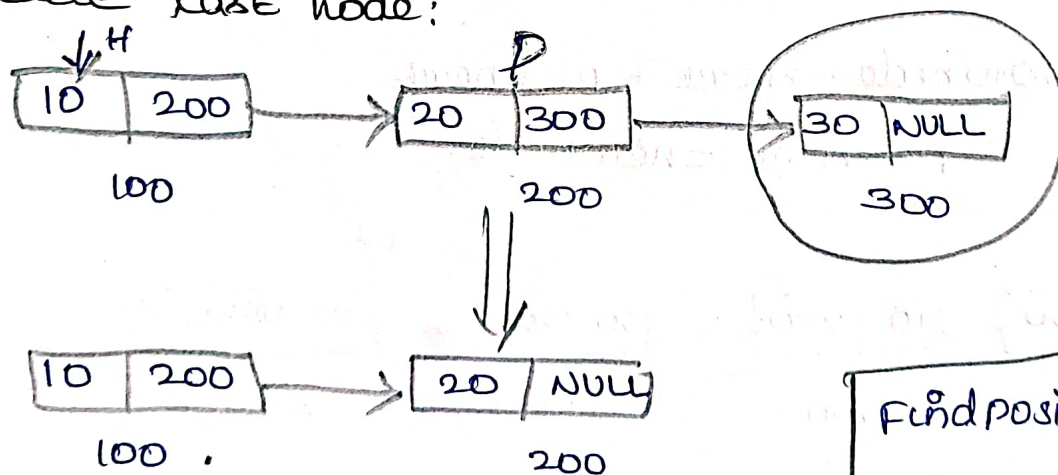
4) Delete operation: Remove the node from List.

(i) Delete First node:



Header → header → next

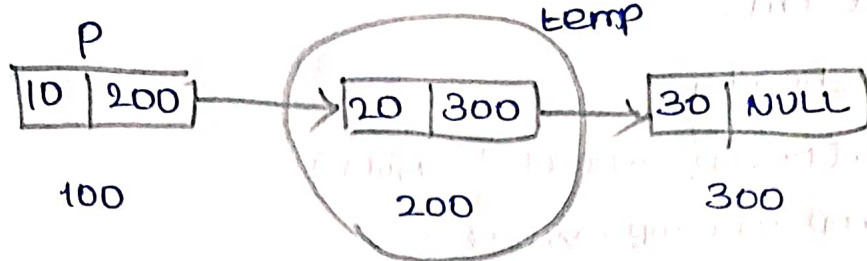
ii) Delete Last node:



Find position (p)

p → next = NULL

ii) Delete Intermediate node:



Find previous (X, L)

$p \rightarrow \text{next} = \text{temp} \rightarrow \text{next}$

free temp.

6) Doubly Linked List:

(*) Linear Linked List - Linear DS.

Three fields are:

- ⇒ Previous Address field
- ⇒ Data field
- ⇒ Next Address field



Node

Operations:

(i) Creation: New node creation.

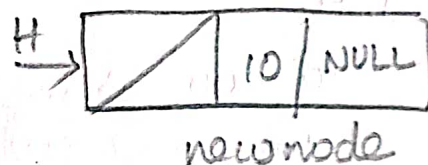
struct dnode

{ int data;

struct dnode *prev;

struct dnode *next;

};



(ii) Insertion:

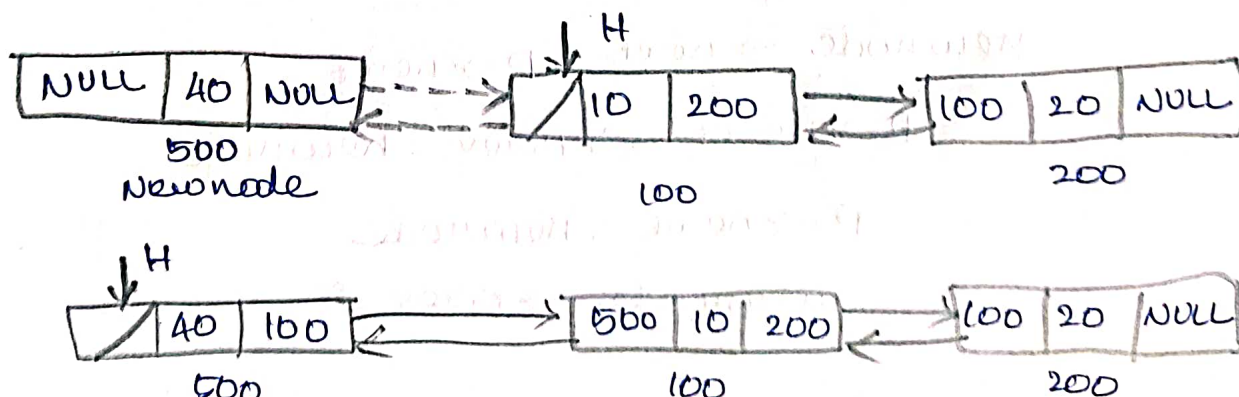
1) Insert a node at beginning:

$\text{newnode} \rightarrow \text{next} = \text{header};$

$\text{header} \rightarrow \text{prev} = \text{newnode};$

$\text{header} = \text{newnode};$

eg:



2) Insert a node at end:

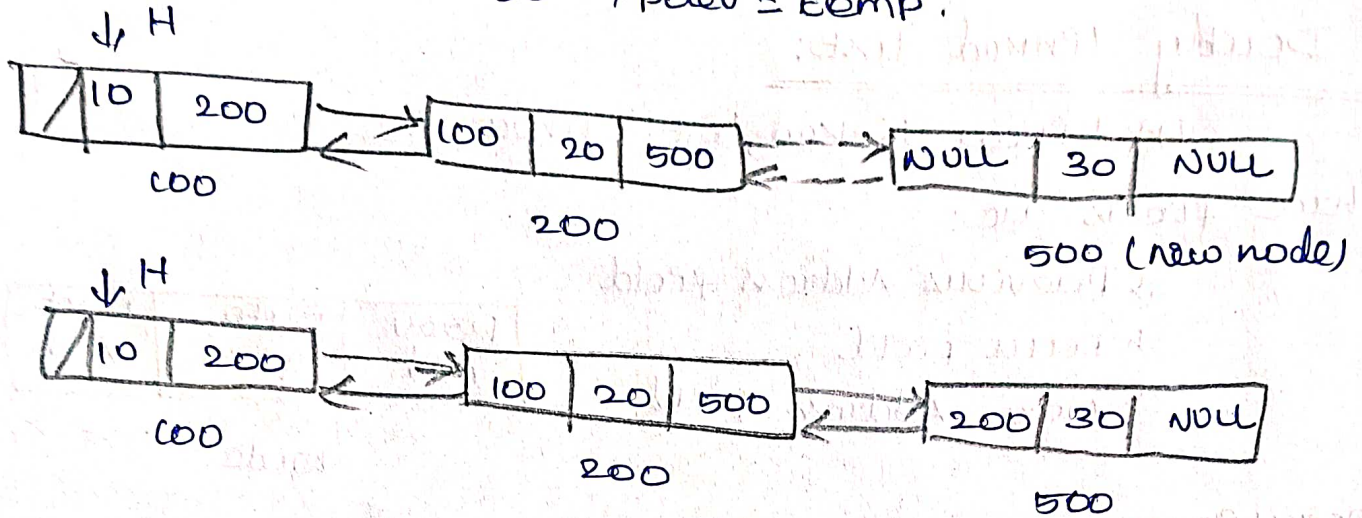
temp = header

while (temp → next != NULL)

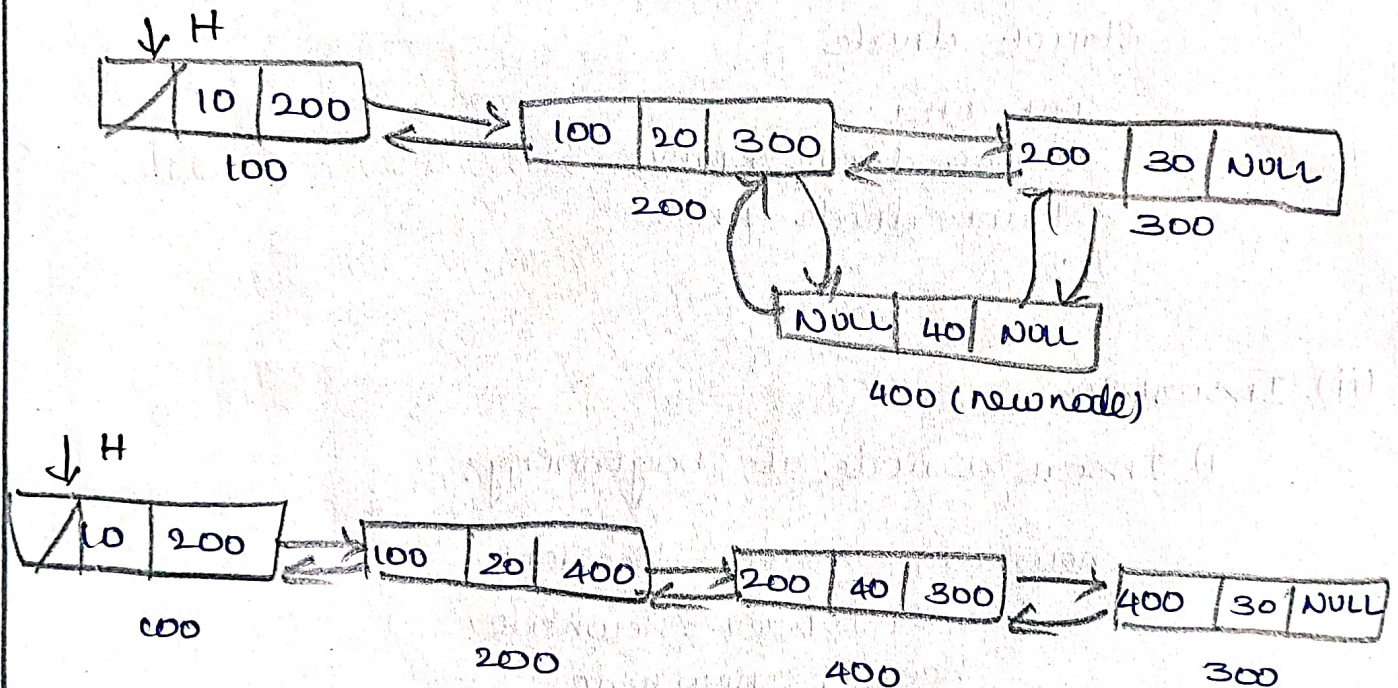
temp = temp → next;

temp → next = new node

newnode → prev = temp.



3) Insert a node at middle:



new node → next = p → next

p → next ⇒ prev = new node

p → next = new node

newnode → prev = p

4) Deletion:

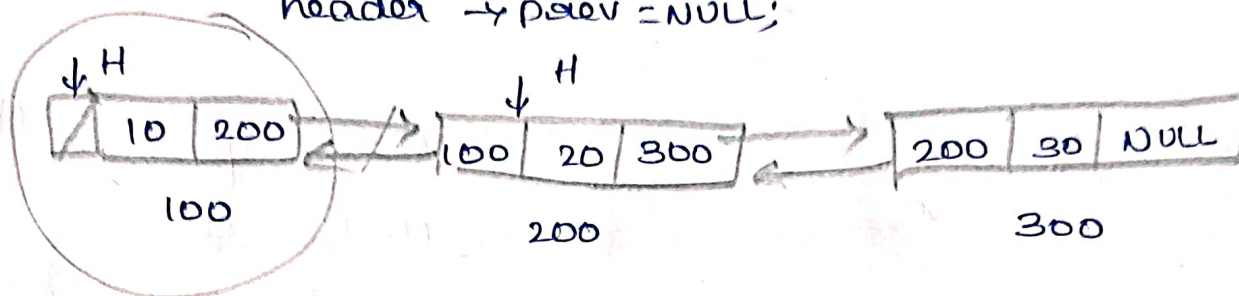
5

i) Delete the first node:

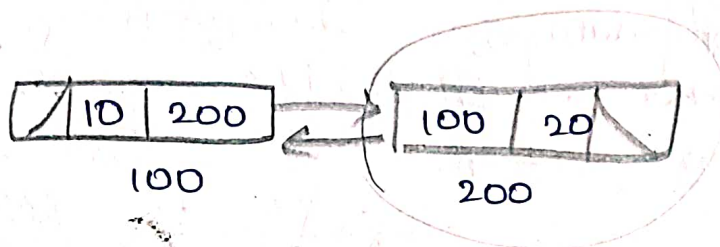
temp = head;

header = header → next;

header → prev = NULL;



2) Delete a node at end:



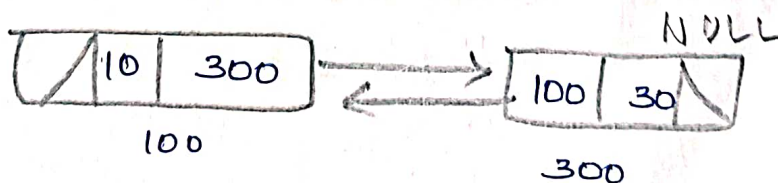
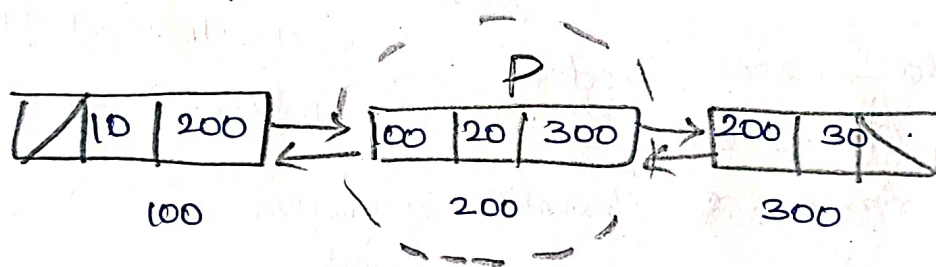
3) Delete Intermediate node:

Find position p

$p \rightarrow \text{prev} \rightarrow \text{next} = p \rightarrow \text{next}$

$p \rightarrow \text{next} \rightarrow \text{prev} = p \rightarrow \text{prev}$

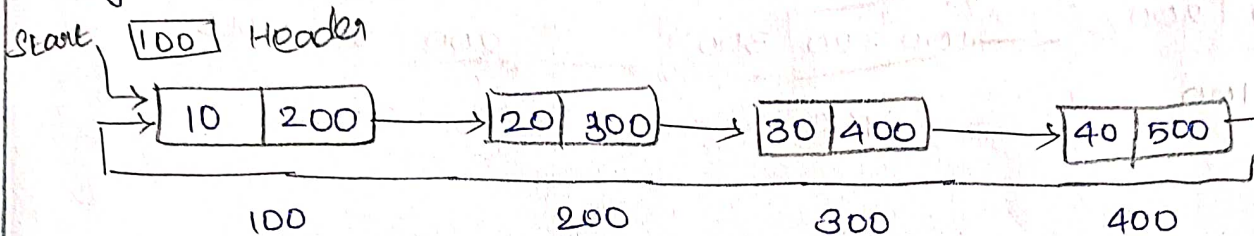
~~Free (P);~~



6) Circularly Linked List LAM - 2020

The link field of the last node is made to point to the start/first node of the list. A circular linked list has no beginning and no end.

Eg:

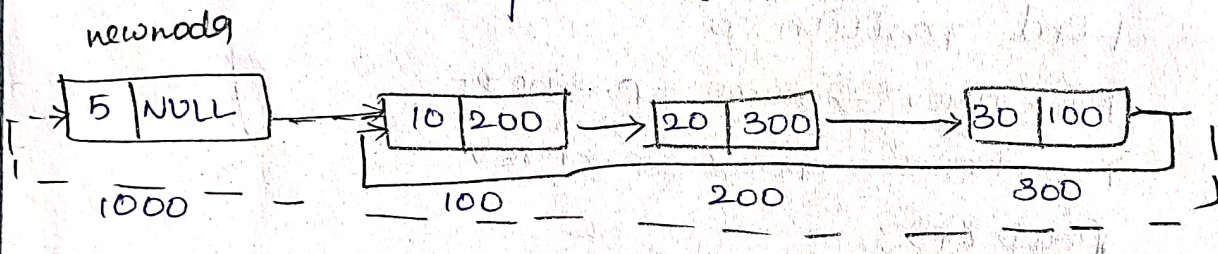


$P \rightarrow \text{data} = 200$
 $\text{temp} \rightarrow \text{data} = 10$
 $P \rightarrow \text{next} = \text{temp}$
 $\text{temp} \rightarrow \text{next} = P$

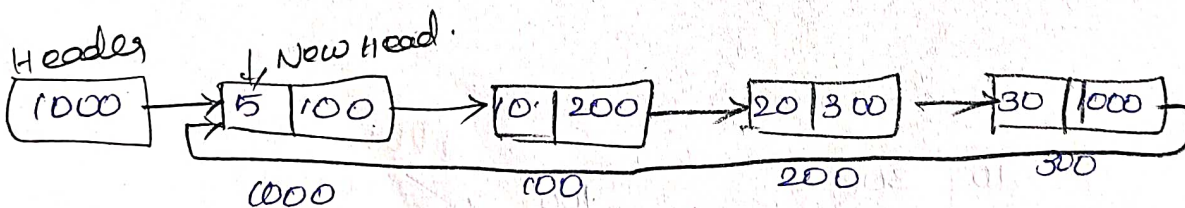
Operations:

1) First Insert:

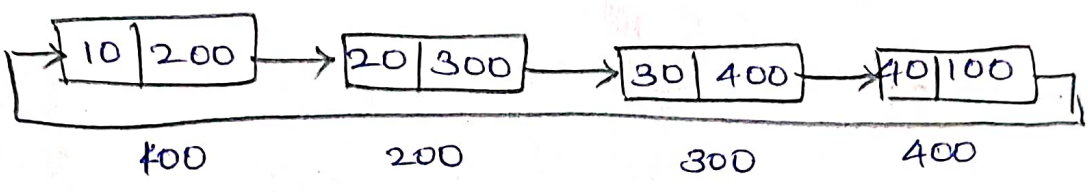
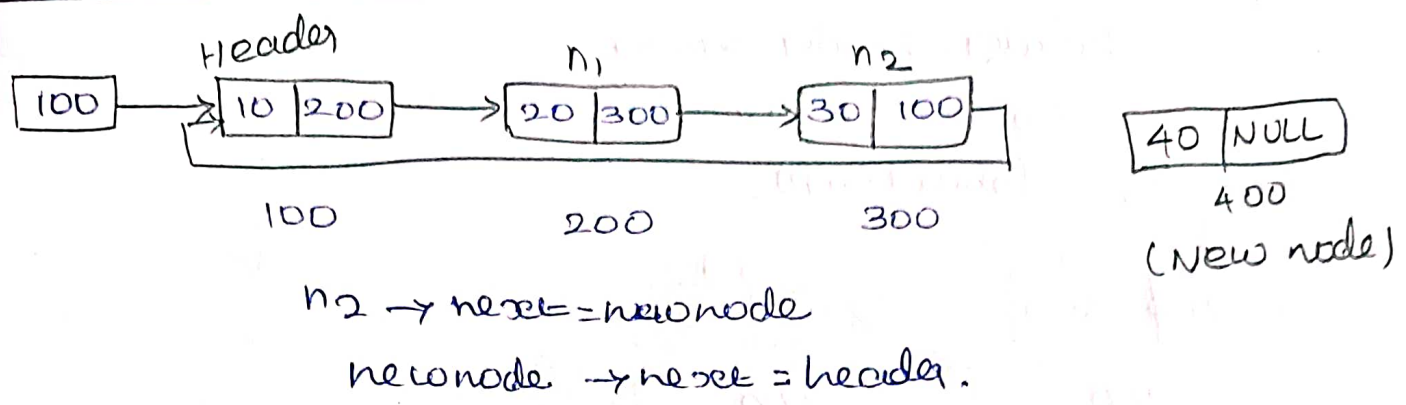
Using search() function we can insert at first



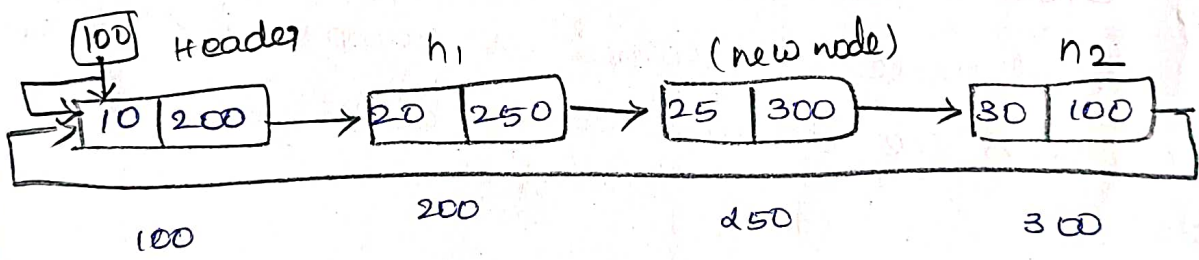
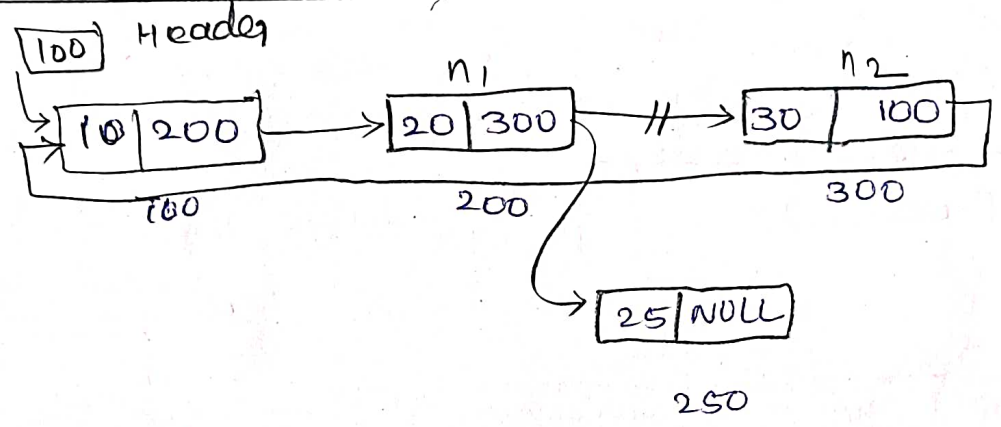
$\text{newnode} \rightarrow \text{next} = \text{header}$
 $\text{header} \rightarrow \text{newnode}$
 $\text{temp} \rightarrow \text{next} = \text{header}$



Insert at Last position:

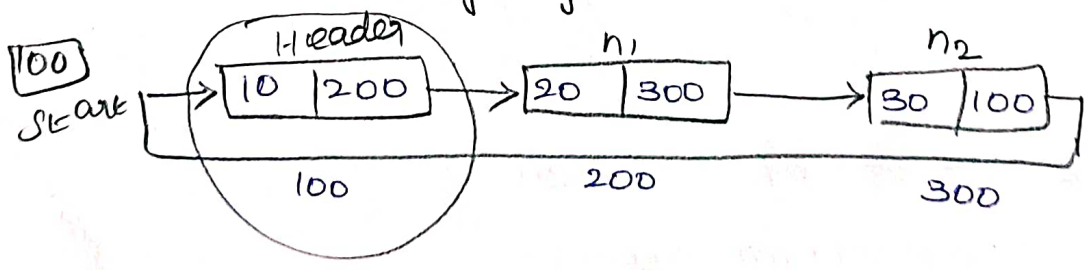


Insert at middle:



Deletion:

Deletion at Beginning:

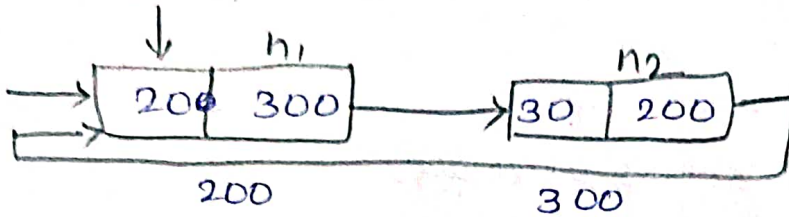


$temp = header;$

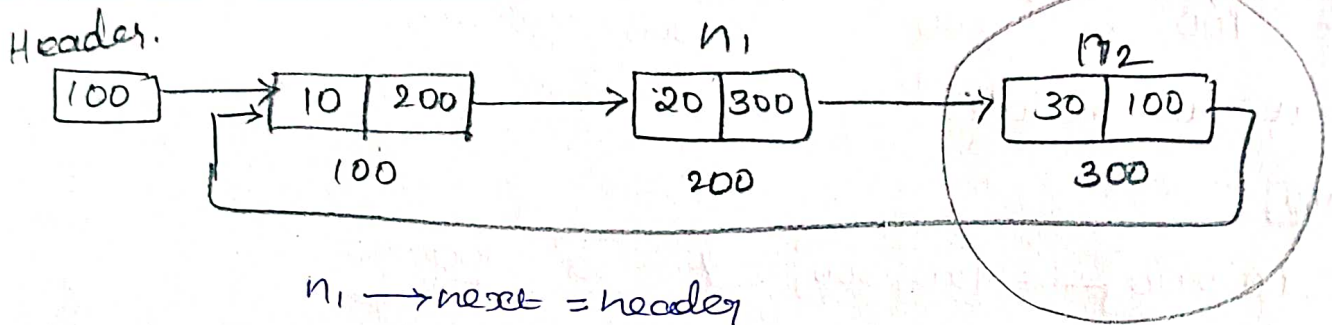
$header = header \rightarrow next$

$n_2 \rightarrow next = header$

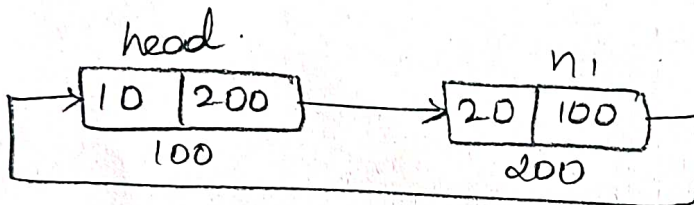
$Header \quad free(temp);$



Delete at last node:

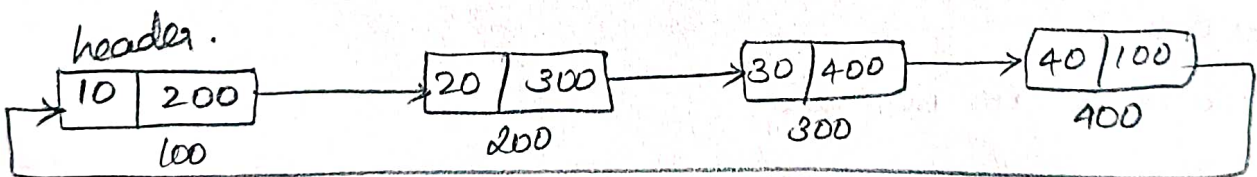


$n_1 \rightarrow next = header$
 $free(n_2);$



Display of Circular list:

Head node is assigned as temp node. If we have a CLL then the data will be displayed as
 $temp \rightarrow data$



$temp \rightarrow next = header$

$temp = temp \rightarrow next$

8) Applications of List [N/D-2021, A/M-2022]

7

Polynomial manipulation:

Polynomial expressions contains terms with non-zero, co-efficients and exponents:

$$p(x) = a_0x^n + a_1x^{n-1} + \dots + a_n.$$

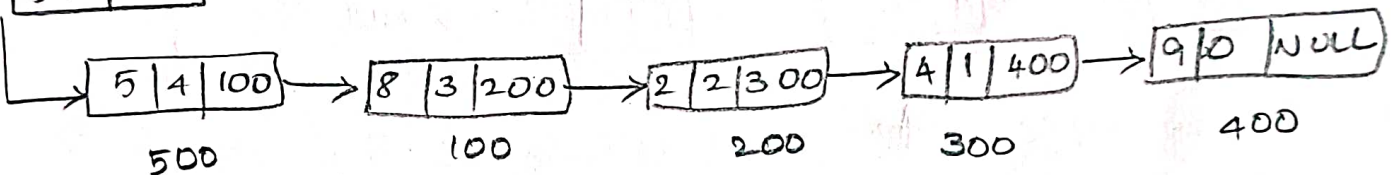
Each node contains three fields namely.

- (*) Co-efficient field
- (*) Exponent field
- (*) Link - field.

Co-efficient	Exponent	Link
--------------	----------	------

$$5x^4 - 8x^3 + 2x^2 + 4x + 9$$

500 | NULL head



Polynomial ADT:

struct poly

{
 int coeff;

 int exp;

 struct poly *next;
};

Creation of polynomial:

poly create (poly *head, poly *next, node)

{
 poly *pt;

 if (head == NULL)


```
{ head1 = newnode1;
```

```
return (head1);
```

```
}
```

```
else
```

```
{ ptr = head1;
```

```
while (ptr → next != NULL)
```

```
ptr = ptr → next;
```

```
ptr → next = newnode1;
```

```
}
```

```
return (head1);
```

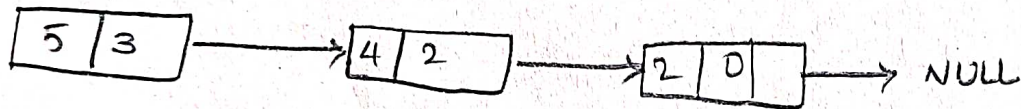
```
}
```

Eg: $5x^3 + 4x^2 + 2x^0$

$5x^1 + 5x^0$

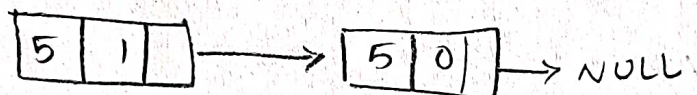
O/p - $5x^3 + 4x^2 + 5x^1 + 7x^0$

List 1:

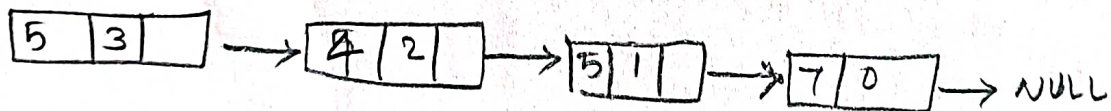


+

List 2:



Resultant list:

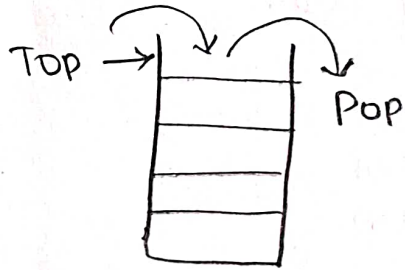


Linear Data Structures, Stack, Queue

Stack: [N/D-2021]

A stack is a non-primitive linear DS and is an ordered collection of homogeneous data elements.

The last element inserted will be on top of the stack, since deletion is done from the same end. LIFO.



Stack:

Operations:

- ① Push,
- ② Pop

Push/Insertion operation:

This operation inserts an element always on top of the stack. $Top = Top + 1$

Delete/Pop operation:

Deleting an element from the top of the stack is called pop operation. The pop operation can be decremented by 1.

$$Top = Top - 1$$

Implementation of stack

Array Implementation

Linked List Implementation

2) Operations:

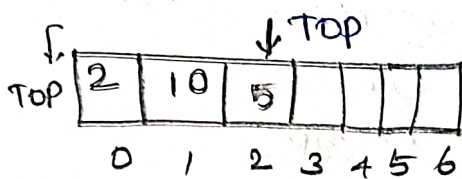
- 1) Push()
- 2) Pop()
- 3) Isfull()
- 4) Is Empty()

Push operation:

It adds a new element to the stack.

Each time a new element is inserted on the stack the top pointer is incremented by one.

Eg:



Push(2)
Push(10)
Push(5)

$$\text{top} = \text{top} + 1$$

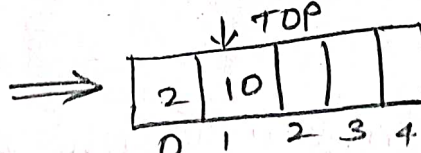
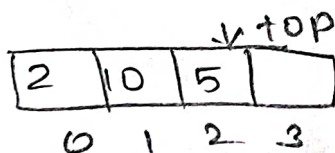
int isfull (stack s)

```
{ if (top == Arraysize)
  return (1);
}
```

Pop operation:

A Pop operation deletes the top most element from the stack.

Each time an element is removed from the stack, the top pointer is decremented by one.



POP(5)

$$\text{TOP} = \text{top} - 1$$

void pop (stack s)

{ if (IS Empty(s))

Errors ("empty stack");

else

{ x = s[Top];

Top = Top - 1;

}

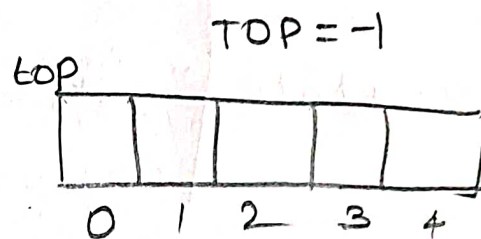
IS Empty:

int ISEmpty (stack s)

{ if (Top == -1)

return (1);

}



Empty stack

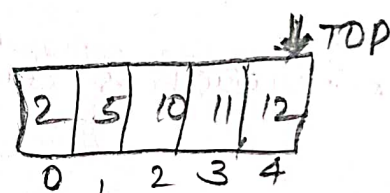
IS Full:

int IsFull (stack s)

{ if (Top == ArraySize)

return (1);

}



Full stack

3) Applications of stack - (N/D - 2018)

(or)

Evaluating Arithmetic Expression:

[Conversions of Infix to Postfix Expressions]

Applications:

(*) Expression Evaluation

(*) Backtracking (Game playing, Finding path)

(*) Memory Management.

Evaluating arithmetic expressions: (N/D-2018)

Infix	Prefix	Postfix
$a + b$	$+ab$	$ab +$
$a + b * c$	$+a * bc$	$abc * +$
$(a + b) * (c - d)$	$* + ab - cd$	$ab + cd - *$
$b * b - 4 * a * c$	$- * bb * * 4ac$	$bb * 4a * c -$

Infix: Operators are written b/w the operands they on,

Prefix: Operators are written before the operands, Eg: $+34$

Postfix: Operators are written after the operands, Eg: $34 +$

Conversions of Infix to Postfix Expressions:

Steps:

- 1) First, we have to take infix expression.
- 2) we read the expression from left to right.
- 3) we read this expression one by one and check whether it is operand or operator.
- 4) If it is operand, then we print it and if operator we store it into the stack.
- 5) In the end, we retrieve operator from the stack and print it.

Infix

postfix

1) $2+3*4$

$234*+$

$a*b+c$

$ab*c+$

$5+6/3*(5+6)-7$

Eg:

Stack	O/P
$\boxed{+}$	$\boxed{2}$
$\boxed{+}$	$\boxed{2}$ read '+' and placed on stack.
$\boxed{*}$ $\boxed{+}$	$\boxed{23}$ now read 3 and placed on o/p
$\boxed{*}$ $\boxed{+}$	$\boxed{234*+}$ now 4 is read & placed on o/p

1) $(a+b)*c/d+e/f$

Step 1:

I/P stack	process	O/P stack
\boxed{c}	The left paranthesis is encountered, then it is pushed on to the stack	$\boxed{}$
\boxed{e}	'a' is read, so it is placed on to the o/p	\boxed{a}
$\boxed{+}$ \boxed{c}	'+' is read, then push it on to the stack	\boxed{a}

$\boxed{\begin{array}{c} + \\ c \end{array}}$

$\boxed{\begin{array}{c}) \\ + \\ (\end{array}}$

$\boxed{*}$

$\boxed{*}$

$\boxed{\begin{array}{c} / \\ * \end{array}}$

$\boxed{\begin{array}{c} / \\ * \end{array}}$

$\boxed{\begin{array}{c} + \\ / \\ * \end{array}}$

$\boxed{\begin{array}{c} / \\ + \end{array}}$

$\boxed{\begin{array}{c} / \\ + \end{array}}$

$\boxed{}$

'b' is read so it is placed on to the o/p

Symbol ')' is read, now we pop the operators

the operator '*' is read & place them in field

the operand 'c' is read & placed on the o/p

'/' is read & placed on to the stack

'd' is read & placed on the o/p

'+' is scanned & it's an operator, so it checks precedence on the stack.

'/' is read & placed on to the o/p

'e' is read & placed on to the o/p

The operator is popped & placed on to the stack

\boxed{ab}

\boxed{abt}

\boxed{abt}

\boxed{abtc}

\boxed{abtc}

\boxed{abted}

$\boxed{abted/+}$

$\boxed{abted/*e}$

$\boxed{abted/*ef}$

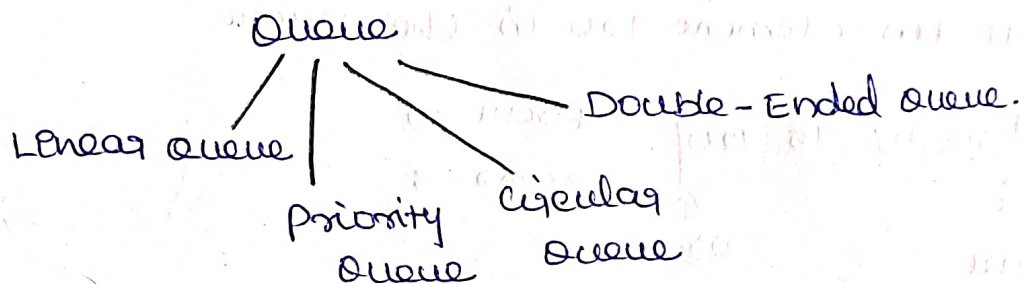
$\boxed{abted/*ef/+}$

Queue ADT

(4)

A queue is an ordered collection of elements in which insertion are made at one end is referred to as the "REAR end", and ^{end}from which deletions are made is referred to as the front end.

Queue is a FIFO - First in First out lists.



Implementation of queues:

- ① Array based Implementation.
- ② Linked list Implementation.

Operations of queue:

- ① Enqueue
- ② Dequeue

Array Implementation of Queue:

Enqueue operation:

It is used to add new element into a queue, at the rear end.

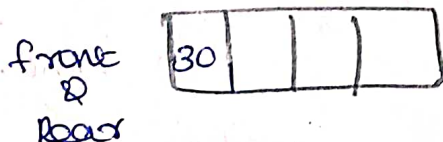
Assign the new element in the array by incrementing the rear.



Empty queue array
Size 4

rear = -1
front = 0

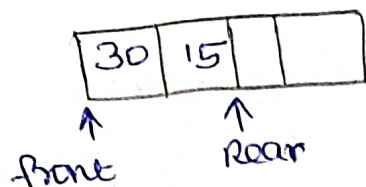
Insert an element 30 in the queue



front = 0
rear = 0

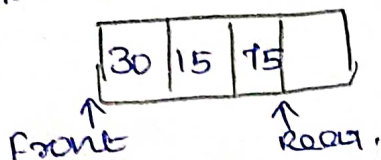
rear = rear + 1

Insert an element 15 in the queue.



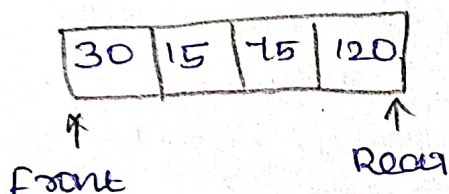
front = 0
rear = 1

Insert an element 75 in the queue



front = 0
rear = 2

Insert an element 120 in the queue



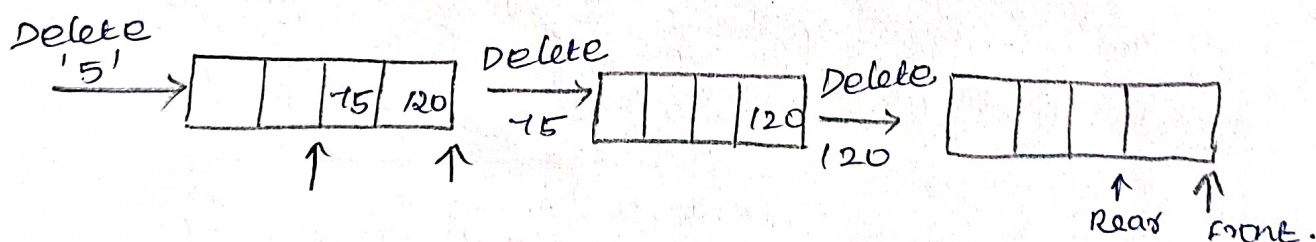
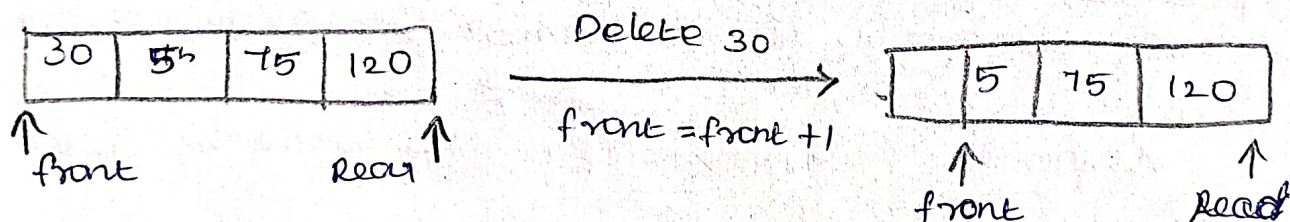
front = 0
rear = 3

~~Remove~~

Dequeue operation:

It is used to delete an element from the front end of the queue. When implementing the dequeue operation underflow condition of a queue, is to be checked.

Increment the variable by 1.



Linked List Implementation of queue - [A/P-2022] ⁽⁵⁾

A queue can be implemented by singly linked list.

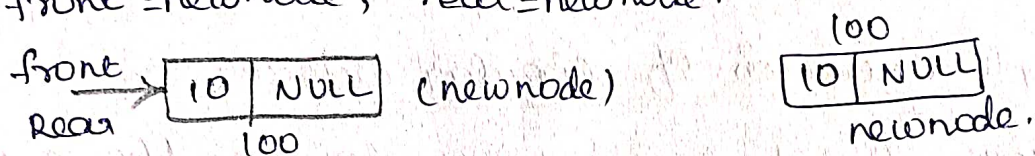
Enqueue operation:

It is used to add a new element onto a queue.

- 1) Allocate the memory for the newnode.
- 2) Assign the value for datapart of the newnode.
- 3) Assign the link of a rear to the newnode.
- 4) Assign the rear to the newnode.

rear = 0
front = 0 } Queue is empty.

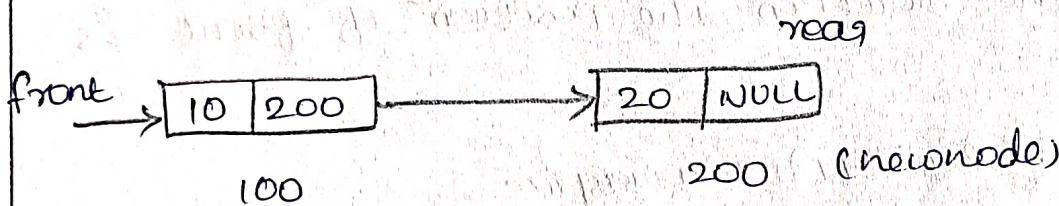
front = newnode; rear = newnode.



It represents queue having a single node.

Insert a newnode to the existing node.

rear → next = newnode.
rear = newnode.



Dequeue operation:

It is used to remove an element from the front of the queue.

- 1) Assign the front pointer to the temp pointer.
- 2) The front pointer is made to point after the first node, so the other nodes remain unchanged.
- 3) Free the allocated mem of the temp pointer.

Applications of queue: [N/D-2021]

⇒ When data is transferred asynchronously b/w to proc

Eg: IO buffers.

⇒ When resource is shared among multiple consumers.

Eg: include CPU and disk scheduling.

(*) In recognizing palindromes.

(*) keyboard buffer.

(*) Job scheduling

(*) Round Robin scheduling

(*) simulation.

Applications of Stack:-

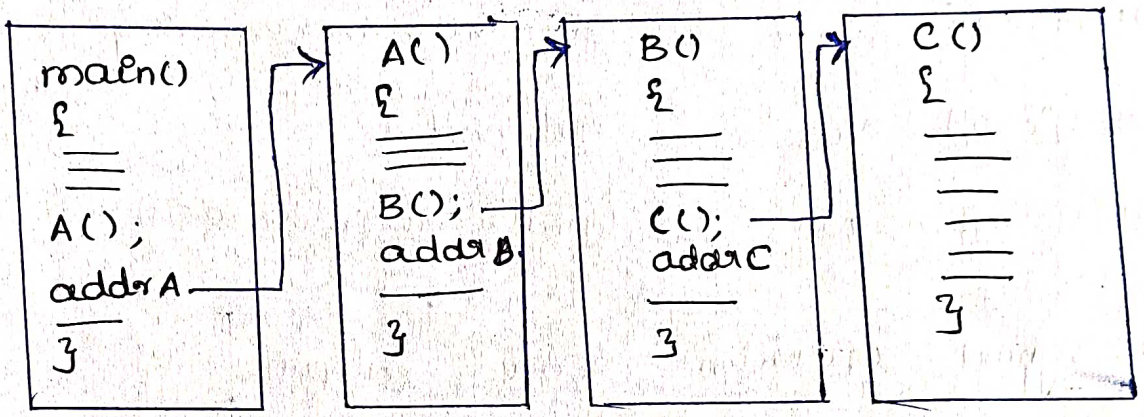
①

< Function Calls:

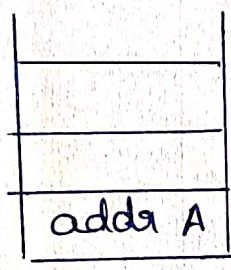
Function call is a dynamic data structure where elements are stored at contiguous memory locations.

Function call stack is maintained for every function call where it contains its own local variables and parameters of the callee function.

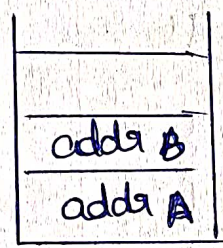
Eg: Three program with A, B, C functions.



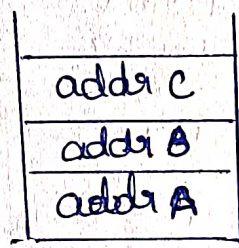
Function calls.



When Fun A
is called



When Fun
B is called



When Fun C
is called

1) Balancing Symbols:

Each time parser reads one character at a time.
If the character is opening delimiter like '(', '{', '[' then pushed on to the stack.

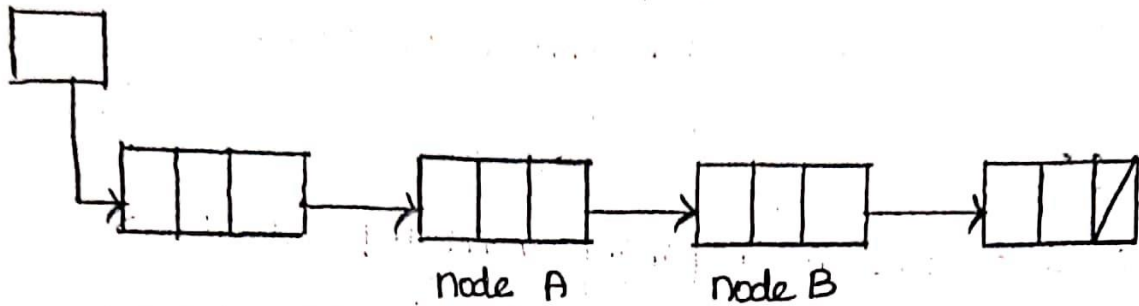
If the character is closing delimiter like ')', '}', ']' then popped on to the stack.

Example	Valid?	Description
$(A+B) + (C+D)$	Yes	Having balanced symbol
$((A+B) + (C-D)$	No	One closing brace missing
$((A+B) + [C-D])$	Yes	Balanced
$((A+B) + [C-D])$	No	Unbalanced (mismatch)

Input Symbol	Operation	Stack	Output
(Push ((
)	POP (
(Push ((
(Push (((
)	POP ((
[push [([
[push ((([
)	POP)	([
]	POP [(
)	POP (
	Stack is Empty		True

Linked list representation of Priority Queue.

Information	Priority number	Address of next node
-------------	-----------------	----------------------



Priority of node A is higher than priority of node B. (or)
Both have same priority → node A was added before node B.

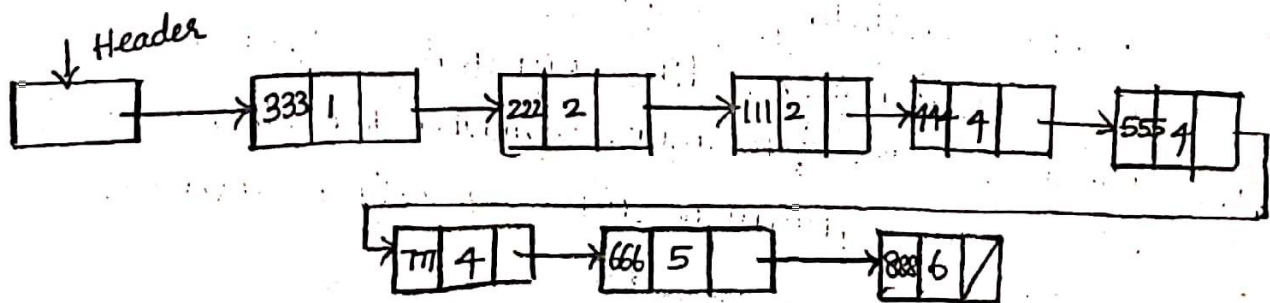
Location Info

1	222
2	
3	444
4	555
5	333
6	111
7	
8	666
9	777
10	888
11	

Priority

2
4
4
1
2
5
4
6

link



UNIT-III

NON LINEAR DATA STRUCTURES - TREES.

- 1) Tree ADT
- 2) Tree Traversals
- 3) Binary Tree ADT
- 4) Expression Trees
- 5) Applications of Trees
- 6) Binary Search Tree ADT
- 7) Threaded Binary Trees
- 8) AVL Trees
- 9) B-Tree
- 10) B⁺ Tree
- 11) Heap.
- 12) Applications of Heap.

A tree is a data structure made up of nodes (or) vertices and edges without having any cycle. The tree with no nodes is called the null (or) empty tree. A tree that is not empty consists of a root node and potentially many levels of additonal nodes that form a hierarchy.

Terminologies Used in Tree:

Root:

The top node in a tree. (A)

Child:

A node directly connected to another node when moving away from the root. Except Root node all are child node.

Parent:

The converse notation of a child. i.e., parent node that has an edge to a child node. (A, B, C)

Siblings:

A group of nodes with the same parent.

Descendant: (children, grandchildren, greatgrandchildren)
(D and E are siblings for B)

A node reachable by repeated proceeding from parent to child. Also known as subchild. (lower hierarchy)

Ancestor: [Parent, Grandparent, Great-Gp and so on]

A node reachable by repeated proceeding from child to parent. (higher hierarchy)

Leaf: (Terminal node) Eg; D, E, F, G

External node (not common). A node with no children.

Branch node (Internal node): A node with at least one child. Eg, Root node. (Non-Terminal) nodes. Eg; A, B, C

Degree: for a given node, its number of children.

A leaf is necessarily degree zero. Eg; Degree(A) = 2.

Edge: The connection between one node and another.

Path: A sequence of nodes and edges connecting a node with a descendant.

Level: The level of a node is defined as: 1 + the number of edges between the node and the

root. Level = Depth + 1.

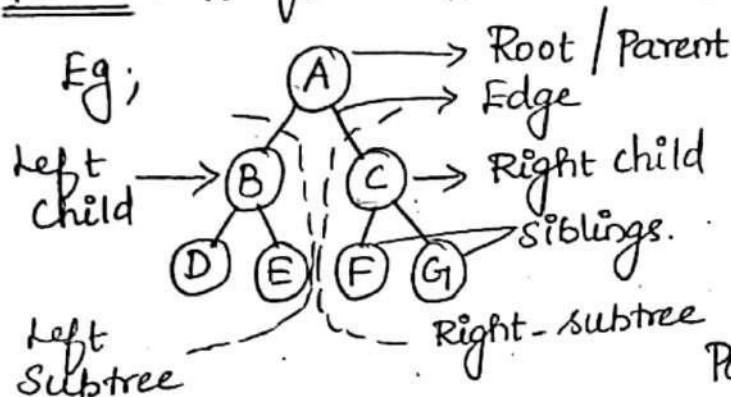
Level of Root = 0.

Height of tree: The height of a tree is the (N/D-2018) height of its root node. [Starts from 0]. Leaf don't have height.

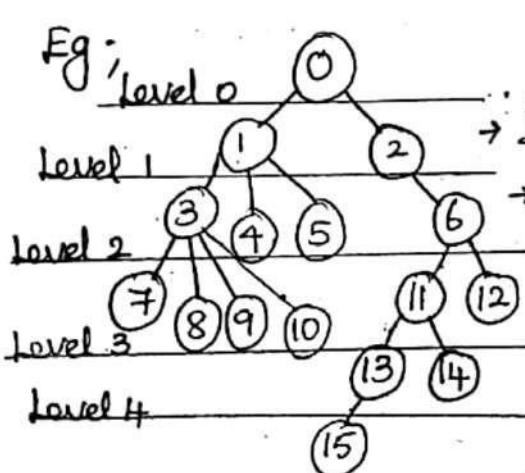
Height of node: The height of a node is the number of edges on the longest path between that node and a leaf.

Depth: The depth of a node is the number of edges from the tree's root node to the node. [Starts from 0]

Forest: A forest is a set of $n \geq 0$ disjoint trees.



Depth of node c: 01
 Height of tree: 2.
 Height of Root: 0
 Height of node c: 01
 Depth of tree: 2.
 Depth of Root: 0.
 Level: 3 levels. (1, 2, 3)
 Path from A to F: A-C-F

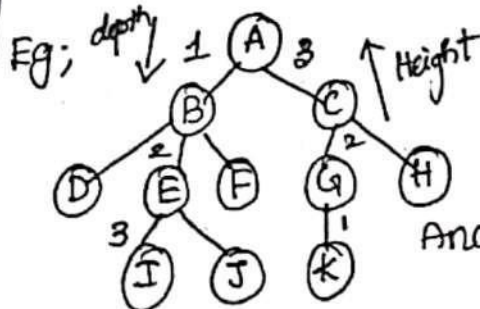


→ It has 16 nodes.
 → Degree of Tree: 5
 → Degree of node 0: 2
 → Depth: 5
 → Root: Node 0
 → Node 4 is a leaf and Node 4 is the child of 1.
 → Root node 0 is the Grandparent of node 4.
 → Nodes 3, 4 and 5 are siblings. since it has same parent 1.
 → Height of tree: 6

In a tree with 'N' nodes, these will be maximum

N-1 edges.

Depth of tree: 3
 Depth of A: 0
 Depth of B: 1
 Depth of K: 3



Height of tree: 3.
 Height of A: 3
 Height of B: 2
 Height of K: 0
 Ancestor: A is ancestor for all nodes.

(2) Tree Traversals.

Tree traversal (also known as tree search) is a form of Graph traversal and refers to the process of visiting (checking and/or updating) each node in a tree data structure, exactly once. Such traversals are classified by the order in which the nodes are visited.

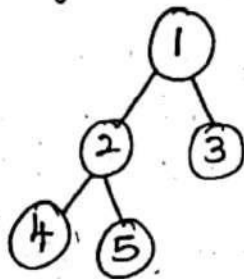
- * Inorder
- * Preorder &
- * Postorder.

(N/D-2018)

Unlike linear data structures (Array, Linked List, Stacks, Queues, etc) which have only one logical way to traverse them, trees can be traversed in different ways.

DFS: Depth First Search.

Eg.,



Inorder (Left, Root, Right):

4 2 5 1 3

Preorder (Root, Left, Right):

1 2 4 5 3

Postorder (Left, Right, Root):

4 5 2 3 1

BFS: (Breadth First Search)

1 2 3 4 5

Inorder:

- 1) Traverse the left subtree.
- 2) Visit the root.
- 3) Traverse the right subtree.

Void inorder (Tree T)

```
{
  if (T != NULL)
  {
    inorder (T->left);
    PrintElement (T->Element);
    inorder (T->right);
  }
}
```


Preorder :

- 1) visit the root
- 2) Traverse the left subtree
- 3) Traverse the right subtree.

```
void preorder (Tree T)
```

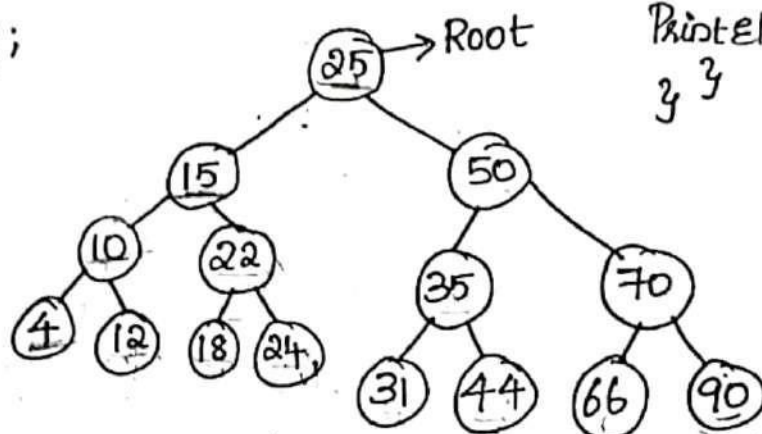
```
{
  if (T != NULL)
  {
    PrintElement (T->Element);
    preorder (T->left);
    preorder (T->right);
  }
}
```

Postorder :

- 1) Traverse the left subtree
- 2) Traverse the right subtree
- 3) Visit the root.

```
void postorder (Tree T)
{
  if (T != NULL)
  {
    postorder (T->left);
    postorder (T->right);
    PrintElement (T->Element);
  }
}
```

Eg;



L-R-R
R-L-R
L-R-R

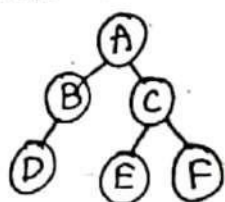
Inorder : 4 - 10 - 12 - 15 - 18 - 22 - 24 - 25 - 31 - 35 - 44 - 50 - 66 - 70 - 90

Preorder: 25 - 15 - 10 - 4 - 12 - 22 - 18 - 24 - 50 - 35 - 31 - 44 - 70 - 66 - 90

Postorder: 4 - 12 - 10 - 18 - 24 - 22 - 15 - 31 - 44 - 35 - 66 - 90 - 70 - 50 - 25
(N/D-2018)

BFS - Breadth first Search.

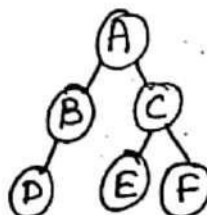
- * It uses the Queue for storing the nodes.
- * Constructs wide and short tree.
- * Vertex-Based algorithm.



BFS : A - B - C - D - E - F

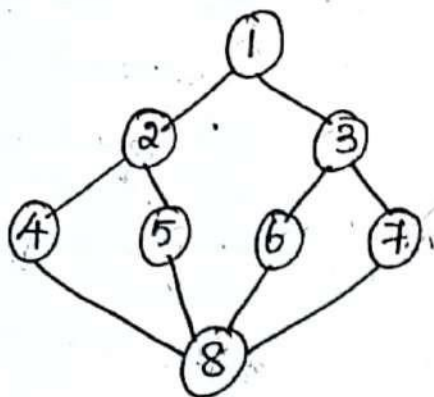
DFS - Depth first Search.

- * It uses the stack for traversal of the nodes.
- * Constructs narrow and long trees.
- * Edge-based algorithm.



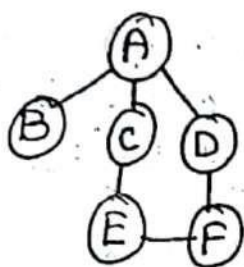
DFS : A - B - D - C - E - F.

Eg;



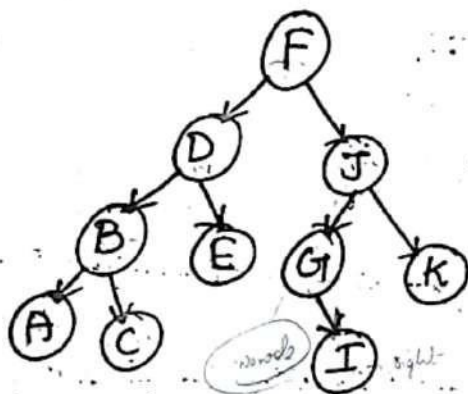
(we use all connections at one time)
 BFS: 1-2-3-4-5-6-7-8
 (we use only one connection at a time)
 DFS: 1-2-4-8-5-6-7-3

Eg;



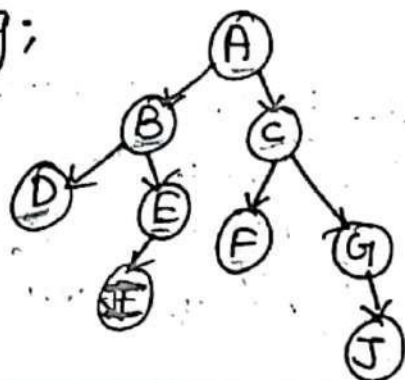
BFS: A B C D E F
 DFS: A B C E ^F D (or)
 A D F E C B (or)
 A C E F D B

Eg;



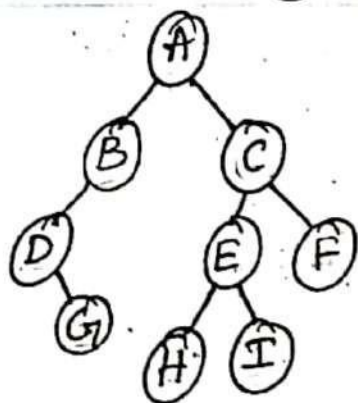
^{L R} Inorder: A B C D E F G I J K
^{R L R} Preorder: F D B A C E J G I K
^{L R R} Postorder: A C B E D I G K J F

Eg;



Inorder: D B I E A F C G J
 Preorder: A B D E I C F G J
 Postorder: D I E B F G J C A

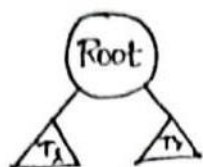
Eg;



Inorder: D G B A H I E C F
 Preorder: A B D G C E H I F
 Postorder: G D B H I E F C A

(3) BINARY TREE ADT

A Binary tree is a tree in which no node can have more than two children. The maximum degree of any node is two. This means the degree of a binary tree is either zero (or) one (or) two.



T_L - Left Tree

T_R - Right Tree.

In the above fig., the binary tree consists of a root and two sub trees T_L and T_R . All nodes to the left of the binary tree are referred as left subtrees and all nodes to the right of a binary tree are referred to as right subtree.

Implementation:

A Binary tree has atmost two children, we can keep direct pointers to them. The declaration of tree nodes is similar in structure to that for doubly linked lists, in that a node is a structure consisting of the key information plus two pointers (left and right) to other nodes.

Binary tree node declaration:

```
typedef struct tree-node *tree-Ptr;
```

```
struct tree-node
```

```
{  
    element-type element; (or)  
    tree-Ptr left;  
    tree-Ptr right;  
};
```

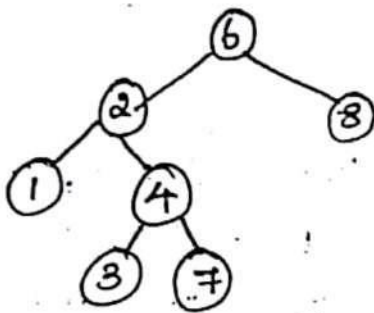
```
typedef tree-Ptr Tree;
```

```
struct node  
{  
    int data;  
    struct node *left;  
    struct node *right;  
};
```

Types of Binary Tree :

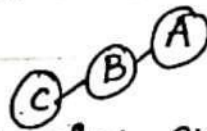
- * Strictly binary tree.
- * Skew tree
- * Left Skewed binary tree.
- * Right Skewed binary tree.
- * Fully Binary tree (or) Proper binary tree
- * Complete Binary tree.
- * Almost Complete Binary tree.

* Strictly Binary tree : It is a Binary tree where all the nodes will have either zero (or) two children. It does not have one child in any node.

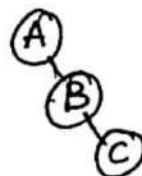


* Skew tree : It is a binary tree in which every node except the leaf has only one child node. There are two types of skew tree, they are left skewed binary tree and right skewed binary tree.

* Left Skewed Binary tree : A left skew tree has node with only the left child. It is a binary tree with only left subtrees.

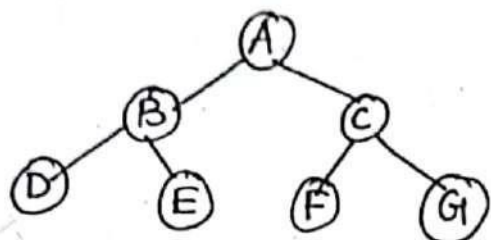


* Right Skewed Binary tree : A right skew tree has node with only the right child. It is a Binary tree with only right subtrees.



* Full Binary tree (or) Proper Binary tree:

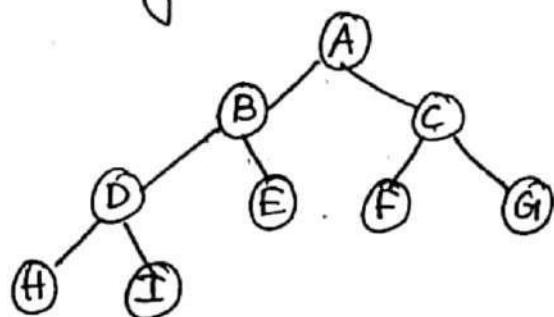
A Binary tree is a full binary tree if all leaves are at the same level and every non leaf node has exactly two children and it should contain maximum possible number of nodes in all levels. *A full Binary tree of height h has $2^{h+1} - 1$ nodes.



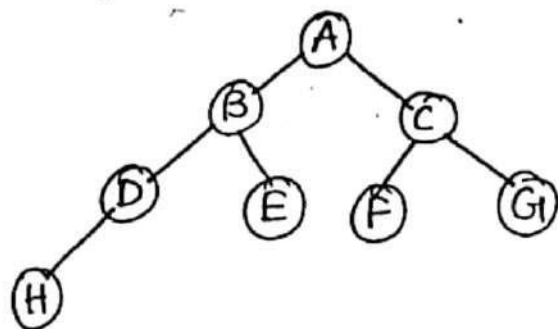
$$2^{h+1} - 1$$

$2^{h+1} - 1$ nodes.

* Complete Binary tree: Every non-leaf node has exactly two children but all leaves are not necessary at the same level. A complete Binary tree is one where all levels have the maximum number of nodes except the last level. The last level elements should be filled from left to right.



* Almost Complete Binary tree: An almost complete Binary tree is a tree in which each node that has a right child also has a left child. Having a left child does not require a node to have a right child.

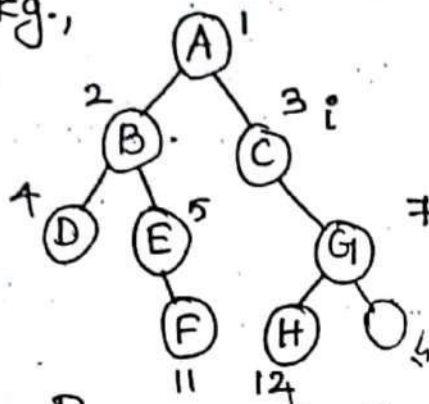


Implementation of Binary tree : (In memory)

* Array Implementation

* Linked list Implementation.

Eg.,



Using Array.

0	A	B	C	D	E		G				F	H
0	1	2	3	4	5	6	7	8	9	10	11	12

$$\text{Parent} :- \lfloor i/2 \rfloor \Rightarrow \lfloor 1/2 \rfloor \Rightarrow \lfloor 3/2 \rfloor \Rightarrow \lfloor 1.5 \rfloor \Rightarrow 1$$

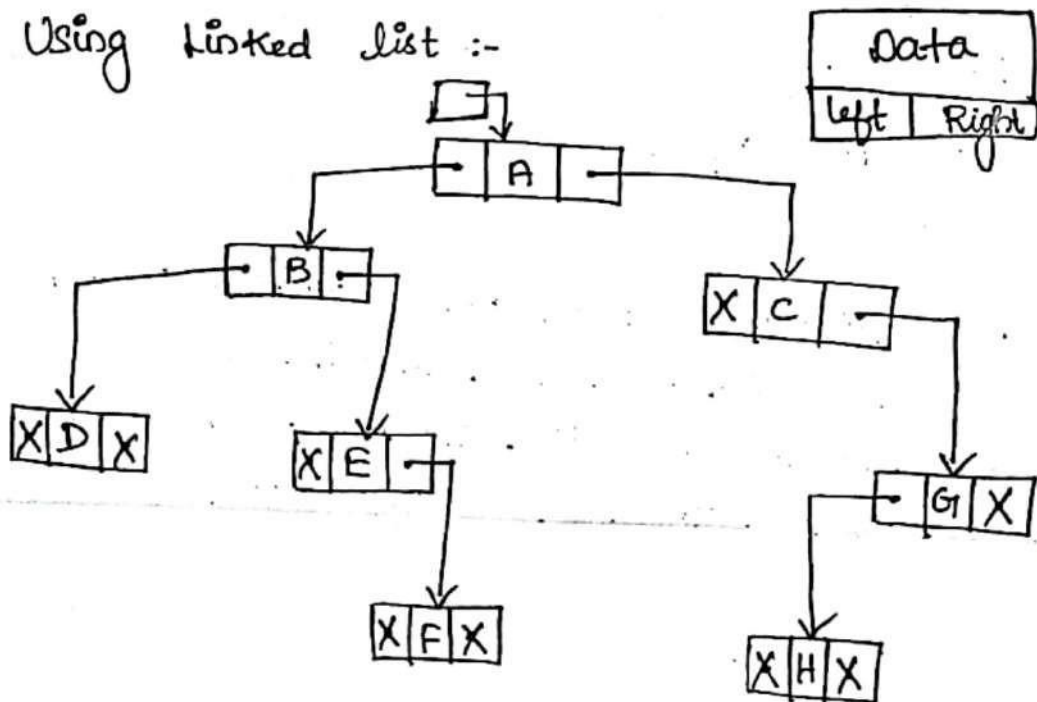
If C is parent for eg., then,

$$\text{left child} = 2 * i \Rightarrow 2 * 3 \Rightarrow 6$$

$$\text{Right child} = 2 * i + 1 \Rightarrow 2 * 3 + 1 \Rightarrow 6 + 1 \Rightarrow 7$$

So if parent is C, then left child is at 6th position and right child is at 7th position.

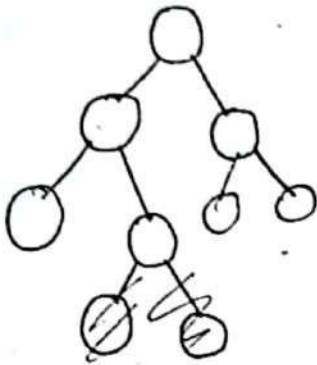
Using linked list :-



Left child Address	Data	Right child Address
--------------------	------	---------------------

Full Binary tree

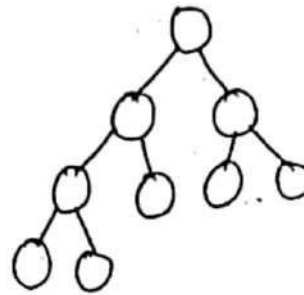
* A full binary tree (sometimes proper binary tree (or) 2-tree) is a tree in which every node other than the leaves has two children.



* Each node has zero (or) two children.

Complete Binary tree

* A Complete binary tree is a binary tree in which every level, except possibly the last, is completely filled, and all nodes are as far left as possible.



* All levels of the tree is full, except possibly the last level, where nodes are filled from left to right.

(4) Expression Trees. N/D-2018

An expression tree is a representation of expressions arranged in a tree-like data structure. In other words, it is a tree with leaves as operands of the expressions and node contain the operators.

Similar to other data structures, data interaction is also possible in an expression tree.

Expression trees are mainly used for analyzing, evaluating and modifying expressions, especially complex expressions.

- Types:-
- * Algebraic expressions
 - * Boolean expressions.

Construction of an expression tree.

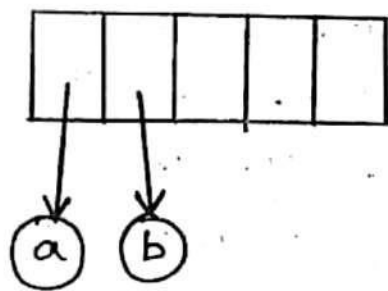
The evaluation of the tree takes place by reading the postfix expression one symbol at a time.

* If the symbol is an operand, a one-node tree is created and its pointer is pushed onto a stack.

* If the symbol is an operator, the pointers to two trees T_1 and T_2 are popped from the stack and a new tree whose root is the operator and whose left and right children point to T_2 and T_1 respectively is formed. A pointer to this new tree is then pushed to the stack. —

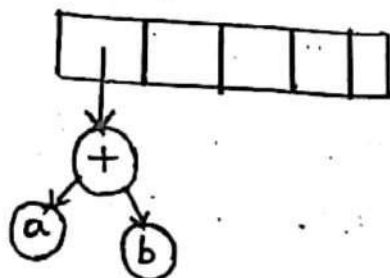
Example : The input is: $ab+cde+**$.

Since the first two symbols are operands, one-node trees are created and pointers are pushed to them onto a stack. for convenience the stack will grow from left to right.



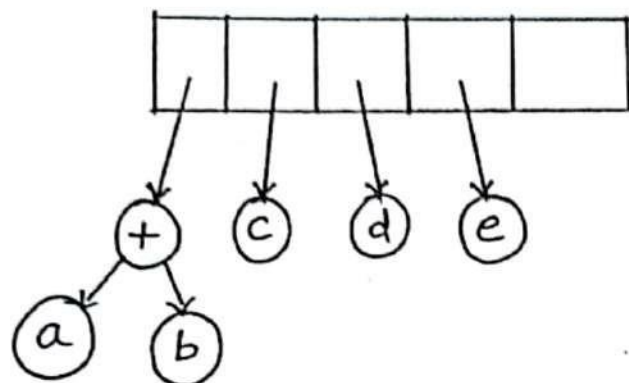
Stack Growing
from left to Right.

⇒ The next symbol is '+'. It pops the two pointers to the trees, a new tree is formed, and a pointer to it is pushed onto the stack.



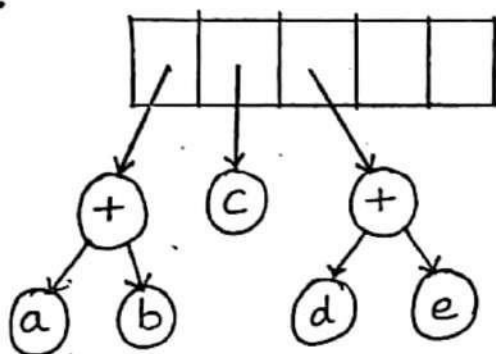
Formation of a
new tree.

⇒ Next c, d and e are read. A one-node tree is created for each and a pointer to the corresponding tree is pushed onto the stack.



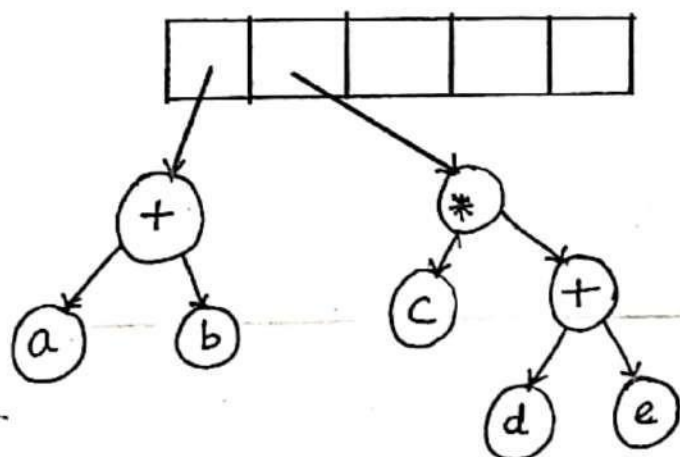
Creating a one-node tree.

⇒ Continuing, a '+' is read, and it merges the last two trees.



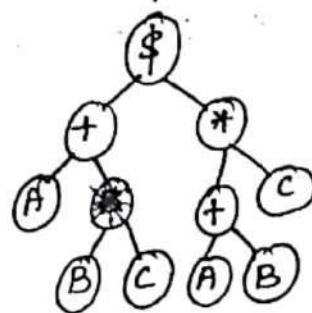
Merging two trees.

⇒ Now, a '*' is read, the last two tree pointers are popped and a new tree is formed with a '*' as the root.

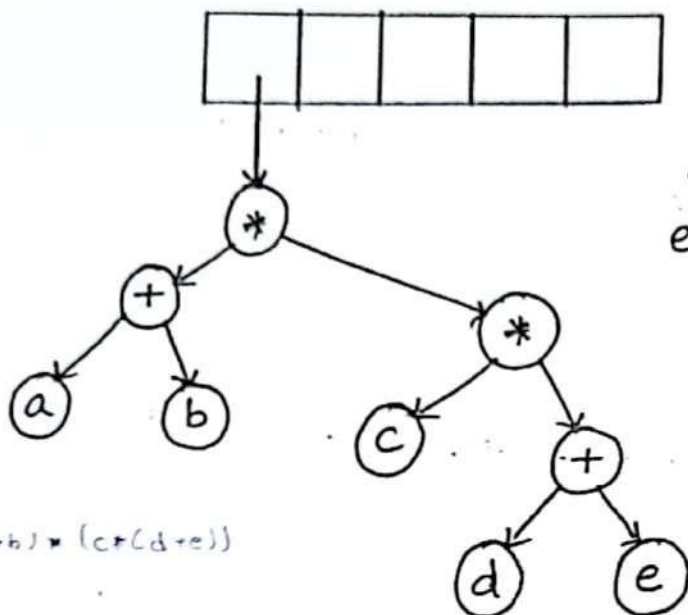


forming a new tree with a root.

Eg $(A+B)*C$ $\$ (A+B)*C$



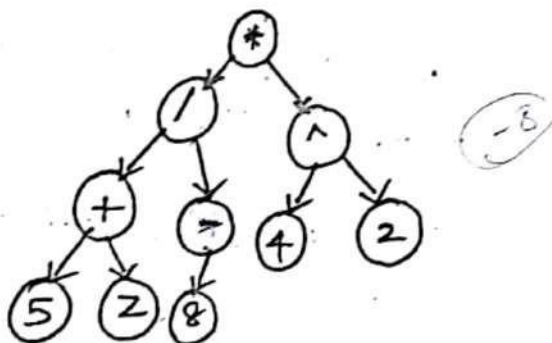
\Rightarrow finally, the last symbol is read. The two trees are merged and a pointer to the final tree remains on the stack.



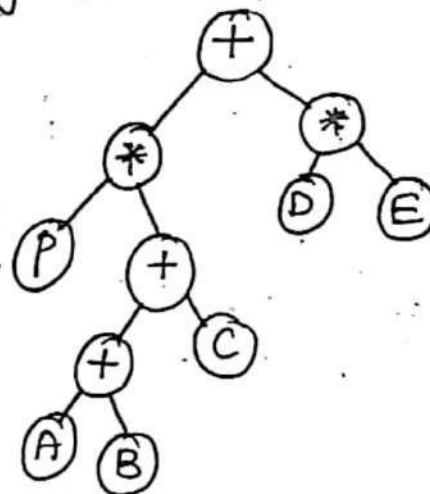
Steps to construct an expression tree.
 $ab+cdet+**$.

Algebraic expressions :-

$$((5+z)/-8) * (4^2)$$

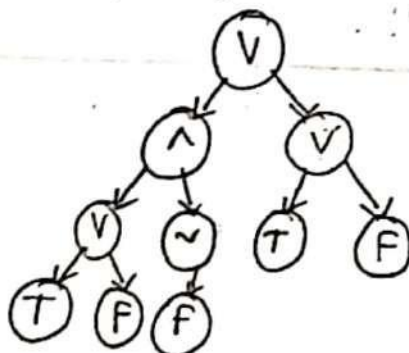


Eg (2) $((A+B)+C) + (D * E)$



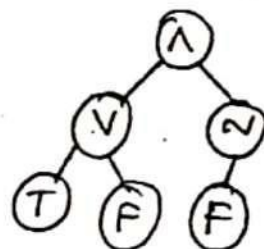
Boolean Expressions :-

$$((\text{true} \vee \text{false}) \wedge \sim \text{false}) \vee (\text{true} \vee \text{false})$$

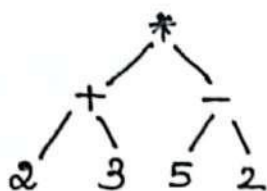


Eg (2)

$$(\text{true} \vee \text{false}) \wedge \sim \text{false}$$

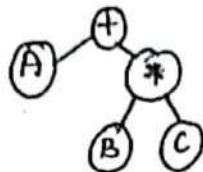


Eg (2) $(2+3) * (5-2)$

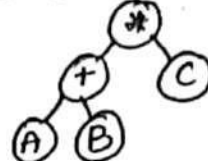


Note :- Internal node - operator
External node - operand

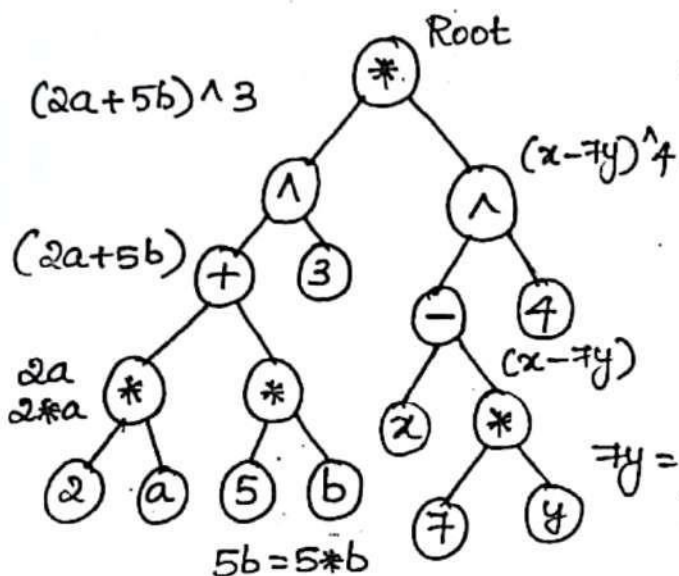
Eg $A+B*C$



Eg $(A+B)*C$



Eg (3) $(2a+5b)^3 * (x-7y)^4$

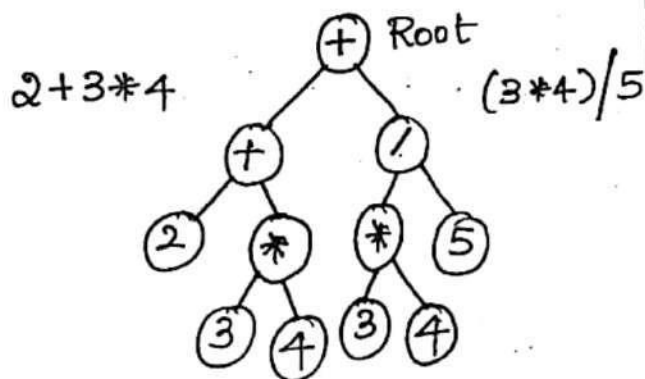


1) Divide expressions into two small mathematical terms to get Root operator.

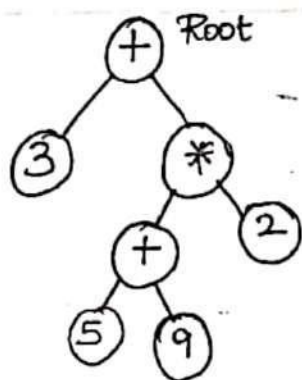
2) Scan symbol from right to left.

3) Place operator then expression on to the node.

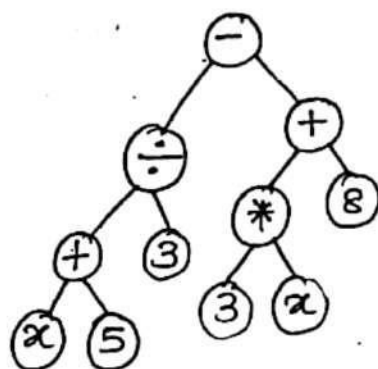
Eg (4) $2+3*4+(3*4)/5$



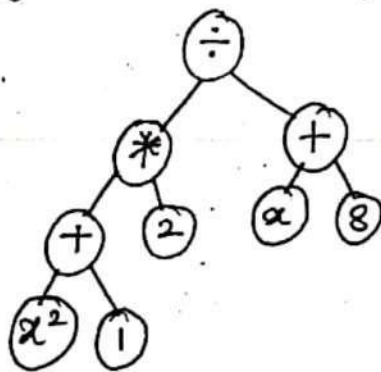
Eg (5) $3+((5+9)*2)$



Eg (6) $((x+5)/3)-(3x+8)$



Eg (7) $((x^2+1)*2)/(x+8)$



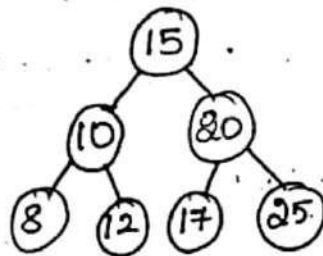
(5) Applications of trees.

* Binary Search Trees / Binary Sorted trees.

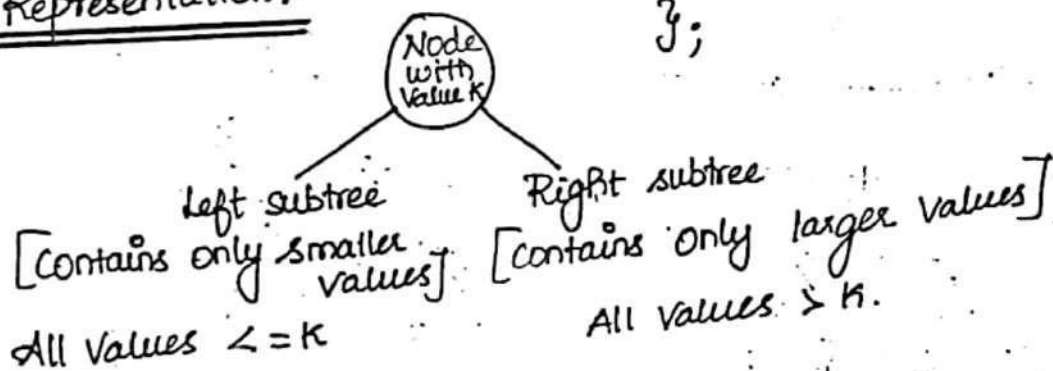
* Decision Trees.

Binary Search Tree (BST) :- It is a binary tree where each node has a comparable key (and an associated value) and satisfies the restriction that the key in any node is larger than the keys in all nodes in that node's left subtree and smaller than the keys in all nodes in that node's right subtree.

Left subtree \leq Right subtree.

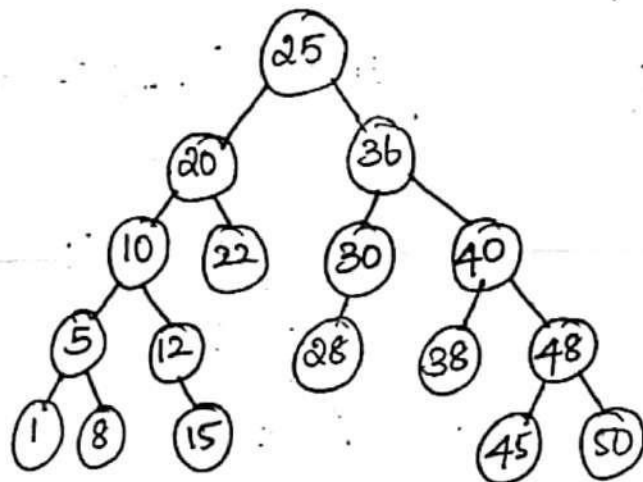


Representation:-



```
struct node  
{  
    int data;  
    struct node *leftchild;  
    struct node *rightchild;  
};
```

Eg.,



Left subtree (keys) \leq node (key) \leq right-subtree (keys)

Operations on BST.

* Search * Insertion

* Deletion.

SEARCH in BST: (N/D-2018)

- Step 1 : Read the search element from the user.
- Step 2 : Compare, the search element with the value of Root node.
- Step 3 : If both matches, then display "Given node found".
- Step 4 : If both not matches, Check whether search element is smaller (or) larger than that node value.
- Step 5 : If larger, then continue search process at right subtree.
- Step 6 : If smaller, then search at left subtree.
- Step 7 : Repeat the same until we found exact element.
- Step 8 : If we reach the node, then display "Element found",
if not then display "Element not found".

INSERTION in BST:

- Step 1 : Create a Newnode with given value and set its left and right to NULL.
- Step 2 : Check whether tree is empty.
- Step 3 : If Empty, then set root to newnode.
- Step 4 : If the tree is not empty, then check whether value of newnode is smaller (or) larger than the node. (here it is root node)
- Step 5 : If Newnode is smaller (or) equal to root node then move to left else move to right child.
- Step 6 : Repeat the above step until we reach to a leaf node.
- Step 7 : After reaching a leaf node, then insert the newnode as left child. If newnode is smaller (or) equal to that leaf, else insert it as right child.

DELETION IN BST:

Step 1: Find the node to be deleted using Search operation.

Step 2: Delete the node using free function (if it is a leaf) and terminate the function.

Insert the following into a Binary Search Tree.

10, 12, 5, 4, 20, 8, 7, 15 and 13.

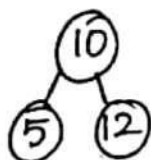
Insert 10.



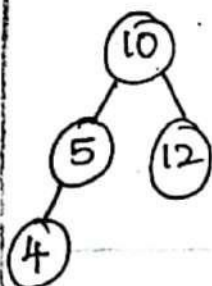
Insert 12



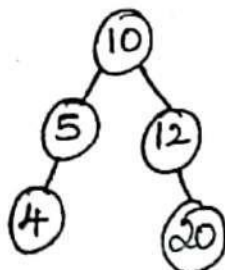
Insert 5



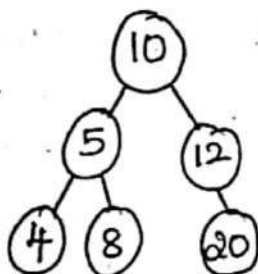
Insert 4



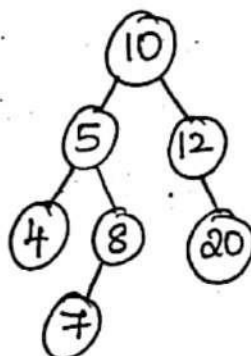
Insert 20



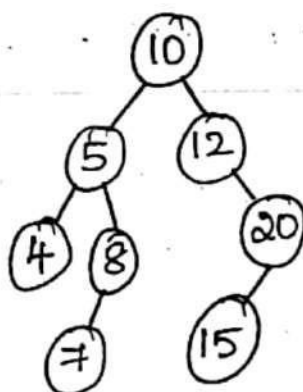
Insert 8.



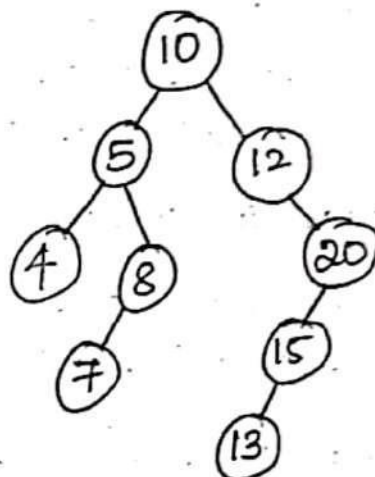
Insert 7.



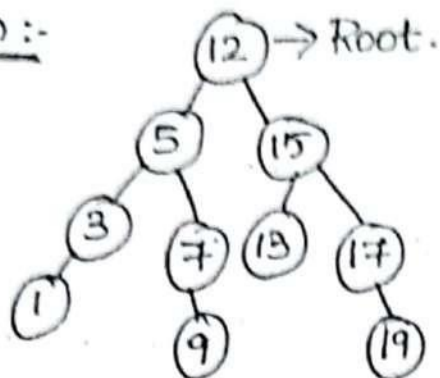
Insert 15.



Insert 13.

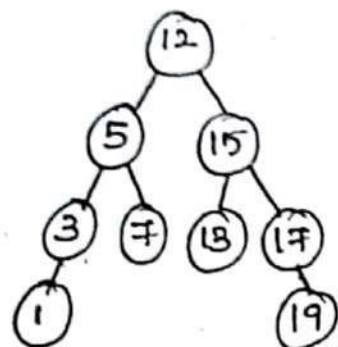


Deletion :-



- Case 1 : No child
- Case 2 : one child
- Case 3 : Two children.

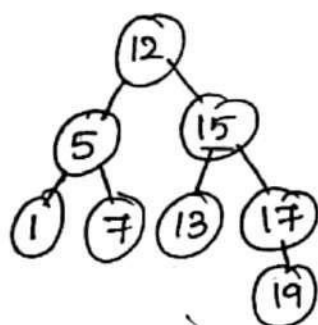
Delete Node 9 :-



Case 1 : No child.

9 is a leaf node, so we just cut the link and wipe off the node that is clear it from memory.

Delete Node 3 :-

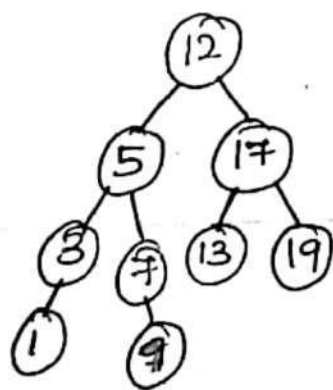


Case 2 : One child.

Wipe it off from memory.

Delete Node 15 :-

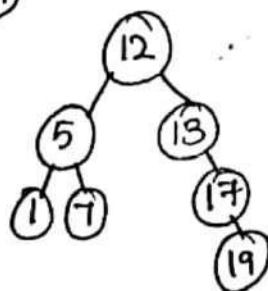
Case 3 : Two child.



wipe it off from memory.

(minimum element from right side deleted)

(or) largest element from left side.



Algorithm: INSERTION.

Void insert (int data)

```
{
    Struct node *tempnode = (struct node *) malloc
        (sizeof (struct node));
```

```
    Struct node *current;
```

```
    Struct node *parent;
```

```
    tempnode → data = data;
```

```
    tempnode → leftchild = NULL;
```

```
    tempnode → rightchild = NULL;
```

```
    if (root == NULL)
```

```
    {
        root = tempnode;
```

```
    } else {
```

```
        current = root;
```

```
        Parent = NULL;
```

```
        While (1) {
```

```
            Parent = current;
```

```
            if (data < parent → data)
```

```
            {
                current = current → leftchild;
```

```
            if (current == NULL)
```

```
            {
                Parent → leftchild = tempnode;
```

```
                return;
```

```
            }
```

```
        } else {
```

```
            current = current → rightchild;
```

```
            if (current == NULL)
```

```
            {
                Parent → rightchild = tempnode;
```

```
                return;
```

```
            }
```

```
        }
```

```
    }
```

Algorithm for Search:-

```
Struct node* Search (int data)
```

```
{
    Struct node* current = root;
```

```
    Printf ("visiting elements:");
```

```
    while (current → data != data)
```

```
    {
        if (current != NULL)
```

```
        {
            Printf ("%d", current → data);
```

```
            //goto left tree.
```

```
            if (current → data > data)
```

```
            {
                current = current → leftchild;
```

```
            }
```

```
        } else //goto right tree.
```

```
        {
            current = current → rightchild;
```

```
        }
```

```
        if (current == NULL)
```

```
        {
            return NULL;
```

```
        }
```

```
    }
```

```
}
```


Fig (2): Binary Search tree.

23, 35, 80, 2, 13, 56, 11, 60, 71.

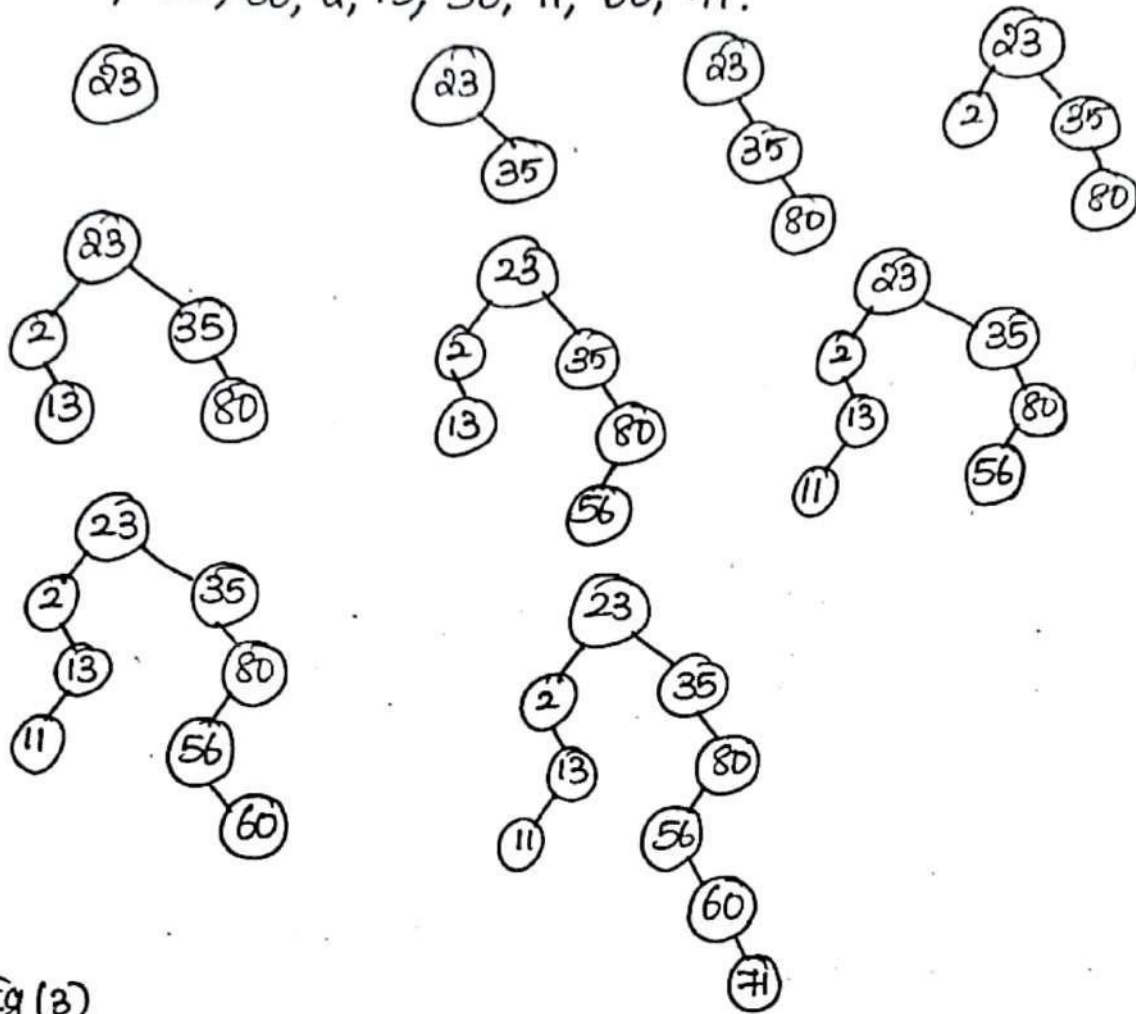
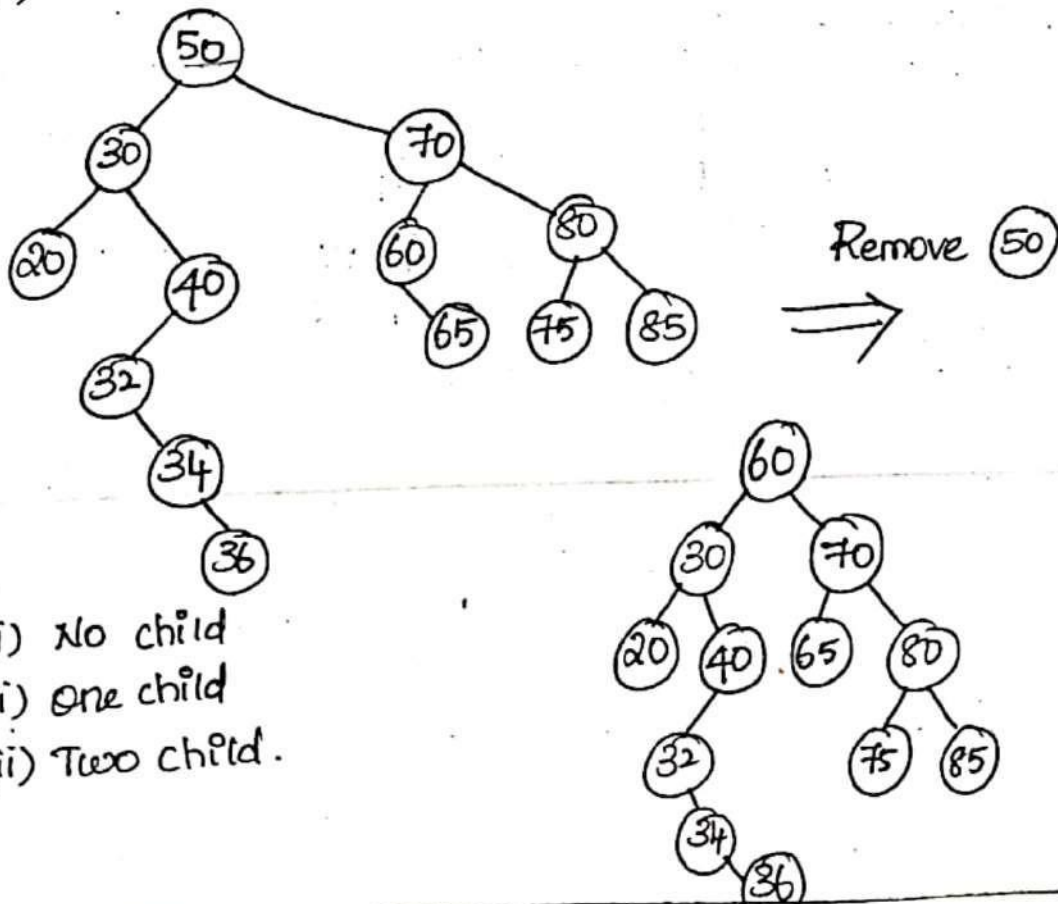


Fig (3)



(i) No child :-

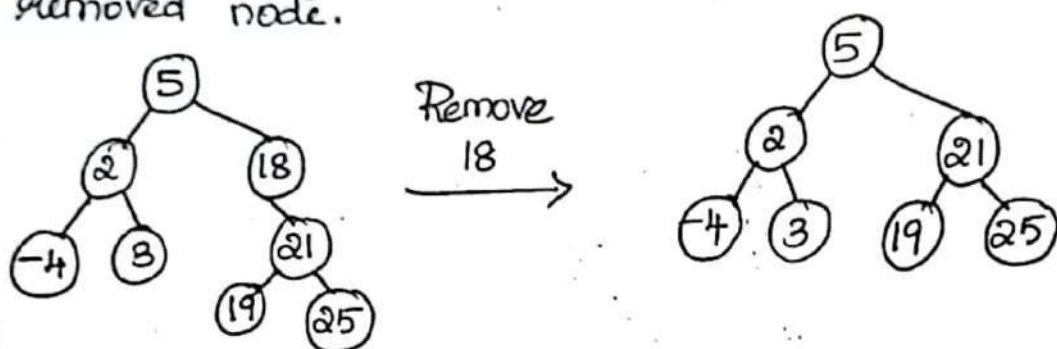
Node to be removed has no children.



(ii) One child :-

"Node to be removed has one child."

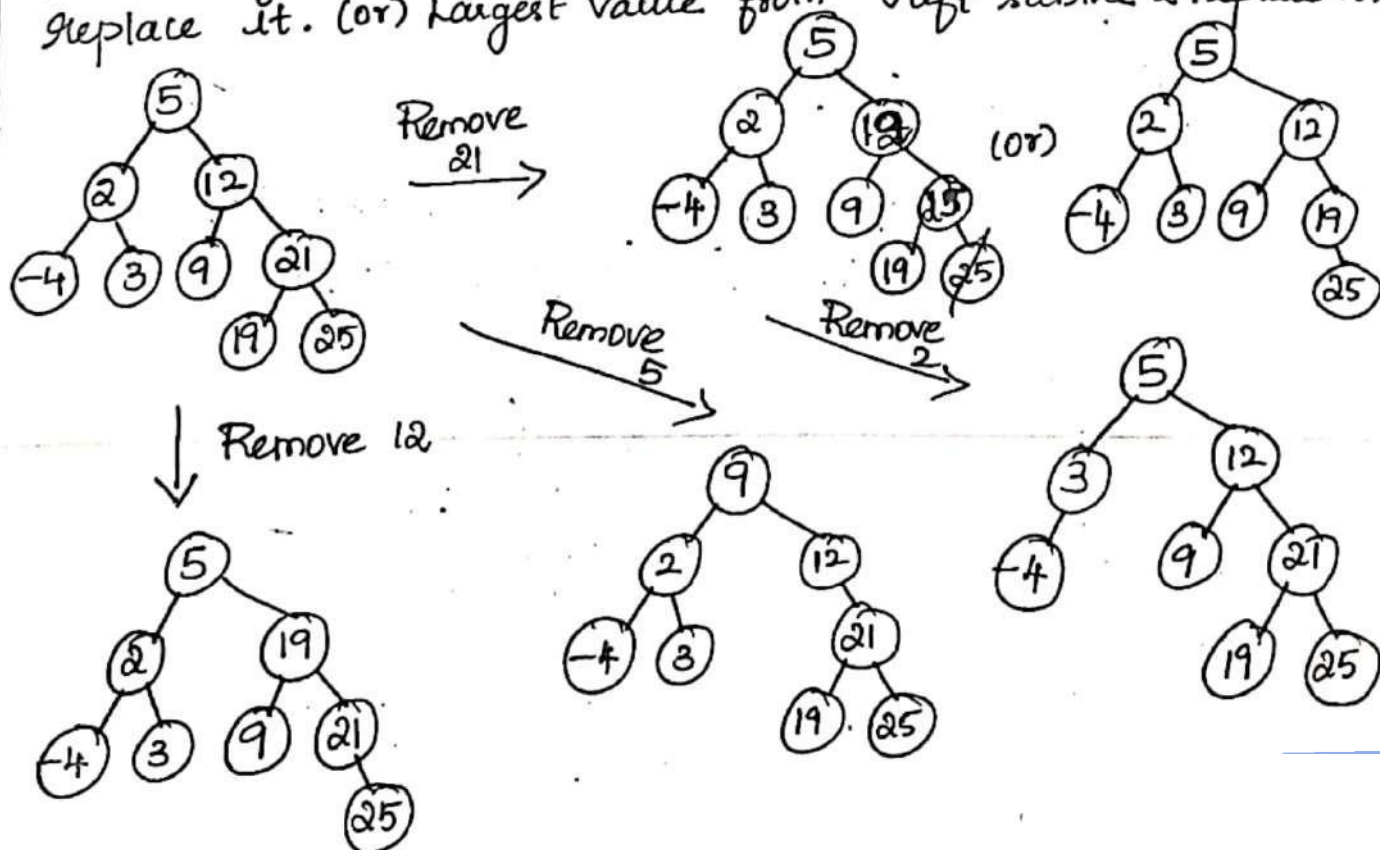
→ Links single child directly to the parent of the removed node.



(iii) Two child :-

Node to be removed has two children.

→ find minimum values in the right subtree & replace it. (or) largest value from left subtree & replace it.



Hashing:

Hashing is the process of mapping large amount of data item to a smaller table with the help of a hashing function.

It is the process of indexing and retrieving element in a data structure to provide faster way of finding the element using the hash key.

Key \rightarrow Hash function \rightarrow Hash value

Hash value	key
0	
1	
2	
3	
4	
5	
...	
n	

← Actual data store

"Hash Table" is just an array which maps a key (data) onto the data structure with the help of hash function.

"Hash function" is a function which takes a piece of data (key) as O/P and O/P an integer (hash value) which maps the data to a particular index in the hash table.

Hash function:

The mapping b/w an item and the slot where that item belongs in the hash table is called the hash function. The hash function will take any item in the collection and return an integer in the range of slot names, b/w 0 and $m-1$.

0	1	2	3	4	5	6
None	None	None	None	None	None	None

54, 26, 93, 17, 77, 31

(5)

$$h(\text{Item}) = \text{Item} \% m$$

Item	Hash value	
54	10	(54 mod 11)
26	4	(26 mod 11)
93	5	(93 mod 11)
17	6	(17 mod 11)
77	0	(77 mod 11)
31	9	(31 mod 11)

$$\begin{array}{r} 11) 54 (4 \\ \underline{44} \\ 10 \end{array}$$

designated position.

0	1	2	3	4	5	6	7	8	9	10
77	None	None	None	26	93	17	None	None	31	54

Note that 6 out of 11 slots are occupied. This is referred to as "Load factor" and commonly denoted by λ .

$$\lambda = \frac{\text{no. of items}}{\text{Table size}}$$

Table size.

$$\lambda = 6/11$$

According to the hash function, two (or) more items would need to be in the same slot. This is referred to as "collision" also called as "clash".

Two methods of hash functions:

(*) Folding method

(*) mid-square method.

Folding method:

If our item was the phone number

436-555-4601

(43, 65, 55, 46, 01) groups of 2.

$$43 + 65 + 55 + 46 + 01 \Rightarrow 210$$

If hash table has 11 slots, then $(210 \bmod 11) = 1$

So, the phone no. 436-555-4601 hashes the slot 1.

Group of 2 (43, 65, 55, 46, 01)

Reverse \Rightarrow 43, 56, 55, 64, 01 \rightarrow Reverse.

$$43 + 56 + 55 + 64 + 01 = 219$$

$$(219 \bmod 11) = 10$$

Mid-Square Method:

First we square the item, and then extract bottom portion of the resulting digits.

If the item was 44, then $44^2 = 1936$.

By extracting the middle two digits, 93 and performing the remainder step we get $(93 \bmod 11) = 5$

Item	Remainder	Mid-Square
54	10	3
26	4	7
93	5	9
17	6	8
77	0	4
31	9	6

Separate chaining: (N/D - 2019)

⑥

The idea is to make each cell of hash table point to a linked list records that have same hash function value.

Simple hash function as "key mod 7" and sequence of key as,

50, 700, 76, 85, 92, 73, 101

Fig 1:

0	
1	
2	
3	
4	
5	
6	

Empty Table

0	
1	
2	
3	
4	
5	
6	

Insert 50
(50 mod 7)
= 1

0	
1	
2	
3	
4	
5	
6	

Insert 700 & 76
(700 mod 7) = 0 76 mod 7 = 6

0	700
1	50 → 85
2	
3	
4	
5	
6	

Insert 85
(85 mod 7)
= 1

Collision occurs
add to chain

0	700
1	50 → 85 → 92
2	
3	
4	
5	
6	

Insert 92
(92 mod 7)
= 1

Collision occurs
add to chain

0	700
1	50 → 85 → 92
2	
3	73 → 101
4	
5	
6	76

Insert 73 and 101
(73 mod 7) = 3
(101 mod 7) = 3

Open Addressing:

Open addressing is a method of collision resolution in hash tables.

$$h_0(\text{key}) = (\text{key} \bmod \text{array size})$$

With this method a hash collision is resolved by probing (or) searching through alternate locations in the array until either the target record is found.

(*) Linear probing

(*) Quadratic probing

(*) Double hashing.

Operations:

⇒ Insert (key)

⇒ Search (key)

⇒ Delete (key)

Linear probing:

In which the interval between probes is fixed - often set to 1.

Quadratic probing:

In which the interval b/w probes increases linearly (hence, the indices are described by a quadratic function).

Double hashing:

In which interval b/w probes is fixed for each record but is computed by another hash function.

Linear probing

(7)

Let us consider a simple hash function as

"key mod 7" and sequence of key as,

50, 700, 76, 85, 92, 73, 101.

0	
1	
2	
3	
4	
5	
6	

Empty Table

0	
1	50
2	
3	
4	
5	
6	

Insert 50

0	700
1	50
2	
3	
4	
5	
6	76

(700 mod 7)
= 0

(76 mod 7)
= 6

Insert 700 and 76

0	700
1	50
2	85
3	
4	
5	
6	76

(85 mod 7)
= 1
Collision
occurs

Insert 85

Collision occurs

Insert 85 at
next field.

0	700
1	50
2	85
3	92
4	
5	
6	76

Insert 92

0	700
1	50
2	85
3	92
4	73
5	101
6	76

Insert 73 and 101

If collision occurs on the particular index field
Insert the element on next of the index
field.

Quadratic Probing

$$h_i(x) = (\text{Hash}(x) + i^2) \% \text{Hash table size}$$

key: 7, 36, 18, 62 and use Hash table size as 11.

0	
1	
2	
3	
4	
5	
6	
7	7
8	
9	
10	

Insert 7
(7 mod 11)
= 7

0	
1	
2	
3	36
4	
5	
6	
7	7
8	
9	
10	

Insert 36
(36 mod 11)
= 3

0	
1	
2	
3	36
4	
5	
6	
7	7
8	18
9	
10	

Insert 18
(18 mod 11)
= 7

0	62
1	
2	
3	36
4	
5	
6	
7	7
8	18
9	
10	

Insert 62
(62 mod 11)
= 7

Double Hashing:

$$h_i(x) = (\text{Hash}(x) + i * \text{Hash}_2(x)) \% \text{Hash table size}$$

$$H_1(\text{key}) = \text{key} \% \text{table size}$$

$$H_2(\text{key}) = M - (\text{key} \% M)$$

m is the prime number < table size

q: 37, 90, 45, 22, 17, 49, 55

Table size = 10

0	
1	
2	
3	
4	
5	
6	
7	37
8	
9	

Insert 37
 $= (37 \bmod 10)$
 $= 7$

0	
1	
2	
3	
4	
5	
6	
7	37
8	
9	

Insert 90
 $(90 \bmod 10)$
 $= 0$

0	
1	
2	
3	
4	
5	45
6	
7	37
8	
9	

$45 \bmod 10$
 $= 5$

0	90
1	
2	22
3	
4	
5	45
6	
7	37
8	
9	

Insert 22
 $(22 \bmod 10)$
 $= 2$

0	90
1	17
2	22
3	
4	
5	45
6	
7	37
8	
9	

Insert 17
 $= (17 \bmod 10)$
 $= 7$

0	90
1	17
2	22
3	
4	
5	45
6	
7	37
8	
9	49

Insert 49
 $(49 \bmod 10)$
 $= 9$

0	90
1	17
2	22
3	
4	
5	45
6	55
7	37
8	
9	49

Insert 55
 $(55 \bmod 10)$
 $= 5$

$H_2(17) = 7 - (17 \bmod 7)$
 $= 7 - 3$
 $= 4$

$H_2(55) = 7 - (55 \bmod 10)$
 $= 7 - 5$
 $= 2$

Rehashing:

Rehashing is the process of re-calculating the hashcode of already stored entries (key value pairs) to move them to another bigger size hash map when load factor threshold is reached.

Load factor: It is a measure, "tells what load, hash map can allow elements to put in it before its size is increased."

Steps:

- 1) Create a large table.
- 2) Create a new hash function.
- 3) Use the new hash fun to add the existing data items from the old table to the new table.

Rehashing Techniques:

- 1) Linear probing
- 2) Two-pass file creation
- 3) Separate overflow area
- 4) Double hashing
- 5) Synonym chaining
- 6) Bucket Addressing
- 7) Bucket chaining.

Eg: 13, 15, 24, 6 : Table size = 7.

$$\text{Hash function } h(x) = x \bmod 7.$$

Linear probing with i/p 13, 15, 24 and 6.

0	6
1	15
2	
3	24
4	
5	
6	13

$$(13 \bmod 7) = 6$$

$$(15 \bmod 7) = 1$$

$$(24 \bmod 7) = 3$$

$$(6 \bmod 7) = 0.$$

After 23 is inserted,

0	6
1	15
2	23
3	24
4	
5	
6	13

$$(23 \bmod 7) = 2.$$

\therefore Table is 70% full
so new table is created,
with size 17.

\therefore New hash function is then,

$$h(x) = x \bmod 17.$$

The old table is scanned, and elements
6, 15, 23, 24, 13 are inserted into the new table.
This entire operation is called as rehashing.

Open Addressing hash table after rehashing.

6, 15, 23, 24, 13

0	
1	
2	
3	
4	
5	
6	6
7	23
8	24
9	
10	
11	
12	
13	13
14	
15	15
16	

Rehashing is expensive operation with running time $O(N)$

Extendible hashing:

Used when the amount of data is too large to fit in main memory and external storage is used.

N records in total to store
M records in one disk block.

In ordinary hashing several disk blocks are examined, to find an element, a time consuming process.

Idea:

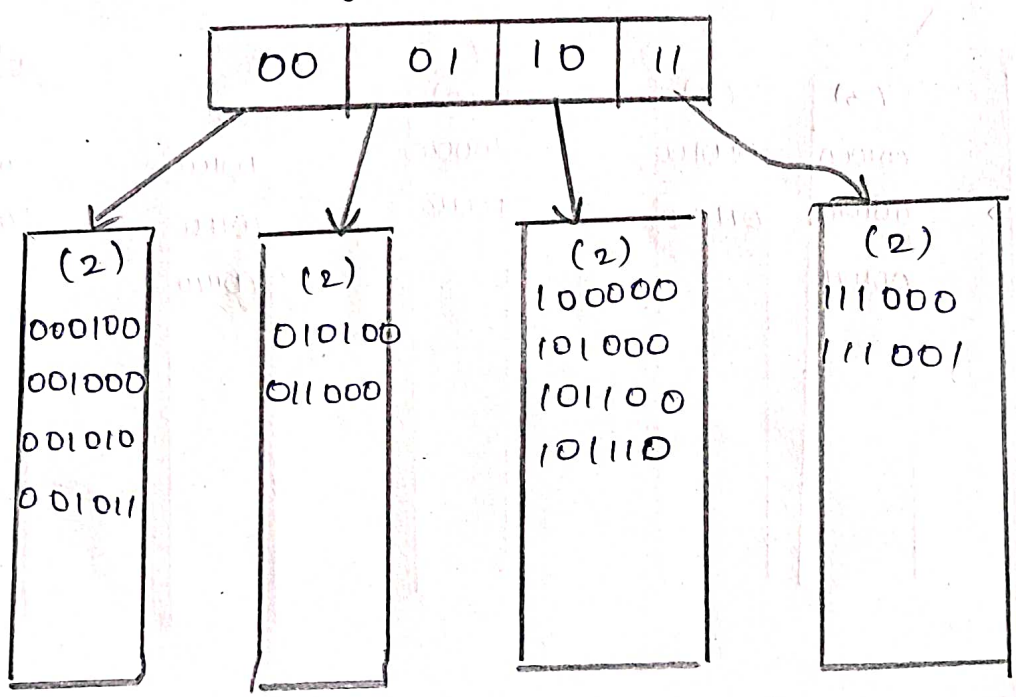
Keys are grouped according to the first m bits in their code.

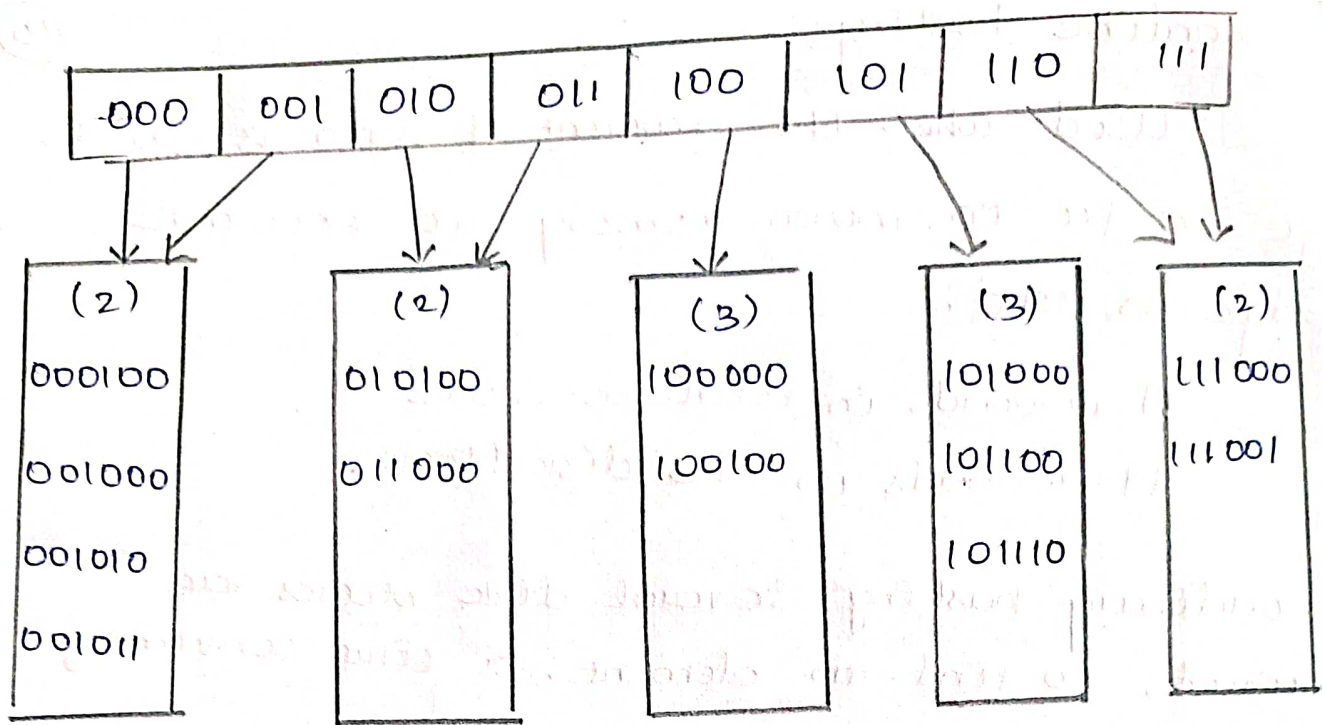
Each group is stored in one disk block.

Eg: Suppose data consists of several six-bit integers.

Each leaf has up to M=4 elements.

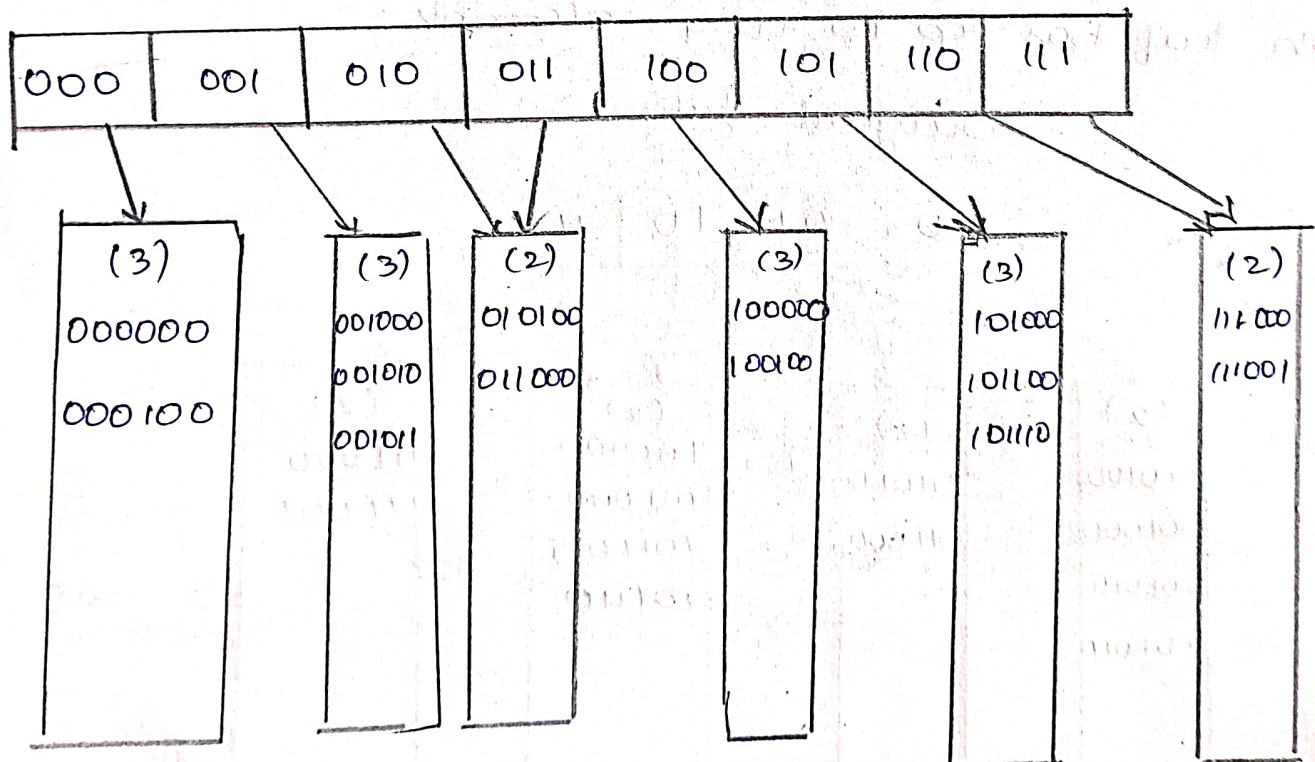
Original data.





Extendible hashing after insertion of 100100 and directory split.

Extendible hashing after inserting of 000000 and leaf split



Searching, Sorting and Hashing Techniques.

Searching: It is an operation (or) a technique that helps finds the place of a given element (or) value in the list.

(*) Linear search (or) Sequential search.

(*) Binary search.

Linear search: (or) Sequential search:

It is a very simple search algorithm. In this type of search, a sequential search is made over all items one by one.

Steps: 1) Starts from the leftmost element of arr[] and one by one compare x with each element of arr[].

2) If x elements matches with an element, return the index.

3) If x doesn't match with any elements, return -1.

0	1	2	3	4	5	6	7
65	20	10	55	32	12	50	99

search(12)

(12) \Rightarrow Both not match. Move to next element

0	1	2	3	4	5	6	7
65	20	10	55	32	12	50	99

(12)

0	1	2	3	4	5	6	7
65	20	10	55	32	12	50	99

(12)

0	1	2	3	4	5	6	7
65	20	10	55	32	10	50	99

(12)

0	1	2	3	4	5	6	7
65	20	10	55	32	12	50	99

(12)

0	1	2	3	4	5	6	7
65	20	10	55	32	12	50	99

(12)

Both are matching. So we stop comparing.

Advantages:

- 1) The linear search is simple.
- 2) It does not require the data in the array to be stored in any particular order.

Binary search:

Binary search, is also known as half-interval search, is a search algorithm that finds the position of a target value within a sorted array.

I/P: 65, 20, 10, 55, 32, 50, 99.

0	1	2	3	4	5	6	7	8
10	12	20	32	50	55	65	80	99

search(12)

(Arranged in ascending order)

0	1	2	3	4	5	6	7	8
10	12	20	32	50	55	65	80	99

↑
(12)

$8/2 = 4$
 $7/2 = 3$

Search element (12), compared with middle element (50)
 $12 < 50$. So search only in the left sublist
 (10, 12, 20, 32)

0	1	2	3
10	12	20	32

$5/2 = 2$

$$\textcircled{2}$$

0	1	2	3
10	12	20	32

(12)

$$3/2 = 1$$

0	1	2	3	4	5	6	7	8
10	12	20	32	50	55	65	80	99

Search(80)

$$80 > 50$$

5	6	7	8
55	65	80	99

5	6	7	8
55	65	80	99

7	8
80	99

7	8
80	99

↑
80

Both are matching. So element 80 is found at Index 7.

Advantages:

⇒ faster, because does not have to look at every element.

Disadvantages:

⇒ This alg. requires the list to be sorted.

Sorting:

Sorting refers to arranging data in a particular format. It specifies the way to arrange data in particular order.

⇒ Bubble sort

⇒ Selection sort

⇒ Insertion sort.

⇒ Shell sort

⇒ Radix sort.

Bubble Sort:

Bubble Sort is a simple sorting algorithm.

This sorting alg. is comparison-based algorithm in which each pair adjacent elements is compared and the elements are swapped if they are not in order.

Eg: 14, 33, 27, 35, 10

14, 33, 27, 35, 10 [14 < 33 Already sorted no swap]

14, 33, 27, 35, 10 [33 > 27, so swap it]

14, 27, 33, 35, 10 [33 < 35. Already sorted]

14, 27, 33, 35, 10 [35 > 10, so swap it]

14, 27, 33, 35, 10 [33 > 10, so swap it]

14, 27, 33, 10, 35 [27 > 10, so swap it]

14, 10, 27, 33, 35 [14 > 10, so swap it]

10, 14, 27, 33, 35 [Last Iteration]

And when there is no swap required, bubble sort learns that an array is completely sorted.

Selection Sort:

Selection sort is a simple algorithm. This sorting algo. is in-place comparison based algorithm in which the list is divided into two parts, the sorted part at the left end and the unsorted part at the right end.

Initially, the sorted part is empty and the unsorted part is the entire list.

(3)

14	33	27	10	35	19	42	44
----	----	----	----	----	----	----	----

The whole list is scanned sequentially.

14, 33 27 10 35 19 42 44 (swap)
 \uparrow min.

we replace 14 with 10.

10 | 33 27 14 35 19 42 44
 (sorted) \uparrow min

10 33 27 14 35 19 42 44

After swapping two least values are positioned.

10 14 | 27 35 19 42 44 (swap it)
 Sorted \uparrow min

10 14 19 | 33 35 27 42 44 (swap it)
 Sorted. \uparrow min

10 14 19 27 | 35 33 42 44 (swap it)
 Sorted. \uparrow min

10 14 19 27 33 | 35 42 44 (NO need swapping)
 Sorted \uparrow min

10 14 19 27 33 35 | 42 44
 Sorted. \uparrow min.

Sorted order is

10	14	19	27	33	35	42	44
----	----	----	----	----	----	----	----

Insertion sort:

This is an in-place comparison-based sorting algorithm.

Steps: 1) If it is the 1st element, it is already sorted. return 1.

2) Pick next element

3) Compare with all elements in the sorted sub-list

4) Shift all the value elements in the sorted sub-list that is greater than the value to be sorted.

5) Insert the value.

6) Repeat until list is sorted.

Original	34 8 64 51 32 21	position moved.
After P=1	8 34 64 51 32 21	1
After P=2	8 34 64 51 32 21	0
After P=3	8 34 51 64 32 21	1
After P=4	8 34 51 32 64 21 8 34 32 51 64 21 8 32 34 51 64 21	3
After P=5	8 32 34 51 21 64 8 32 34 21 51 64 8 32 21 34 51 64 8 21 32 34 51 64	4

No. of elements : 6

$n-1 : 6-1 \Rightarrow 5$ passes.

Merge Sort:

↳ Merge sort is sorting techniques based on divide and conquer techniques.

↳ Complexity $O(n \log n)$

↳ It divides the array into equal halves and then combines them in a sorted manner.

Merge sort works:

14	33	27	10	35	19	42	44
----	----	----	----	----	----	----	----

Divide into equal array (4)

14	33	27	10
----	----	----	----

35	19	42	44
----	----	----	----

Divide into array (2)

14	33
----	----

27	10
----	----

35	19
----	----

42	44
----	----

Divide into single array

14

33

27

10

35

19

42

44

Combine each element : 14, 33

14	33
----	----

10	27
----	----

19	35
----	----

42	44
----	----

10	14	27	33
----	----	----	----

19	35	42	44
----	----	----	----

10	14	19	27	33	35	42	44
----	----	----	----	----	----	----	----