Department of Civil Engineering

Regulation 2021 III Year – VI Semester CE3602/ Structural Analysis –II

UNIT-I

INTLUENCE LINES FOR DETERMINATE BEAMS

Definition:

An influence is a graph showing, For any given beam, Frame or Bitmes, the variation of any Torce or displacement quantity (such as shear force, bending Moment,) For all position of a moving unit load as it crosses the structure from one unit load as it crosses that structure from one end to the other.

Problems 1:

A single rolling boad of tookn moves on a girder of span som. a) Construct the influence lines for shear force and bending moment for a section "5m" from the left support. b) Construct the influence lines for points at which the absolute Max shear and absolute max bending moment Mox shear and absolute max values.

Sola:

a) To Find Mase Shear fore and Bending Moment at 5m from the Left Support

Influence lines Diagram for Shear Force

It oxdinate to the right of D

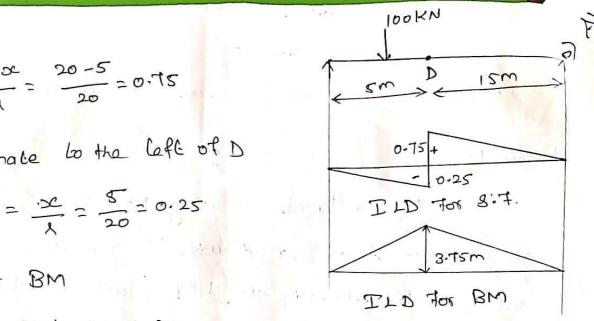
= 1-x

$$\frac{2}{100} = \frac{100}{20} = 0.75$$

II ordinate to the left of D

IL For BM

= 3.75m



Max positive Shear Force = load x ordinate = 100 x 0.75

= 75KN (+)

Max Negative Shear Force = hoad x Ordinate

= 100×0-25

= 25 KN E)

Mase Bending Moment

= load x ordinate

= '(00X3.75

= 375KNm.

>b) Absolute Masc Shear Horre and Bending Moment

for Stear Force.

II ordinate al 1. A

Il ordinate at B.

$$\frac{20}{20} \approx 1$$

It ordinate at BM. at Midspan

$$=\frac{1}{4}=\frac{20}{4}=5$$

Positive Shear Force.

= load x ordinate

= 100%

= (OOKN (+)

Megalive Shoor Force

= load xordinate

1 x001 =

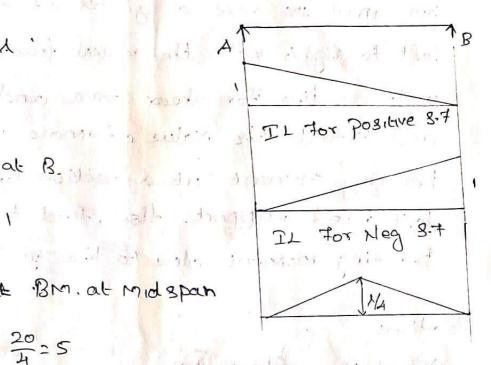
= tookn (-)

Absolute maximum BM

= load x ordinate

= 00X'S

= 500 KNM.



to sales of the sales of

7

Two point boods of lookn and 200kn span 3m apart are cross a girder of span 15m from the left to right with the lookn load leading. Draw the influence line for shear force and benching moment and & find the value of max shoar force and benching moment benching moment at a section D. 6m from the left hand support. Also, Find the absolute max bending moment due to the given load system.

Solution:

a) Tend Max Shear Force.

Shear inexeament.

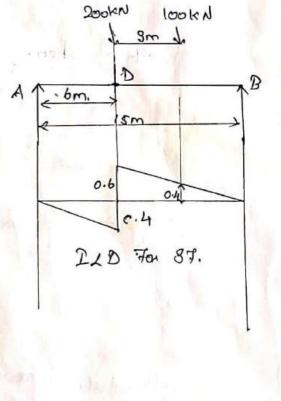
$$3i = \frac{Wc}{\lambda} - Wi$$

$$= \frac{300}{15} - 200 = -180$$

(i) Positive Show Force.

$$\frac{1-3c}{3} = \frac{15-b}{15} = 0.6$$

$$\frac{3c}{3} = \frac{6}{15} = 0.4$$



Ordinate under 200KN 20.6

0 x d crate Under 100 KN = 0.4

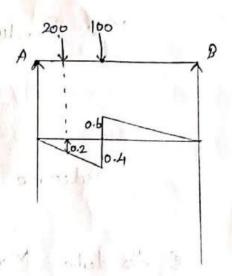
Max positive Shear Force = (200x0.6) + (00x0.4)

Shear increament.

$$3i = \frac{We}{1} - W_1$$

$$= \frac{300 \times 3}{15} - 100$$

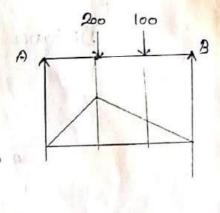
$$= -40'.$$



Ordinate under 200KN =
$$\frac{0.4}{6} \times 3$$

= 0.2

Find cribical load



$$=\frac{200}{6}-\frac{100}{9}=22$$
 (4ve)

D. C.

Ordinate under look
$$N = \frac{3.6}{9} \times 6 = 2.4 \text{ m}$$

Taking Moment about 200 KN

Distance of this 200 KN From a.

8m

Max ordinate under 200KN =
$$(2-x)x = 8x7 = 3.73m$$

Absolute Mosc Bending Mornant = (200×3.73) +(100×2.33)
= 979.3 KNM

Problem No: 3

A brain of 5 wheel loads crosses a 38 beam of 3pan 22.5m. Using influence lines, calculate the Max positive and regulive shear forces at mid span and absolute move bending moment anywhere in the 3pan. We was we wis 240 km.

Solution.

a) Max Shear Force.

Lind Shear crereament.

$$3i = \frac{We}{l} - W_1 = \frac{1180 \times 2.5}{22.5} - 120 = 11.11 (40e)$$

Ordinale under 400KN.

ordenate under 260 KM

$$= \frac{0.5}{11.25} \times 6.25 = 0.27$$

ordinate under 240 km

ordenate under 120 kN

Max positive Shear Force

(ii) Negative Shear Force.

Find Shear increament

120 KN 160 400 260 240

DLD for St

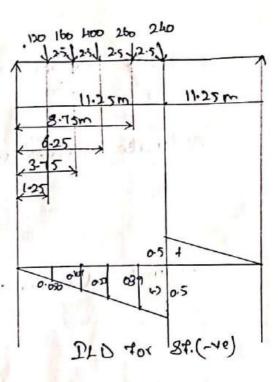
ordinale under 200 KN

Ordenate under 400 km

$$=\frac{0.5}{(1.25)}\times6.25=0.27$$

ordinate Under 160 km.

Ordinate Under Izoka



Max Negative Shear force &

b) Absolute Max Bending Moments
120 160 400 260 240
12.51, 2.51, 2.51, 2.51

Taking Moment about 120 km

$$(160\times2.5) + (400\times5) + (260\times7.5) + (2610\times210) = 2.56$$

$$120 \quad 160 \quad 400 \quad 260 \quad 240 \quad 6750 \quad 180 \approx 1.2.5$$

$$10.89 \quad 636 \quad 036 \quad 10.89$$

Ordenate under =
$$5.62$$
 160
 10.89 $\times 8.39 = 4.33$

Ordenate under 120 km

ordinate Under 260 km

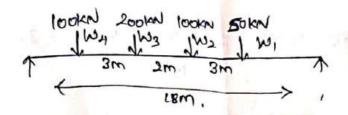
ordinate under shown

= 120(3.0W +160 (4.33). + 400 (6.62)+260 (4.41)+(240+3.2)

PROBLEM: 4

A ginder having a span of 18m 19 99 20th the ends. It is traversed by a train of loads as shown in Figure. the sound load leading, Find the maximum Bending Moment Which can occur (i) under the 20010N load (ii) Under 50KN load, using influence line diagrams.

rebuilt almaker



Solution.

Mars Bending Moment 100 200 100 50

(1) Under 200KM load

Resultant foods = 100+200+ 100+50

=450 KN

Teiking Moman & about W4. 100km 200 100 50km

(200×3)+(00×5)+(50×8) = R50

1500 = 450 50 56 = 3.33m Ordinate Max = ochow = 9(9)

. Distance between c and 200km = Dist Bln. c and R

8.335

3.52

Ordinate under jooky = 4.5 8.835 x 5.835 = 2.97

Ordenate under workn

TV.

BM und 200 KN load

(ii) Bendeng Moinant under soku load

Centre of 19 pain to BM. Equial Distince

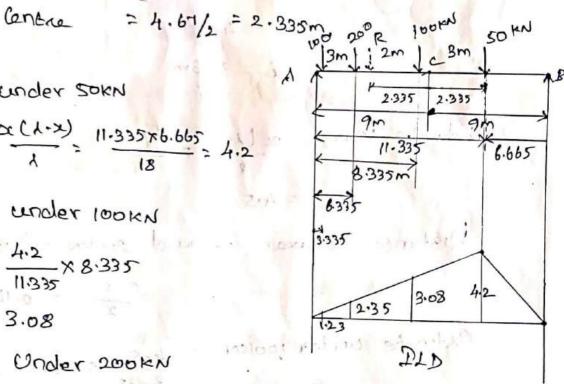
Ordenate under SOKN

Ordenate under looky

- 3.08

Ordinate Under 200KN

Ordenate Under looken $=\frac{4.2}{11.335}\times3.335=1.23.$



PROBLEM: 5

Using the relevant influence line diagrams, Find is The max bending Moment, (ii) the max positive and Negative shear at Am from the left support of a 38 girder of span 10m. When a train of 4 wheel loads of 10km, 15km, 30km, 30km, Spaced at 2m, 3m, 3m respectively, class the 3 pan with the low load leading.

Problem: b

Draw the influence Line Diagram For Shear Force

and Bending moment for a section at 5m from the Left

and Support of a simply Supported beam, 20m long. Hence

beautiful the max Bending Moment and shear force

at the section, due to an uniformly distributed rolling load of length sm and intensity lokalin run.

Solution.

10km/m

10km/m

10km/m

20m.

- a) Maximum Shear Force.
 - (i) Positive Shear fora.

Ordinate under C,

$$=\frac{0.75}{15} \times 7 = 0.35$$

MaximumPosibre Shear Force

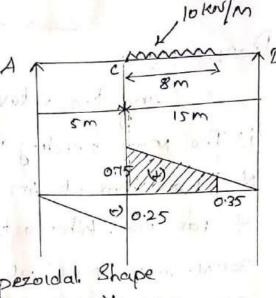


$$=\frac{3c}{\lambda}=\frac{5}{20}=0.25$$

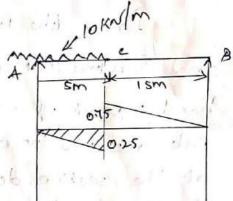
Max Negative Shear Force

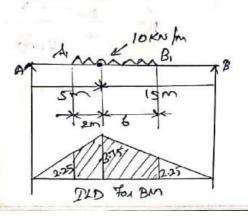
= 6.25 KN.





(atb) K isin = LAKNA 10KM/m





max ordinate =
$$\frac{x(1.x)}{1}$$
 = $\frac{5(15)}{20}$ = 3.45m
ordinate under A_1 = $\frac{3.75}{5}$ $\times 3$ = 2.25m
Ordinate under B_1 = $\frac{3.75}{15}$ $\times 9$ = 2.25m

Max Bending Moment
$$= \frac{10 \times \left[(2.25 + 3.75)^2 + (2.25 + 3.75)^6 \right]}{2}$$

= 240 KNM.

Four Equal loads of Isokn each equally PROBLEM: 7 spaced at 2m apart followed by a U.D.1 of Go KN/m at a distance of 1.5m . from the Last 150km load across a girder of som span from Right to left Using influence lines. Calculate the shear force and bending moments at a distance em From the left hand Support, when the leading ISOKN load is at ism from the left hand

Support: 150 150 150 150 60 km/m

a) glass Force out this section

Positive Shear Horce

ordinate Under 'c' left

Ordinate under '7'

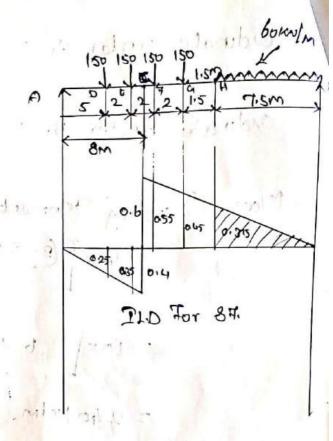
ordinate under a

Ordinate under H

ordinate under E

orginate ander D'

to sin bust Shear Force at 2 = -(50 x 0.25) - (50x 0.35) +(150x 0.55) +(150x 0.45) + (60 x 1 7.5 x0.3 45)



3) Bending Moment For Caren load position

Max Ordinate at 'c'

$$=\frac{x(\lambda-x)}{\lambda}=\frac{8(12)}{20}=4.8$$

ordinate under E

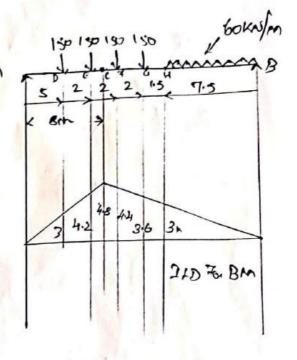
ordinate under D

Ordinate cender it!

ordinate under 'a'

ordinate under . H

Bending Moment at C



UNIT-I

INTLUENCE LINES FOR INDEPERMINATE STRUCTURES

Muller Breslau Principle:

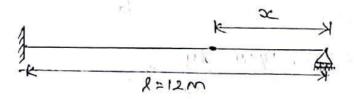
It states that, if we want to sketch the influence line for any force quantity (like Bhear, reaction, Bending Moment) in a generative.

* We remove from the structure the restraint to that force quantity

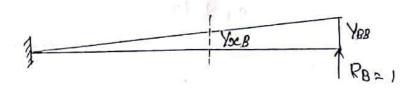
* We apply on the remaining schucture a unit displacement corresponding to that force quantity

PROBLEM 1:

Draw the influence line for reaction at B and that support moment MA at A for the propped cantilever as shown in Fig. Computes the It oxidinales at 1.5m intervals.



Solution:



When RB=1, YxB is displacement at or Section. due to unit load applied at B

Integrating on both sides

$$\frac{GQ}{dx} = -\frac{xe^2}{2} + 4$$

Again Integrate on Both sides

$$0 = -\frac{12^2}{2} + 0$$

$$\begin{array}{rcl}
Sub & 52:12, & 4:29 & 10 \\
0 & -123 \\
\hline
b & +123:12 + C2
\end{array}$$

$$\begin{array}{rcl}
0 & -576 + C2
\end{array}$$

$$\begin{array}{rcl}
C_2 & -576
\end{array}$$

AL DE: 0

ILO and FOR RB at X

$$-X = \frac{7 \times B}{Y_{BB}} = \frac{1}{EL} \left[-\frac{\times^3}{5} + 72 \times -576 \right]$$

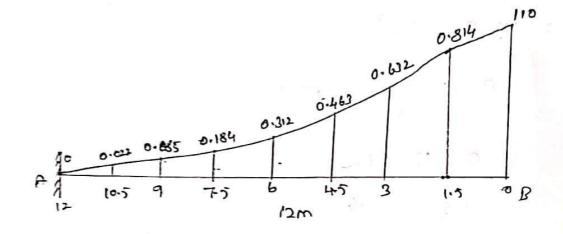
$$-\frac{576}{EL}$$

$$= \frac{-\infty^{3} + 72x - 576}{5}$$

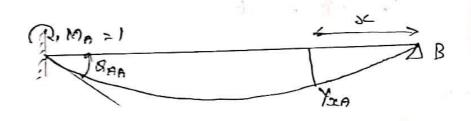
Pa - 20 - 12

Orderates of ILD for RB at 1-5m intervals.

2 (m)	0	1.5	3	4-5	6	7.5	q	10.5	12
RB	١	0.814	0.632	o.463	0.312	0.184	0.085	0.022	0.0



We have to apply a unit rotation at 1.



$$M_{\infty} = -ET \frac{d^2y}{dx^2}$$

$$\frac{\dot{z}}{12} = -EDd^2y$$

$$\frac{dx^2}{dx^2}$$

$$\frac{dx^{2}}{2} = -\frac{x}{12}$$

Integrale on Both sides

Main Incegrate:

16.000,400 x=12, 4=0

21 -

Henre C220, C122,

$$\frac{Q_{\text{BA}}}{z_{\text{A}}} = \frac{dy}{dx} = \frac{1}{\text{ED}} \left[-\frac{3c^2}{24} + 2 \right]$$

$$Q_{AA} = \frac{1}{ED} \left[-\frac{12^{2}}{24} + 2 \right]$$

$$= -4$$

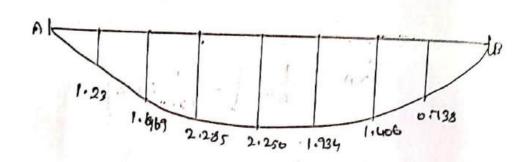
When we divide Your by DAA We get the Ito at se

$$\frac{1}{2} = \frac{1}{2} + \frac{1}{2} = \frac{1}{2}$$

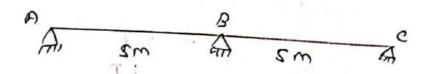
$$\frac{1}{2} + \frac{1}{2} = \frac{1}{2}$$

Ordenaces of the IFD for MA at 1.5m.

sc(m)	0	1.5	3	4.5	6	7.5	9
IYO	0	-07138	-1.406	-1934	-2.290	-2.185	-1.069



PROBLEM 2: Determine the influence line For Ra Fr. Continuous beam shown in Fig. Compute the DL Oldinates at Im intervals.



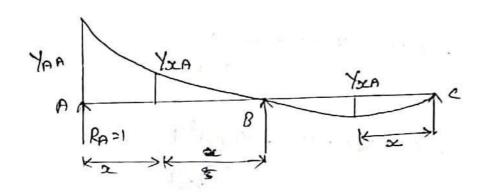
2 Solution

(i) Remove Support A.

(ii) Apply a unit Torce at it and compute the deflection at any "x" on co and BA.

(iii) Divide these deflections by the alisplaceme

Elastic curre due la RA=1.



Taking Moment about C.

$$1x - 2(x - 6) = -\frac{d^2y}{dx^2} EE$$

$$-x + 2x - 10 = EDd^2y$$

$$-x + 2x - 10 = EDd^2y$$

$$de^2$$

Intergrate on Both side

$$EPdy = -\frac{x^2}{2} + 2x^2 - 10x + c,$$

Again integrate on Both side

$$ERY = -\frac{x^3}{6} + \frac{x^3}{3} - 10x^2 + C_1x^2$$

$$EEY = -3e^{3} + 3e^{3} - 53e^{2} + Cext$$

Apply conditions scro, yro

$$0 \Rightarrow 0 = -5^3 + .5^3 - 5(5)^2 + .6.1 \times 5 + 0$$

Apply adcz.

$$\sqrt{xA^{2} + \frac{1}{EE} \left[-\frac{x^{3}}{6} + \frac{x^{2}}{3} - 5x^{2} + 20.83x + 0 \right]}$$

At 30= 10

$$Mx = -d^2y$$
 dx^2

Integrale on Both side:

$$\frac{\text{EPdy}}{dx} = -\frac{x^2}{2} + c_1 + 2kx - 5)^2$$

Endy =
$$-x^2 + (x-5)^2 + (1)$$

Again Integrale Both side

EIY =
$$-\frac{x^3}{6} + (\frac{x-5}{3})^3 + (1x + c_2)$$

a) x=0, y=0

(ii) x25, y20.

Apply C, & Cz.

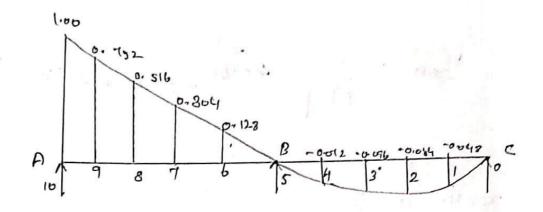
$$= \frac{1}{61} \left[-\frac{20}{6} + 4.167 \times + (2x-5)^{3} \right]$$

$$= \frac{1}{61} \left[-\frac{20}{6} + 4.167 \times + (2x-5)^{3} \right]$$

$$\frac{1}{4} \left[\frac{1}{2} + \frac{1$$

De orderate at ILD for RA

1	عد(س)	Support	1	2	3	4/	Japone	6	o . H	8	ام!	Supar
	DLO (RA)	0	-0.048	-0,084	or 096	- ০ -এ১	0	0-128	0 - 128	0-304	6.516	c 1



PROBLEM:

Using Muller Breslau Principle, alraw the influence line for bending Moment out the Mid-point of span AB of the continuous beam ABC shown in Figure Determine the influence line ordinales at suitable. Intervals and plot them.

Solution.

To get the enfluence line for MD

- (i) Introduo a hurge at D.
 - (ii) Apply a unit bendery knowent at D.
 - (iii) Determina the Markinsonie deflection you and to Slope ADD at D.
 - (10) You is the influence line ordinate at any or

Berding Mounant out any oc is

Mac: -EI d29 +0183300 +1010.

0.333x -0.555(x-6) = -EDd29

ED 227 = -0.333 x 40.552 (oc-b)

Integrale on both sides

EPdy $\frac{1}{2} + 0.555(x-6)^2$

ET dy

-0.1665 x2 +0.2715 (x-6)2 434

Again integrale on both sides:

EIU = 20033 - 0.1665003 + 0.2275 (2-6)3

EDY =-0.0222x3 +0.0922+61x+c5

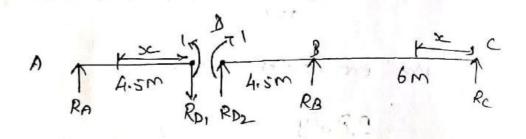
the second of the second

Find Ra, PB, Rc, Ro, Roz

Malab.

RAYA.5 =1

RA=1 =0.222 KN



RD, = 0.222 1

RD2 = 0-9921

Taking Moment about c.

0.222×10.5 +17 RBX6 =0

RB 7 -0.555 KN

RA + RB + Rc = 0

0.222 + -0.555 + Rc 20

Rc = 0 333 KM

Two regions AD and DBC will be considered separatively (because of aliscontinuity at D).

(i) x=0, y=0,

Apply Cides in Slope of Deflection Values.

$$4 = \frac{1}{EI} \left[-0.0555 \left(10.5^{3} \right) + 0.0925 \left(10.5 - 6^{3} \right) + 2 \left(10.5 \right) + 2 \left(10.5$$

Flor the zone AD M=1-0.222x Er deg don2 = 0.222x-1 Integrale on Both sides EP dy = 0.222 x2 -x+c3 Ezdy

Ezdy

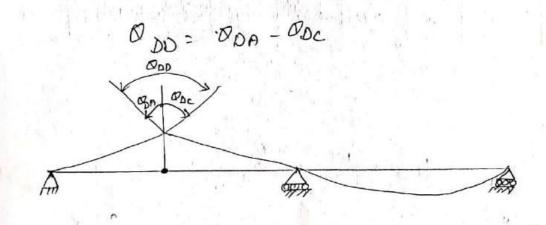
Ezdy Again Docegeale on Both side. EDY = 0.111 x2 = x2 + C4 EZY=0.03722 -22 Boundary Conditions.

(i) sc=0, y=-34.82

ED 2 + C3 x + C4 - B @=> -34.82 EZ =0.037 (0) ~0 +0 +e4

Apply C3 d C4 in B

$$3 \Rightarrow ED \frac{dy}{dx} = 0.222 \left(sc^{2} \left(\frac{1}{2} \right) - x + 9.24 \right)$$



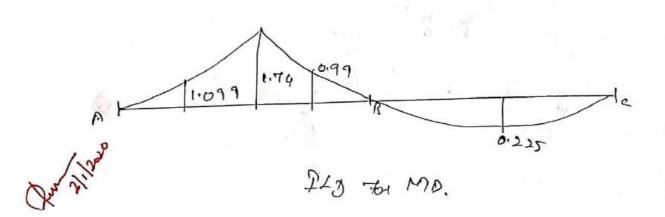
for the region cD,

$$ILO \cdot 401 \text{ PD} = \left[\frac{6!222 \times 3}{6 - \frac{5c^2}{2} + 9.24 \times -3432} \right]$$

$$19.973$$

Influence leve ordinate:

er (w)	0	3	6	9	10.5	12	15
140	0	0.225	0-0	-0.799	-1-743	-1.099	0



Arches:

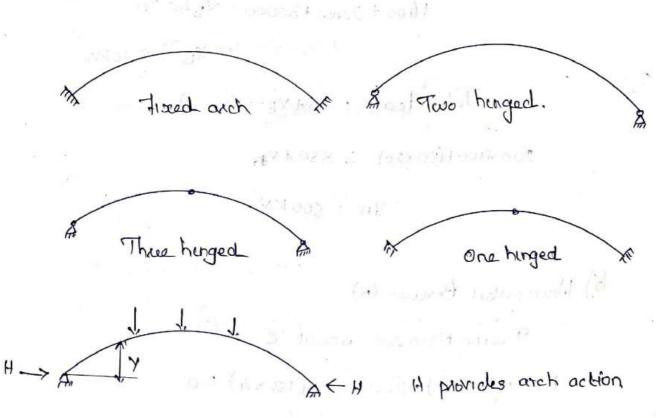
Arches are shaped to take the load above them and develop only compression. Arches to develop bending mornent. and shear too.

Arches can be:

- * Crecular
- * Parabolic
- * Polygoral
- * Ellybical
- * Any other curved shape.

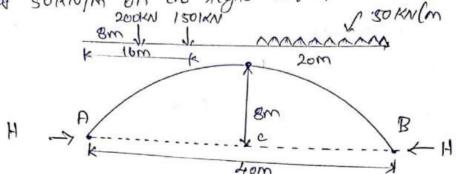
Arches can be build of mosonry, RCC ox steel.

Hinges in Anches.



BISOBLEM 1:

A 3 hunged such of span Aom and rise on load of 200KN and ISOKN OF Carries concentrated distance of 8m and 16m from the left end and an udd of sokn/m on the right half of the span.



Solution!

a) Vertical Reactions VA and VB

Taking moment about it,

(200 KB) + (150 x 16) + (50 x 20 x (20+20/2)) - VB 40 =0

1600 + 2400 + 30000 - VB 40 =0

NB = 850KN

Total load = YA+ YB

200 +150+(50x20) = 850 + VA

JU = 200 KN

b) Hoxizontal Chrust (H) Taking Moment about 'E' HX8-VA(20) +(200x12) +(150x4) =0 84 - 4000 + 2400 +600 =0

H = 325KN

I have the same of the same

PROBLEM 2:

A parabolic 3 hinged arch corries loads as

Shown in Fig. Determine the resultant xas reactions at

Supports. Find Bending moment, normal thrust, and radial

Shown at D, sm. from A. What is the mass bending moment

 $B \rightarrow A$ $A \rightarrow A$ A

Solution:

Vertical Reactions. Vn and VB

Taking Moment about 1.

(20x3) +(30x7) +(25x10x L10+10/2) - VBx20 =0

18 2 201KN

V'A = 99 KN

House (H)

(HX5) + (20×7) + (80×3) - VAKIO =0

5H+140+90 -990 20

H = 122KN

Resultant reactions (. RA and RB)

$$PB = \int_{H^{2}+VP^{2}} = \int_{IS2^{2}+QQ^{2}} = (81.39KN)$$

$$PB = \int_{H^{2}+VB^{2}} = \int_{IS2^{2}+20I^{2}} = 252KN$$

$$PB = \int_{IH^{2}+VB^{2}} = \int_{IH^{2}+VB^{2}} = \int_{IH^{2}+VB^{2}} = 252KN$$

$$PB = \int_{IH^{2}+VB^{2}} = \int_{IH^{2}+VB^{2}} = \int_{IH^{2}+VB^{2}} = 252KN$$

$$PB = \int_{IH^{2}+VB^{2}} = \int_{IH^{2}+VB^{2}} = \int_{IH^{2}+VB^{2}} = \int_{IH^{2}+VB^{2}} = \int_{$$

Bending Mornent, Mormal thruse., radial 37 at D

Bin at 1 2

Slope of the arch at D.

$$0 = \tan^{-1} \left[\frac{4x}{2^2} \cdot (x - 2x) \right].$$

$$0 = \tan^{-1} \left[\frac{4xs}{20^2} \cdot (20 - 2xs) \right].$$

$$0 = 26^{\circ} 33^{\circ} 55^{\circ} \cdot 18.$$

Scanned by CamScanner

Mormal Etrase:

You - Nec beam Shoan force.

P=79800 26 33 55". 18. + 152 cos 26 33 55". 18 =171-28

Radial Shear Force.

Max BM in CB.

$$BM_{3c} = V_{8x} - W_{3c}^{2} = 144x$$

$$4x^{2} + 4x + 3x(1-3c)$$

$$= \frac{4x}{20^{2}} \times 3x(20-3c)$$

$$= 0.05x(20-x)$$

$$Mx = 201x - 25xx^{2} - H(0.05x(20-x))$$

$$= 201x - 12.5x^{2} - 7.6x(20-x)$$

$$= 201x - 12.5x^{2} - 152x + 7.6x^{2}$$

$$Mx = 49x - 4.9x^{2}$$

Diff, W. A. G. Sc.

. . BM to be Max

9.82 -49 20

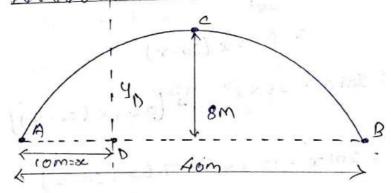
x = sm

Moc = 49(x5) - 4.9(52)

= 122.5KN.

1) Symmetrical three hunged parabolic anch BrobLew 8; of span from and rise 8m convies an U.D. I ey som over the left half of the span. The hinger are pro at the supports and at the centre of arch. Colour the realtions at the supports. Also colculate the bending morrent, radial shear and normal thrust a distance of low from the left support.

nananana 30km/m



Solution:

Vertical Components Va and VB

Taking Moment about 1.

VB = 150 KN

= 450 (CN.

Housental Components.

H =375KN.

Resultant Reactions Rn & RB.

. I to spok.

Bending Moment at tom from 1.

Bending Moment. at com.

= VA (10) - HA(Y) :-30 ×10×10/2

= 450.(10)-(3754) -30(50)

= 3000 - 3754

23000 - 375(6)

2 7 50 KNM

Radial Shear force out x 210m

R= 42 1030-148100

YOL= VA - 30X10

= 450 -300 = 150KN

Slope as D.

 $0 = \frac{4r}{1^2} \left(\frac{4r}{1^2} \left(\frac{1}{1^2} \right) \right)$ $= \frac{4r}{1^2} \left[\frac{4r}{4r^2} \left(\frac{1}{1^2} \right) \right]$

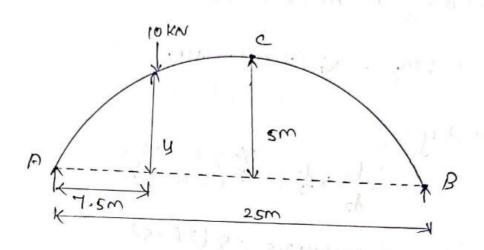
= 21°48'

R. R= 150 C03 21°48' - 375 3cn 21°48'

Normal through.

P= Yor 8cn & +He080 = 1508cn21°48' +375c0821°48' = 403.89 km. oblem 4:

A 3 hinge auch is circular, 25m in 3 from with a central ruise of 5m. It is loaded with a concentrateo load of roken at 4.5m. from the left hand hinge, Find the houizontal Ahrust, Reactions at each end hinge, Banding Moment under the toad.



Polution

Vertical Reactions. VA & UB

Taking Moment about d.

VBX25 - 10x7.5 =0 118 = 3KN

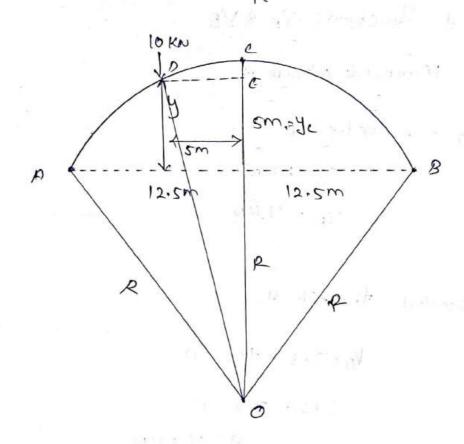
House thrust. H

VBX12.5 -HX5 = 0 3x12.5-45=0 H=7. SKN Reactions RA and RB.

Bending Moment Under the load.

fond y:

$$\frac{1}{12.5\times12.5} = \frac{1}{12.5\times12.5} = \frac{1}{12.5\times$$



18.125 = (18.125-5+4)+52

303.515=(13.12574)2

17.44 = 13.12549

y= 43m.

BMD: 7(+5)-7.5(4.3)

= 20, 25 KNM

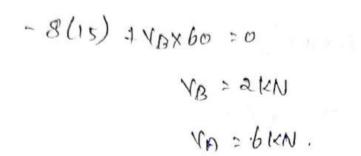
PROBLEM 5:

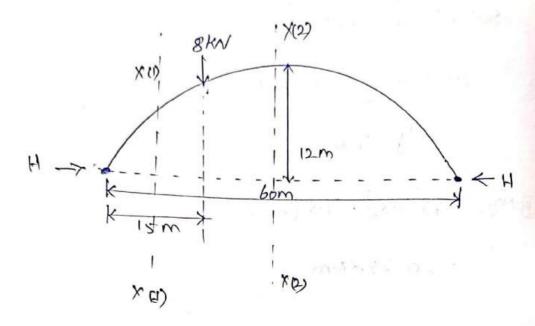
A parabolic anch hunged at ends has a gpan of bom and a rise of 12m. A concentrated load of 8kN act at 15m from the left tringe. The second thornant of area varies as the seccent of the credination of anch axis. Calculate the horizontal thrust and the reactions at the hunge. Also calculate the net bending mornent of the section.

Solution.

Vertical Reaction: Mn &MB.

Taking Moment about it.





Horizontal Arruse (H)

$$= \int_{0}^{80} \frac{(4\pi)^{2}}{6e^{2}} \times (60-x)^{2} dx$$

$$= \int_{0}^{60} y = (0.8x^{2} - 0.0133x^{2})^{2}$$

$$= 0.64x^{2} - 0.0213x^{2} + (1.76xx^{4})x^{4}$$

$$= \int_{0.64}^{60} \frac{(6.64x^{2} - 0.0213x^{2} + 1.76xx^{4}x^{4})^{2}}{3} dx$$

$$= \frac{0.64x^{3}}{3} - 0.0213x^{4} + 1.76xx^{4}x^{5}$$

$$= \frac{0.64x^{3}}{3} - 0.0213x^{4} + 1.76xx^{4}x^{5}$$

$$= \frac{0.64x^{3}}{3} - 0.0213x^{4} + 1.76xx^{4}x^{5}$$

$$= \frac{1.76xx^{4}x^{5}}{5}$$

$$= \frac{1.76x^{4}x^{5}}{5}$$

$$= \frac{1.76xx^{4}x^{5}}{5}$$

$$= \frac{1.76xx^{4}x^{5}}{5}$$

$$= \frac{1.76xx^{4}x^{5}}{5}$$

$$= \frac{1.76xx^{5}}{5}$$

$$= \frac{1.76xx^{$$

$$= 5400 - 999.84$$

$$= 4400.$$

$$M_{15} = V_{10} \times 2 - 8(x_{2}-15)$$

$$= 6x - 8x + 180$$

$$= \int_{15}^{60} (120 - 2x) (.0.8x - 0.0133x^{2}) dx$$

$$= \int_{15}^{60} (96x - 1.596x^{2} - 1.6x^{2} + 0.0266x^{3}) dx$$

$$= \int_{15}^{60} (0.0266x^{3} - 3.196x^{2} + 96x) dx$$

$$= \int_{15}^{60} (0.0266x^{4} - 3.196x^{3} + 96x^{2}) dx$$

$$= \left[(36184 - 230112 + 172800) - \frac{8}{33}6.6 - 359 + 10800 \right]$$

$$= 21330.9$$

7.5.79 KN

Reactions.

the test to the test of the body that is Max Bending Moment

$$M_{\infty} = V_{A}(15) - H_{y}$$

 $y = 4x_{12} \times 15 \times (60-15) = 9m$

=39.87KNm.

Fored Liches:

Thosed arches are more common than hunged arches,

Analysis of focad archos.

1. Castiglianois theorem

2. Elossia contro marthad

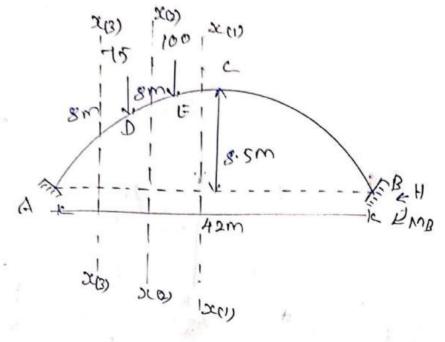
3. Column analogy method.

PROBLEMS:

A parabolic ouch fixed at both en has a span of 42m and a central Hee of 8.5m. DE is subjected to concenerated loads of TSICN and 100 KN at 8m and 16m respectively from the last end. The moment of enertia or the arch sib varies as the secont of the inclin cy rib axis. Analyse the arch and Find the Bending Moment at either support and at the crown.

Solution

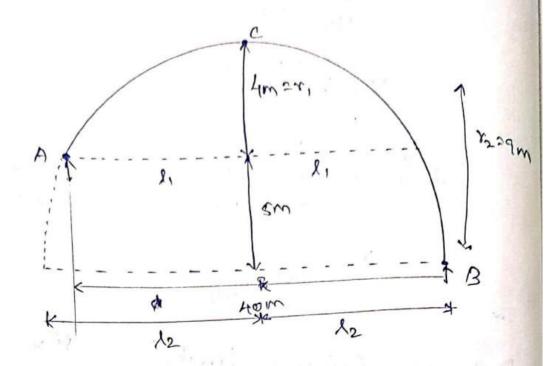
= 0.81x - 0.0192x2



	e e		Mac
Postion	Origin	Limits (m)	1.136
BE	В	0-26	NBOC-HO-MB
ED	В	2-6-34	VBOC-HBY-MB-(x-26)
De	В	34-42	VBX-HBY-MB-{100(2-26)
			-75-(x-34)

PROBLEM: 7

A three hunged parabolic arch of 40m span has abutments at unequal levels. The heighest point of the circh is 4m above the left Support and and 9m above right support abutments. The arch is subjected to an udd of 15 kn/m over its entire horizontal span. Final the horizon tal thrust and bending moment at a point 8m from the left support.



Solution.

Reactions A, B and II.

Find kilz

$$\frac{\chi_1}{\chi_2} = \sqrt{\frac{\chi_1}{\chi_2}}$$

considering leafe side efc. YA (16) - 114) -15416416/5 0 1640-411-1920:0 HVA-H-480-0-0 considering eight side of c. -118(24) 4 H(9) +15×26×26/2=0 -24 NB + 9H+14320=0 -8 VR +3H+1440=0 10+18:900 VB = 600 - VA _ B - (600 - VA) + 3 HA1440 =0 8VA - 600 +3H + 1440 20 8YA +3H - 3360=0 -B Od @ => Jolve P. V. ICKE - HISDA 4NA-H-480:0 8YA-2H-960 1440 VA-3H-480:0 8VA+3H-3360 3360 6 8VA+3H-3360 -XH - 480 = 0 8VP +3H - 3360 -344 - 47 + 1920 = 0 8VP +3H - 3360

H=480KN

Raclial Shear.

$$\theta = \frac{1}{2} \left[\frac{4x4}{(2x16)^2} \left(32 - 2x8 \right) \right]$$

$$= 1402'$$

Normal thrust N at scien

formulas.

SERVICE

5.) Rodial Shoor Force.

6) Three hingood circular onch. Find Radius 'R'

Find y

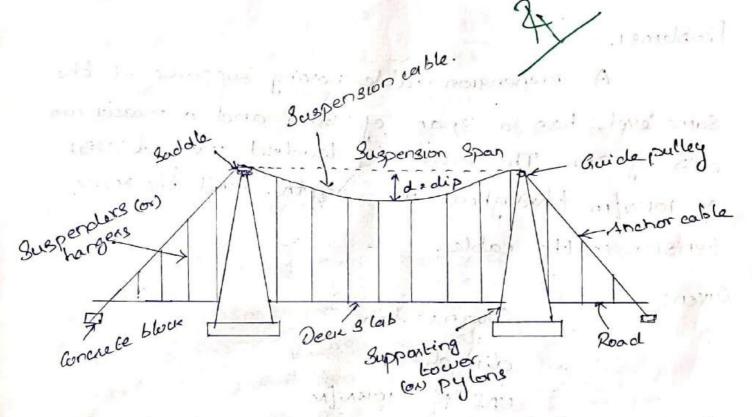
To Two hinged arch

8) Fixed arches.

UNIT-TV

CABLES AND SUBPENSION BRIDGES

Suspension cable. Components and their functions



Suspension Cable: Main load bearing Member flexible, take direct tension only.

Suspenders: Cincler with cleux Blab is
Suspended from the the Buspension
cable, (Ox) hargers, Lianster load
from cleux to suspenders.

Anchor cables. After passing over pylons, cables anchored to the bedrous.

Passing the cable over pylons

(i) Guide Pulley Support.

(ii) Roller (or) Soddle Support.

Anchoraging into a huge mass of concrete.

Problems 1:

A suspension cable having supports at the same level, has a span of som and a maximum dip of 3m. The cable is loaded with a UDL of 10141/m throughout its length. Find the max bension in the cable.

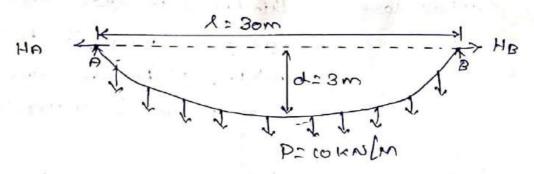
awen:

3 pani= 30m dip d= 3m UD; p' = 10KN/M

To Find

Max tension in the cable

Solution:



Find Verbical Reactions.

VA=VB= PA = 10 x30 = 150KN

Max Tension in cable

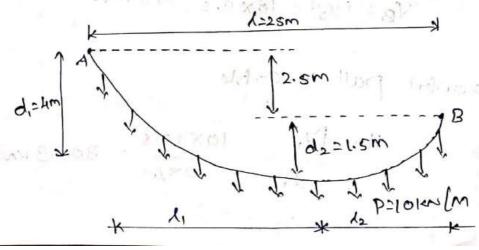
Horizontal pull in the cable

endin I had is

Problems 2:

A suspension cable is supported at two points 25m aport. The left support is 2.5m above the right support. The cable is loaded with a uniformly distributed toad of toknown throughout the span. The mase dip in the cable from the left support is 4m. Final mase and min tension in cable.

aven:



To find

Max and Min Gension in cable.

Solution

Find length li and le

$$\lambda_2 = 9.5 \, \text{m}$$

$$\lambda_1 = \lambda - \lambda_2$$

$$= 125 - 9.5$$

= 15.5m

Vertical Reactions

Horizontal Pull in eable

$$H = P I_{1}^{2}$$
 10×15.5^{2} 2×4 2×4 2×4

Tension in cable.

Max Tension = 337.9 KN

Min Tension: 300.3KN

1 5 4 65206...

Problem 3:

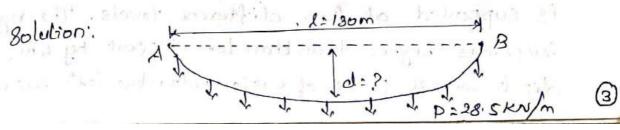
A suspension cable of 130m horizontal Span is supported at the same level. DC is subjected to a uniformly distributed load of 28.5 km/ hoursontal Metre. If the max tension in the cabbe is limited to soookN. Calculated central dip Meedled.

Given data:

8pan 1=130m UD1 P= 28.5 KN/M Tmax = SODOKN

To find

Central Dip.



Vertical Reactions:

Horizontal pull (tensio).

Max Tension

$$T_{\text{NOIX}} : \sqrt{2} + H^2$$

$$5000 = \sqrt{185^2 \cdot 5^2 + \left(60206.25\right)^2}$$

$$5000^2 = 1852.5^2 + 60206.25^2$$

$$5.95\times10^{-3} = \frac{1}{4^2}$$

PROBLEM 4:

A suspension cable of hoursontal span 95m is supported at two different levels. The right support is higher than than Left support by 4m. The dip to Lowest point of cable below the left support

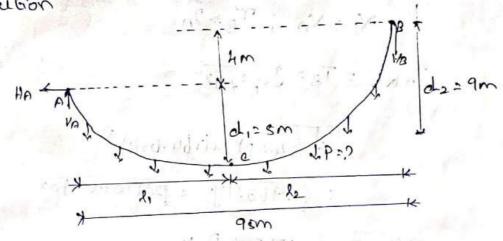
sm. The cross sectional orea of the cable is soomm? Find the uninformly distributed load that can be carried by the cable if the max stress in is limited to boo N/mm?

Given data:

Span 2=95m d= 3500mm² Stress ==600 Nlmm².

To find Uniformly Distributed load."

Solution



Find length

$$\frac{l_1}{l_2} = \sqrt{\frac{d_1}{d_2}}$$

$$\frac{1}{12} = \sqrt{\frac{5}{9}}$$

$$A = 1.4$$
 $A = 0.745$ $A = 40.56$ $A = 0.745$ $A = 40.56$ $A = 4$

Merbical Reactions

Horizontal Pull.

$$H = \frac{PR^2}{2d} = P(.54.4)^2 = 164.4 P.$$

Maxe tension will occur at right support

$$T_{\text{mood}} = T_{\text{B}} = J_{\text{VB}}^2 + H^2$$

$$= J_{\text{C4.4P}}^2 + (164-65P)^2$$

$$= \sqrt{2963.71} \sqrt{P^2 + \sqrt{27109.62}} \sqrt{P^2}$$

Mm² x mm

P= 12110 N/M

ROBLEMS: 5

A cable of horizontal span 21m is to be used to support six equal loads of 40kN each at 3m spacing. The control dip of the cable is limited to 2m. Find the length of the cable required and also its sectional area if the safe censile stress is 450 N lmm².

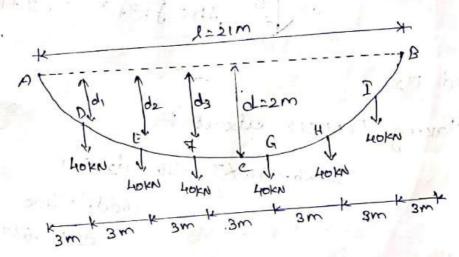
Given data:

Span 1:21m dip d'=2m 5=750 N/mm²

To Find

Longth of cable
'Sectional Area

Solution.



Vertical reaction

and - Evall - Carrier

Horizontal Pall.

Tailing Moment about 'c'

VAXIOS - 40x 7.5 - 40x4.5 - 40x1.5 - HX2=0

120 ×10.5 - 540 - 2H =0

-120 = 2H

H= 360KN.

Find D.

Taking Moment about D.

120×3 - 360×d1=0

$$AD = \sqrt{\frac{b}{b^2 + c^2}} = \sqrt{3^2 + i^2} = 3.16m$$

Find de

Taking Mornent about E

120x6-40+3 -360xd2 =0

360d2 = 600

d2=1.667m

 $c d_{2} - d_{1} DE = \int b^{2} + c^{2} = \int 3^{2} + 0.667^{2} = 3.073 \text{ m}$

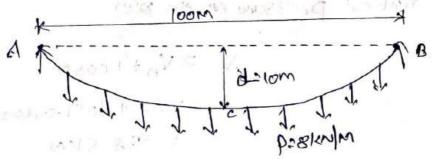
Find obs

Taking Moment about 7 120×9-40×6-40×3-360×d3=0

Area

HOBLEM! 6

A suspension cable of Span loom and dip 10m carries a uniformly alistributed Load of skn/m of housantal Span over the full span. Find the vertical and how sontal forces bransmitted to the supporting pylons.



- a) If the cable is passed over a smooth pulley
- b) If the cable is clampled to a gaddle with rollers of the top of the piens. The anchor cable makes 30 to the horizontal at the pylons.

Given data:

MAKEI

8 pain laworn

dip d = 10m

P= 8KN/M.

Q = 30°

Solution:

Yestical Reactions:

VA= VB : PR = 8x100 = 400KN

Induizontal pull

Tension in cable.

a) · Anchor cable · passing over pulley.

Ventrical prossure em on pier

Housental force at lops of pylon.

.= H- TSIND

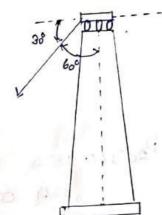
= 1000-\$ 1077 gin 600

= 67.29 KN.

b) Cable passing over saddle support

MIZER T, = H/ Sen 600 1000

TO LOUIS AND SHE SHIT KN



Verbical pressure

The second of the second second

= 400 + 1154.7 Cosbo

- 977.35KN

PROBLEM: 7

A suspension cable of horizontal span 210m is Supported the at the same level and has a central dip of 20m. Find the increase in alip of the carble if the cable is subjected to a rise in temperature cy 28°C. Take &= 12 K10-6 per °C.

aven data:

Span Larrow d = 20m £=28°C L = 12×10 6 per °c Solution.

Change on dip.

$$312 \times 10^{2} \times 12 \times 10^{6} \times 28$$

$$= 3 \times 210^{2} \times 12 \times 10^{6} \times 28$$

$$= -0.138m.$$

$$= 138mm.$$

Brobrem : &

A cable supported at the same level on either 81 end is of 140m hoursontal span with a central dip of 14m. It carries a load of 15km/m on the hoursontal span. Calculate the change in the hoursontal tension when the temperature rises through 28°c. Co. efficient of linear expansion of the eable materials. I = 4 xiob./°c.

Given data: of the sales and and a

Span 1-140m.

0=14m.

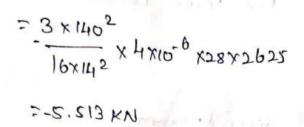
P=15KN/M

L=28°C

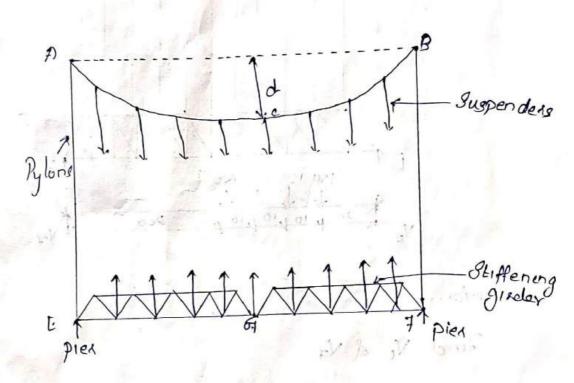
x=4x10-6/0c

Solution

Change in housental tension.



Suspension BRIDGES WITH THREE HINGED STITZENING. GIRVERS.



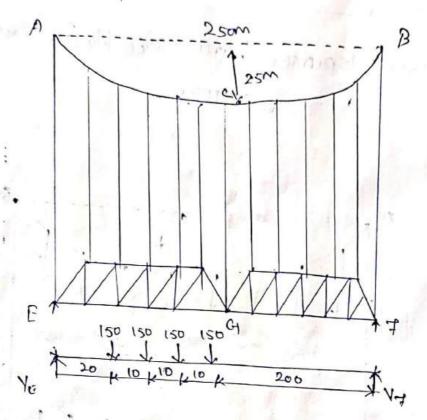
PROBLEM!8.

A. Suspension bridge of 250m 3pan has two nos. of three hinged stiffening girders supported by cables with a central clip of 25m. If 4 point loads of 300kN each are placed at the centre line of the roadway at 20m, 30m, 40m and 50m from the left hand hinge. Find the shear force and Bending moment in each girder at 62.5m From each end

calculate also the max tension in the cable.

Given data:

Span 1=250m dip'di = 25m



Solution:

Find Ve & V4

Taking Moment about 7'

Ve x250 - 150x 200 - 150x210 -150x220-150x230=0

Total load = Ve + V+

600 = 516 + K4 1 100 00 01 10

14 = 84KN

Housental buil

a) Bending Moment

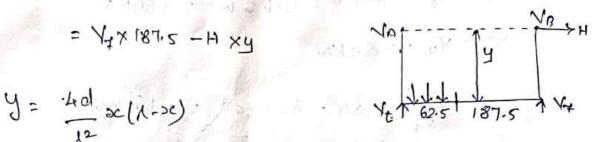
BM @ .62.5m From left hand heize

= 18.75m

Bm @ 62.5m (13/10) (1) 10. 11/11 (1)

BM @ 62.5 From Right hand hinge

87 @ 62.5 From legs hand hinge



$$\tan B = \frac{4d}{R^2} (1.2 \times 2)$$

$$= \frac{4 \times 25}{250^2} (250 - 2 \times 62.5) = 0.2$$

tana : 0.2

ND = NE - 4X120 = 516 = 600 = -84KN

V= -84 - 420 x0.2 = -168KN

87 @ 62.5 From Right Side

8th & Vist. = - V+ H banco

= -84 +420 x0.2=0

c) Vertical pull on the eable.

H= . Px2

 $420 = P \times 2.50^2$ 8×2.5

P= 1.34 KN/M

d) More tension in cable

JANEAR MA

JORNA OLMS:

Buppart at Same Level.

2. Suppose at different level

$$H = P l_1^2 + H = P l_2^2$$
 $1 = 2 d_1^2$

$$\frac{l_1}{l_2} = \sqrt{\frac{l_1}{d_2}}$$

3. Mase Tension

5. Cable passing over pulley

Vertical pressure = VA+TCOBB

Horizontal Horce = A-Tamo

6. Cable passing over saddle.

W

Vertical pressure = V+T, coso 1.T, = H 3000

7. Charge in dip. (on increau in dip

old: 312 26.

8. Charge in horizontal Tension

DH= -322 2 + H

9. Three hunged problems.

H= Me

y= 4d sc(1-sc)

87 @ left = Yb - Htano

87 @ Right = Hlance - Vb

PLASTIC ANALYSIS

Définition.

Plastic Hinge:

Tully plastic moment is considered to have develop at any section of a structure subjected to a system of loads, When the section is completely yielded of plastified.

Plastic hunge is defined as an yielded zone due to bending in a structural member, at which large rotations can bake place at a section of a constant plastic moment. Mp.

and sould become

Types of Mechanism.

- 1. Beam Mechanism
- 2. Panel Mechanism (ox) Sway Mechanism
 - 3 Gable Mechanism.

Static mathod or Virtual Inlor Mathod

This knethool is based on the states that Static on lower bound theorem. Which states that A load computed on the basis of an assumed equilibrium BM diagram in which the mornants are not greater than Mp.

Load Factor:

PROBLEM 1'.

A beam of span bon is to be designed to an ultimate U.D.L of 25 KN/m. The beam is so at ends. Design a suitable I. section using plastic theo assuming of = 20 H/mm²

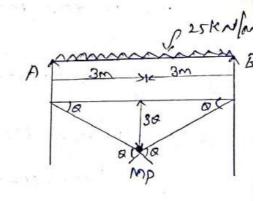
promissing 6m.

Goldtion:

Internal Work Done

= 0+ MP x28 +0

= 2MPQ.



Exchernal Kloric Dona

= Load intensity x Area of under triangle.

$$= 25 \times (\frac{1}{2} \times 6 \times 30)$$

= 225 8

Equating E T. W.D = E.W.D

Scanned by CamScanner

$$Zp = \frac{Mp}{\sigma} = \frac{1125 \times 10^6 \text{ Nmm}}{250} = 4.5 \times 10^5 \text{ mm}^3$$

$$3 = \frac{ZP}{Z}$$

$$Z = \frac{ZP}{S} = \frac{4.5 \times 10^{5}}{1.15} = 391.304 \times 10^{3} \text{ mm}^{3}$$

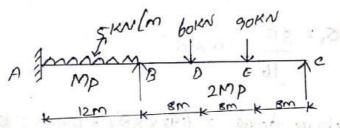
PROBLEM 2:

A continuous Beam ABC is loaded as shown in

My ore Virgelin

Figure. Determine the required Mp it the load factor

ig 3.2.



Solution.

TRANSPORT FRANCIS

Mechanism . T.

External Work Done = 16x [1/2×12×60]

= 8760 -0

Internal Work Done

= &Mp+(mp x20) + Mp0

= 4Mpa-0

Equating O of 3

STER = LMPO

MP= 576 = 144KNM

Medanism-II

Mp

288Kg

Mechanism - II

Excernal Wark done = (192×80) + (288×80)
= 15360 + 2304×0.50
= 15360 + 11520
= 26880.

Internal Work Done = $Mp \otimes + 2Mp (\otimes + 0,) \neq +0$ = $Mp \otimes + 2Mp (\otimes + 0.5 \otimes) +0$ = $Mp \otimes + 2Mp (1.5 \otimes) = 4Mp \otimes$

Scanned by CamScanner

Exceed = Internal

2688 @ = 4Mp8

Mp= 2688 = 692KMM.

Mechanism II

External Work Done = (19288160) + (288x160) . = 61440

Internal Work Done:

= MPB +2MP(B+B)

 $\therefore \ \, \mathcal{O}_1 = \frac{160}{8} = 20.$

= Mp Q + 2Mp3Q

= MPR+6MPR

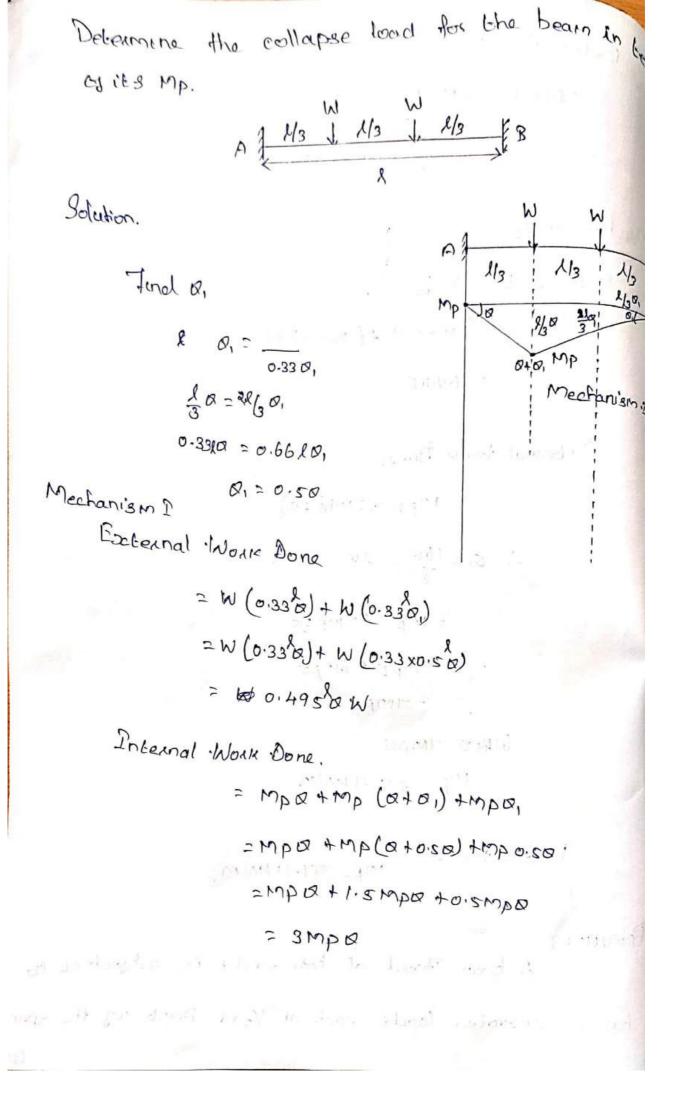
= JINPO

MP= 8777 KNM.

Plastic Moment: Mp=877.71 KN/m.

PROBLEM 13

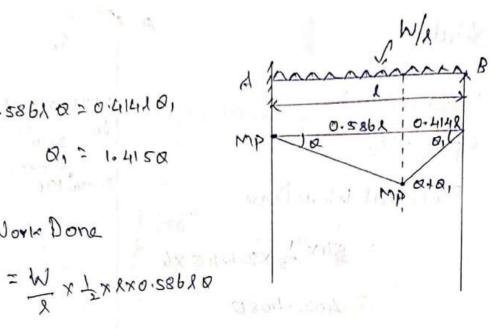
A beam Thread at both ends is subjected to two concentrated loads, each at Y3rd Point 'of the span.



ROBLEM: 4

Analyse the propped cantilorer loaded as Shown and decermina the collapse load A Jamananana B

Solution.



Excernal Work Done

Internal Work Done

PROBLEM S!

A two span continuous beam abe has span ilongth . AB: bm, Bc: bm, and coursies a box 3012N (m completely covering the span AB and Be A and a completely covering the span AB and Be A and a come is . If the iloud factor is 1.80.9, Shape ifactor is 1.15 ifor the I. Section. Find a section inodulus headed. Assume yield stress for the modulus headed. Assume yield stress for the material as 250 N/mm²

Solution.

Mechanism I.

Span . AB.

Exclernal Work Done

= 54x 12x2-484 0x6

= 402.4080

2.4840= \$ 3.5160,

0, 20,7060

2. 484. Mp

0.41441 0.5861

Internal Work Done

= Mp(a+0,)+mp0,

= Mp(&+0,060)+mp0,060

= 2.412mpa

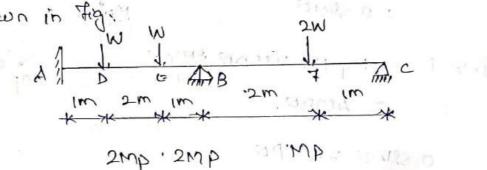
$$Zp = \frac{Mp}{\sigma y} = \frac{166.8 \times 10^6}{250} = 667.2 \times 10^3 \text{ mm}^3$$

$$3 = \frac{ZP}{Z}$$

$$Z = \frac{Zp}{8} = \frac{667.2 \times 10^3}{1.15} = 580.18 \times 10^3 \text{ mm}^3$$

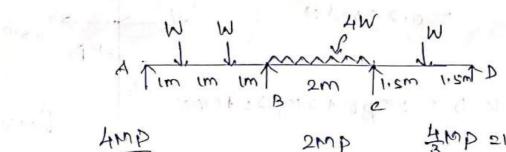
50Bren: 6

Debeurine the collapse load of the beam load as shown in Fig.



PROBLEM: 7

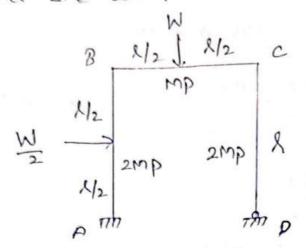
Find the collapse load We for the continuous beam shown in fig: The bearn has uniform plastic moment mp.



4MP 21,33MP

LEGBICIN: 8

Find the collapse load for the frame.



Solution.

(i) Beam Mechanism.

2 0. SXIN 0

I. W.D = MpB+ 2mpB+mpB

O. SIND ZUMPR

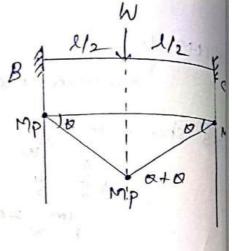
MB. M = 8Wb

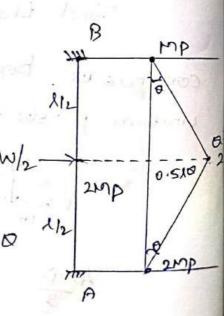
(ii) Colum Mechanism.

E.W.D = W. LoseR)

= 0.25W10

D.W.D = 2mp0+2mp20+mp0





0.25 W/B = 7MPB

Charles to be per

(iii) Panel Mechanism. (Bway Mechanism)

$$E.W.D = W/2 \times 20$$

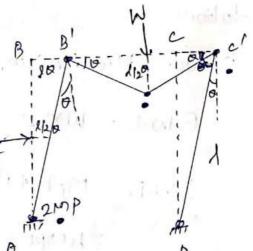
$$= 0.25W10 W/2 + 11200$$

$$= 10.25W10 W/2 + 11200$$

$$= 10.25W10 W/2 + 11200$$

I. W.D = 2mp& +mp.o+mp& A = 4mp&

(iv) Combined Mechanism.



I.W.D = 2Mp & + mp (0+0) + mp (0+0)

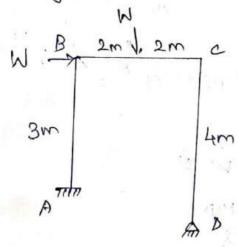
= 6Mp &

0:15 W. a = 6mp &

W = 8mp

PROBLEM: 9

Determine the collapse load for the for Shown in Figure, Mp 13 the same for all members



Solution:

i) Beam Mechanism.

E.W.D = WXZB

IW.D = Mpx+mp2x+mpx

 $\frac{1}{2m} \frac{2m}{mp} \frac{1}{mp}$

2WB = 4MPB

(ii) Sway Mechanism

E. W.D = 1230.

I. W.D = Mpattapa +mpo,

30 =40,

0,=0.730

= Mpa+ mpa +onsomp

= 2.75 MP Q

W30=275MP0

W= 0-916MP

ii) Combined Mechanism.

E.W.D: 30W+ W20

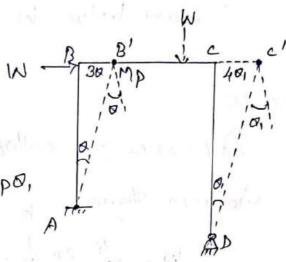
= 5WB

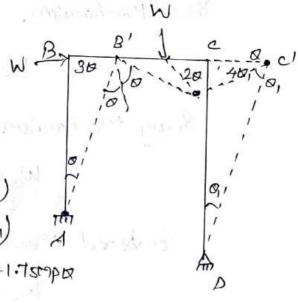
I.W.D = Mpa+mpla+a)

+ MP(0+01)

= Mp 04 2mp 0 + 1.75mp 0

= 4.75 MPB





5 WO = 04.7519PD

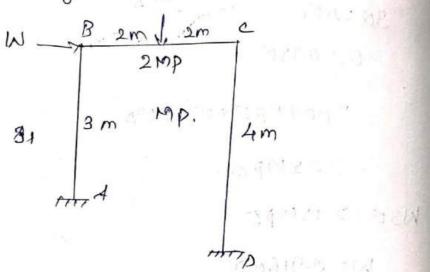
W=09.5MD.

. . Leage Value W: 0.916Mp.

PROBLEM: 10:

Decemene the collapse load. For the Too

as shown in Figure. W



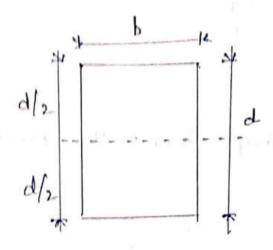
Beam Mechanism.

Sway Mechanism.

We = 7/6Mp Combined Mechanism We = 1.5Mp

OBIEM 11:

Tind Shape Tanton The Rectangular section



30/ ulton.

$$= \frac{bd}{2} (d/4 + d/4)$$

$$= \frac{bd}{2} (\frac{1}{2}d)$$

$$= \frac{bd^2}{4}$$

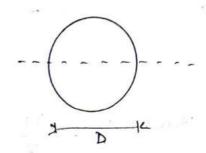
$$2 = \frac{\Gamma}{y}$$
 . $\frac{1}{2} = \frac{6d^3}{12}$

$$Z = \frac{5d^{3}}{12} \times \frac{2}{d} = \frac{5d^{2}}{6}$$

$$3 = \frac{bd^{2}}{4} = \frac{bd^{2}}{4} \times \frac{b}{bd^{2}} = 1.8.$$

Brobrew 15:

Find Shape Factor For circular section



Solution:

$$8 = \frac{7P}{2}.$$

$$\frac{7P}{2} = \frac{4}{2}(\hat{y}_{1} + \hat{y}_{2})$$

$$= \frac{4P}{4} = \frac{2P}{3\pi} + \frac{2P}{3\pi}$$

$$= \frac{7D^{2}}{8} = \frac{2P}{3\pi} + \frac{2P}{3\pi}$$

$$= \frac{7D^{2}}{8} = \frac{4P}{3\pi}$$

$$= \frac{D^{3}}{6}$$

$$= \frac{D^{3}}{6}$$

$$= \frac{D^{3}}{6}$$

$$= \frac{17D^{4}}{4} \times \frac{2}{D} = \frac{77D^{4}}{32}$$

$$= \frac{77D^{4}}{4} \times \frac{2}{D} = \frac{77D^{3}}{32}$$

Shape Factor
$$8 = \frac{7p}{7} = \frac{5}{6}$$

$$= \frac{5}{6} \times \frac{32}{5}$$

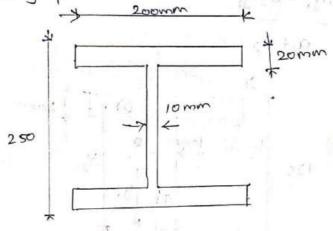
$$= \frac{5}{6} \times \frac{32}{5}$$

$$= \frac{5}{6} \times \frac{32}{5}$$

$$= \frac{5}{6} \times \frac{32}{5}$$

ROBLEM 18:

A mild steel I section 200mm wide and 250mm deep has a mean flange thickness of somm and a web thickness of room. Calculate the shape factor. Find the fully plastic moment if oy= 252 N/mm2.

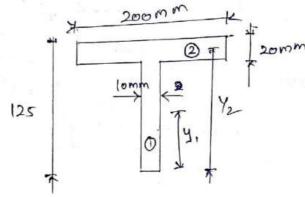


3dution.

Shape Factor
$$3 = \frac{ZP}{Z}$$

$$T = 200 \times 250^3 - 190 \times 210^3 = 113.78 \times 10^6 \text{ mm}^4$$

Plastic Section modulus.



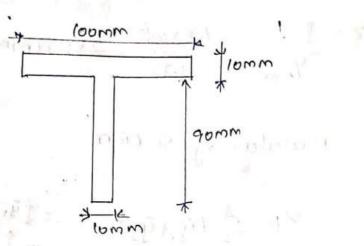
$$3 = \frac{ZP}{Z} = \frac{1.03 \text{ mob}}{910.27 \text{ mob}} = 1.13$$

fully plastic moment.

Mp= Gy x Zp = 252 x1.03x106: 259.6x10 Nmm

watern 14:

Find the shape factor for the Tee Section. as

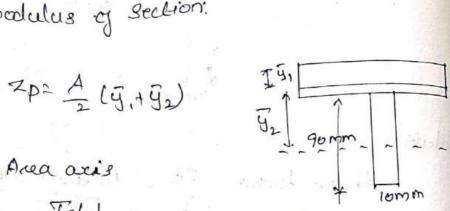


Solution

Etaglic Modulus. Z.

Plastic modulus of section:

Equal Area axis



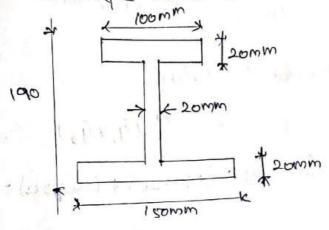
$$\frac{y_1}{2} = \frac{4.15mm}{100\times0.5} \times \frac{y_1}{2} + \frac{\alpha_2}{100\times0.5} \times \frac{y_2}{2} + \frac{\alpha_2}{100\times0.5} \times \frac{y_2}{100\times0.5} \times \frac{y_2}{$$

01x0P+5.0x 00)

=43.12mm

fobten 12;

Find the shape Factor of the I. Section.



Solution:

Location of controid

Morney extoneors about pop.

(100 r20) + C150r20) + C150r20)

2105.6mm

Moment of Incitio.

I = 100x203+[.100x20x(105.6-10)2]+ 20x103

x (105.6-95)2+ 150x203 (20x150) x (84-4.

= 4101-35×104 mm4

Z = 4101.35 x104 105.6 = 388.39 X103mm3

Playlic Section Modulus

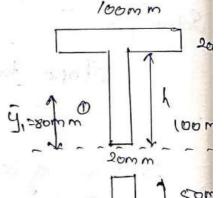
A= (100 x20) + (150 x20) + (150 x20) = 8000 mm2

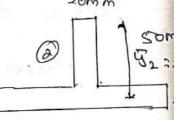
8000 = (100×20) + 20×h

20 h= 2000

h= 100mm.

J, = (100 x 20 x 50 + 100 x 20 x 100+10) (100x20) + (100x20)





= 80mm,

J2 2 (20 × 50 × 25) + 1 50× 20× (50+10) (20x20) + (120x20)

= '51,25mm

$$Zp = \frac{8000}{2} \left[80.1 \text{ 51.25} \right] = 525 \times 10^{3} \text{ mm}^{3}$$

 $S = \frac{Zp}{Z} = \frac{525 \times 10^{3}}{388.39 \times 10^{3}} = 1.35.2$

Jamalas:

I. W.D = Based on Bupport.

gs at Ends is Mo pimp is absent fixed Support inpis present

E.W.D for UDL = Load x Area . cy Exicingle. E.W.D for point = Load x Lerm.

2)
$$\sum_{i=1}^{\infty} z^{i} = \sum_{j=1}^{\infty} y^{j}$$

Rectangular.

A=bd, G=d/4, I=bd3, y=d/2

$$A = \frac{710^2}{4}$$
, $\bar{y} = \frac{20}{311}$, $\bar{I} = \frac{710^4}{64}$, $y = 0/2$

Equal Prea axis.

who to analy it done

Dur 2/1/20